

# EMI attenuation in a DC-DC buck converter using GaN HEMT



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**Abstract**—A dc-dc buck converter using gallium nitride (GaN) high electron mobility transistors (HEMT) is experimentally investigated at the discontinuous current mode (DCM) and at the triangular current mode (TCM) operation. The paper objective is to specify the power conversion efficiency and attenuation of common mode (CM) and differential mode (DM) noise voltage, measured at the line impedance stabilization network (LISN) for compared control strategies. Zero voltage switching achieved for the TCM operation improves efficiency with reference to the DCM operation. However, significant attenuation of electromagnetic interference (EMI) spectra is obtained for TCM operation with capacitive snubber. Sizing of capacitor snubber dependent on parasitic inductances of commutation circuit and rapid switching of GaN HEMTs are illustrated.

**Index Terms**—Buck converter, triangular current mode (TCM), zero voltage switching (ZVS), electromagnetic interference (EMI), gallium nitride high electron mobility transistor (GaN HEMT)

## I. INTRODUCTION

EXTENSIVE development of wide-band gallium nitride (GaN) power transistors reveals new horizons in converter design achieving increased operation frequency, higher power density, lower switching and conduction losses [1], [2]. Particularly, superiority of the GaN high electron mobility transistor (HEMT) in cascode structure over silicon MOSFET and IGBT technologies has been proved in a number of comparative research tests carried out for buck-boost dc-dc converters [3] or inverter configurations [4], [5]. In order to properly exploit high frequency switching ability of GaN HEMT devices, the design objective of an ultralow inductance commutation cell (including package and circuit layout) should be fulfilled [6]–[9].

In high frequency dc-dc buck-boost converters, for limitation of turn on switching losses, the zero voltage switching (ZVS) conditions are strongly recommended. The ZVS operation may be directly achieved in a resonant circuit consisting of the filter inductor and the switches capacitance. By applying control of the triangular current mode (TCM) [10] (defined

also, as critical current mode [11]), resonant transitions are evoked at successive converter state commutations. Relatively large triangular current waveform ripples characterizing TCM operation can be attenuated by introducing interleaved multi-phase topology [12], in a form of coupled inductors [11] or using circuit extension with additional clamp switch [13]. However, an impact of high frequency  $dv/dt$  switching on electromagnetic interference (EMI) emission has not been specifically considered in above works. The EMI effects including near field couplings, signal stability, layout, operation mode and passive components are presented in [14]. The impact of parasitic capacitance between PCB board and heat-sink is described in [15]. The modelling of CM impedance is performed to predict the conducted EMI in [16], [17]. In view of the growing demand for application of GaN HEMT technology, in this paper, EMI conducted emission of a dc-dc buck converter operation in the TCM ZVS was investigated and compared with the conventional hard switching discontinuous current mode (DCM) control technique. Experimental setup, as in Fig. 1, consisted of GaN HEMT based dc-dc buck converter with resistive load, supplied by the line stabilization network (LISN) from the dc voltage source. The paper objective is to specify the power conversion efficiency and attenuation of common mode (CM) and differential mode (DM) noise voltage of the compared switching control strategies. For the TCM operation, the sizing of an additional snubber capacitor is considered to reduce the switch turn off voltage overshoot and to stabilize resonant transition period. In section II, the switching strategies are briefly introduced. In section III, the test setup, implemented control strategies with energy based analysis of snubber capacitor are presented. Next, experimental results of EMI and converter efficiency measurements are compared, that are resumed in conclusions.

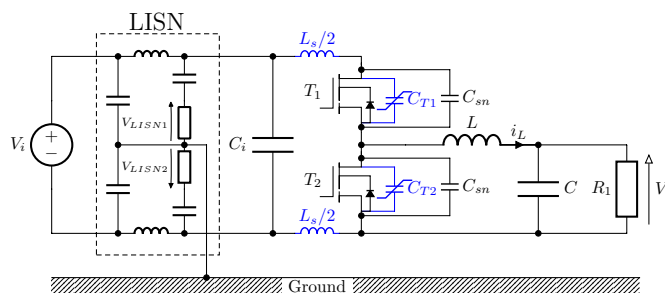


Fig. 1. Test circuit of GaN HEMT buck converter

## II. SWITCHING STRATEGIES

### A. DCM strategy

For the purpose of comparative study, the DCM waveforms are recalled in Fig. 2. with corresponding operation modes presented in Fig. 3. During the interval  $[t_0 : t_1]$  when the  $T_1$  is on, the inductor current  $i_L$  increases linearly. At instant  $t_1$ , the  $T_1$  turns off. Voltage  $v_{T1}$  is rising and capacitance  $C_{T1}$  changes from a large to low value according to the nonlinear capacitance characteristic. This involves providing a charge to  $C_{T1}$  and discharge of  $C_{T2}$ . After  $T_1$  is turned off  $[t_2 : t_3]$ , the inductor current  $i_L$  decreases linearly flowing through the load and the body diode of transistor  $T_2$ .

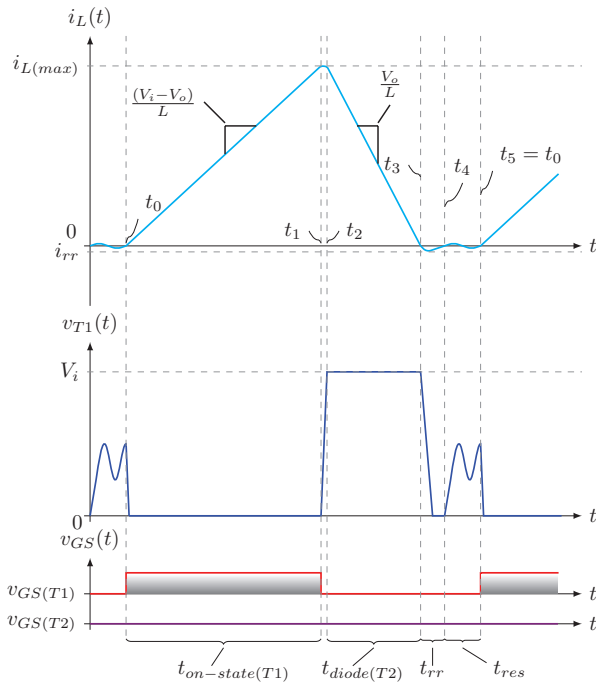


Fig. 2. DCM waveforms

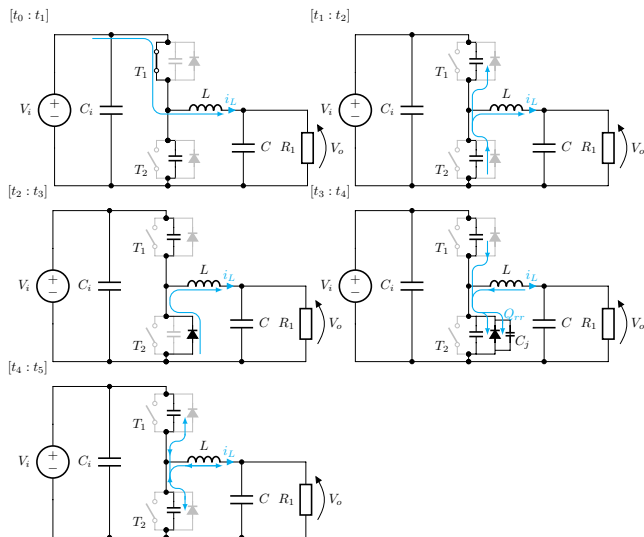


Fig. 3. DCM operation subcircuits

When  $i_L$  reaches zero, the reverse recovery charge  $Q_{rr}$  has to be provided to turn off the body diode – exciting oscillatory currents from capacitances:  $C$  and  $C_{T1}$ . In the interval  $[t_4 : t_5]$  the  $C_{T1}$  and  $C_{T2}$  are reloading in resonant circuit with the inductor  $L$  causing voltage oscillations across transistors until next period begins [18].

### B. TCM strategy

Similarly to the preceding case, the TCM waveforms are presented with operation modes respectively in Fig. 4. and Fig. 5.

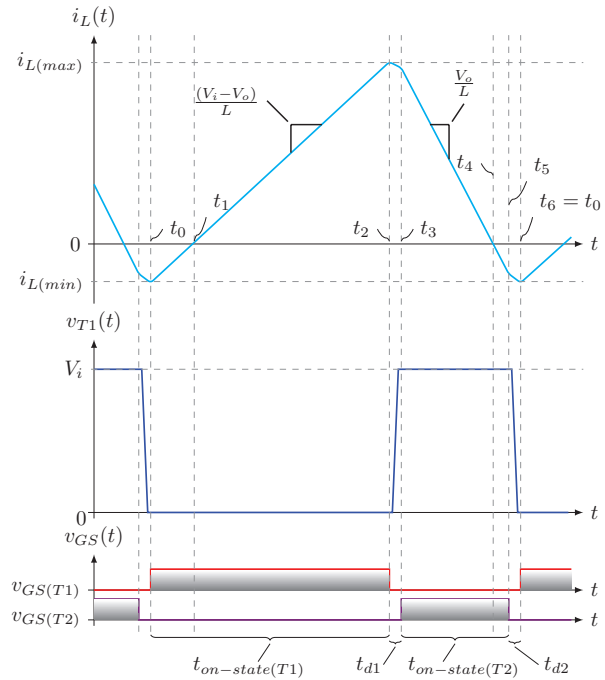


Fig. 4. TCM waveform

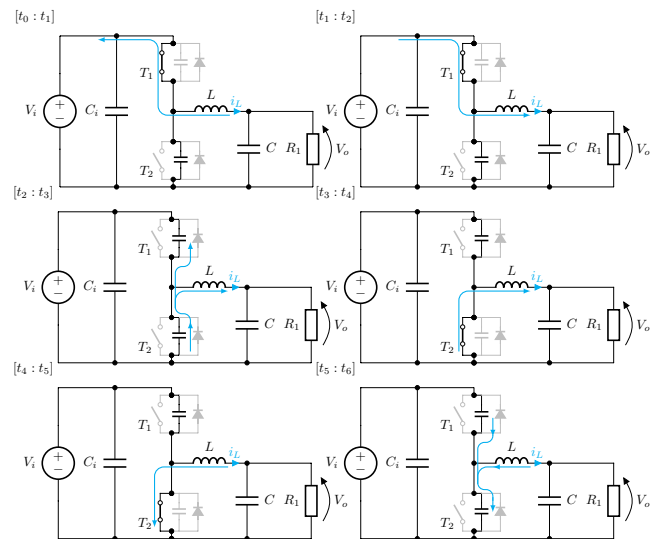


Fig. 5. TCM operation subcircuits

In the active subinterval  $[t_0 : t_2]$ , when the  $T_1$  is turned on, the inductor current  $i_L$  rises linearly in the range from  $i_{L(min)}$

to  $i_{L(max)}$ . At instant  $t_2$  the  $T_1$  turns off. Accumulated energy of the inductor  $L$  is sufficient to discharge the  $C_{T2}$  and charge the  $C_{T1}$  capacitances in a resonant transition to enable ZVS turn on of the  $T_2$ . Next, in the passive subinterval  $[t_3 : t_5]$  the inductor current  $i_L$  decreases linearly flowing through the load and the  $T_2$ . When  $i_L$  reaches predetermined negative threshold  $i_{L(th)} > i_{L(min)}$ , the  $T_2$  turns off reinitiating resonant transition to recharge  $C_{T2}$  and discharge  $C_{T1}$  capacitances. After half of the resonant period, the ZVS conditions occur to turn on the  $T_1$  and to restart the TCM operation.

### C. TCM with capacitive snubber

At transistor  $T_1$  turn off transients, an overvoltage can be induced due to rapidly decreasing current in stray inductances  $L_s$  of input power loop (Fig.1). In the following part, a snubber capacitor  $C_{sn}$  is applied to attenuate voltage spikes. Sizing of the snubber capacitor is based on energy balance equations. The energy  $E_{bf}$  before transistor  $T_1$  turn off can be approximated by:

$$E_{bf} \approx \frac{I_{T1(max)}^2 L_s}{2} + \frac{2V_{T2(off)}^2 C_{T2(off)}}{3} + \frac{V_{T2(off)}^2 C_{sn}}{2} \quad (1)$$

where:  $C_{T2(off)}$  - the voltage dependent drain-to-source capacitance  $C_{DS}(V_{DS})$  of transistor  $T_2$  in off state is obtained from the producer data-sheet capacitance characteristics  $C_{DS} = C_{OSS} - C_{RSS}$  for  $V_{DS} = V_i$ . The energy stored in the drain-to-source capacitance  $C_{DS}$  at  $V_{DS}$  results from the following formula [19]:

$$E_{oss} = \frac{2C_{DS}(V_{DS})V_{DS}^2}{3} \quad (2)$$

and

$$I_{T1(max)} = \frac{V_i - V_o}{L}(t_2 - t_1) \quad (3)$$

The energy  $E_{af}$  after transistor  $T_1$  turn off

$$E_{af} \approx \frac{2V_{T1(max)}^2 C_{T1(max)}}{3} + \frac{V_{T1(max)}^2 C_{sn}}{2} \quad (4)$$

where:

$V_{T1(max)}$  - the maximal value of overvoltage on  $T_1$  and  $C_{T1(max)}$  - the  $T_1$  drain-to-source capacitance for  $V_{T1(max)}$ . Assuming the energy before transistor turn off equals to the energy after turned off:

$$E_{bf} = E_{af} \quad (5)$$

the capacitance of snubber capacitor  $C_{sn}$  is derived for acceptable  $V_{T1(max)}$ :

$$C_{sn} = \frac{3I_{T1(max)}^2 L_s + 4(C_{T2(off)} V_i^2 - C_{T1(max)} V_{T1(max)}^2)}{3(V_{T1(max)}^2 - V_i^2)} \quad (6)$$

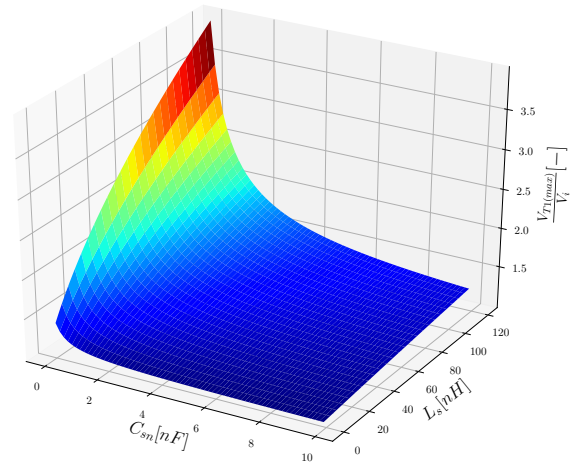


Fig. 6. Impact of snubber capacitor  $C_{sn}$  and input stray inductance  $L_s$  on voltage overshoot at the T1 turn off

## III. EXPERIMENTAL RESULTS

### A. Test setup

The dc-dc buck converter shown in Fig. 1 was built using half-bridge connected two GaN HEMT in cascode structure of Transphorm (TPH3207WS: 650V/50A) with low pass LC filter, sized to the cut-off frequency  $f_c = 1630\text{Hz}$ . The converter was supplied from dc input voltage source  $V_i$  by the LISN Schaffner NNB 41. The resistive load  $R_l$  was set to dissipate 350W at the output voltage  $V_o = 55\text{V}$ .

Switching of GaN transistors was accomplished by the gate driver with two gate circuit branches as presented in Fig. 7. In this configuration, turn on and off time can be set individually using various values of  $R_1$  and  $R_2$  resistors respectively. Thus, switching performance is limited by resistor values, which determines the value of  $dv/dt$  existing in the converter. In the considered setup, a gate

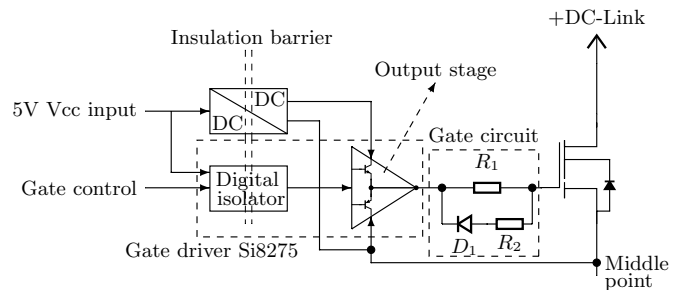


Fig. 7. Schematic of the gate driver

driver based on Si8275 IC was used to accomplish a signal insulation and the output stage of the driver. Moreover, two commercial DC-DC power supplies were used to provide independent powering of upper and lower switch. They create positive and negative voltages for driving each GaN device. Their stray capacitance is in the range of tens pF. Gate

circuits contained  $R_{on} = 36\Omega$ ,  $R_{off} = 10\Omega$  and provided voltages  $V_{GS} = +8V/-2V$  for turn on and turn off switching.

The gating control pulses were generated using the STM32F407VG microcontroller. To obtain tight timing of gate signals, control program with three master-slave counters was configured to avoid delays deriving from internal interruptions in the microcontroller. In this way, the 40ns resolution for gate signal and dead times was obtained at the switching frequency  $f_s=80$  kHz.

Using buck converter parameters from Table I in equation (6), an impact of snubber capacitor  $C_{sn}$  and input stray inductance  $L_s$  on  $V_{T1(max)}/V_i$  voltage overshoot is calculated as in Fig. 6. This case study revealed increasing sensitivity of commutation transients for the input stray inductance  $L_s$  above 40nH. Minimization of  $L_s$  by careful circuit layout design is of primary importance. Otherwise, to attenuate turn off voltage overshoot, a snubber capacitor has to be applied. In the tested buck converter to limit turn off voltage overshoot to approximately 40% the  $C_{sn}=3.2$ nF was applied.

TABLE I  
BUCK CONVERTER PARAMETERS IN TCM

Output power ( $P_o$ )	350W
Input voltage ( $V_i$ )	70V
Output voltage ( $V_o$ )	55V
Output current ( $I_o$ )	6.35A
Min. value of inductor current ( $I_{L(min)}$ )	-1.3A
Max. value of inductor current ( $I_{L(max)}$ )	15.2A
Input capacitor ( $C_i$ )	5.11 $\mu$ F
Input stray inductance ( $L_s$ )	114nH
Input stray resistance ( $R_s$ )	90m $\Omega$
Output capacitor ( $C$ )	1.1mF
Inductor ( $L$ )	8.7 $\mu$ H
Parasitic capacitance of $T_2$ in off state $C_{T2(off)}$	600pF

The switching strategies described above were compared in Fig. 8 by voltage waveforms across  $T_1$  transistor. During DCM and TCM operation, at  $T_1$  turn off significant overvoltage spikes had been recorded due to rapid decrease of current flowing through the stray inductances of input supply circuit. Only application of TCM with capacitive snubber attenuated overvoltage amplitudes, in accordance with analytical results of equation (6). In zero  $i_L$  current intervals of DCM operation, a typical resonant process between capacitances  $C_{T1}$ ,  $C_{T2}$  and inductor  $L$  was evoked. In TCM strategy both transistors operated alternately with predetermined dead times for soft switching transitions.

For TCM+ $C_{sn}$  Fig. 9 depicts, in larger time scale, current commutation from  $T_1$  to  $T_2$ . The  $T_1$  gate turn off initiated resonant charging of  $C_{T1}$  and discharging of  $C_{T2}$  with corresponding rate of change of transistor voltages:  $V_{T1}$  and  $V_{T2}$  that depended on load inductor current  $i_L$ . The LISN perturbation pulse was coherent with change of transistor voltages. After the recharging process had been completed the  $T_2$  was turned on in ZVS conditions to conduct  $i_L > 0$  as synchronous rectifier. To complete TCM sequences Fig. 10 presents load current

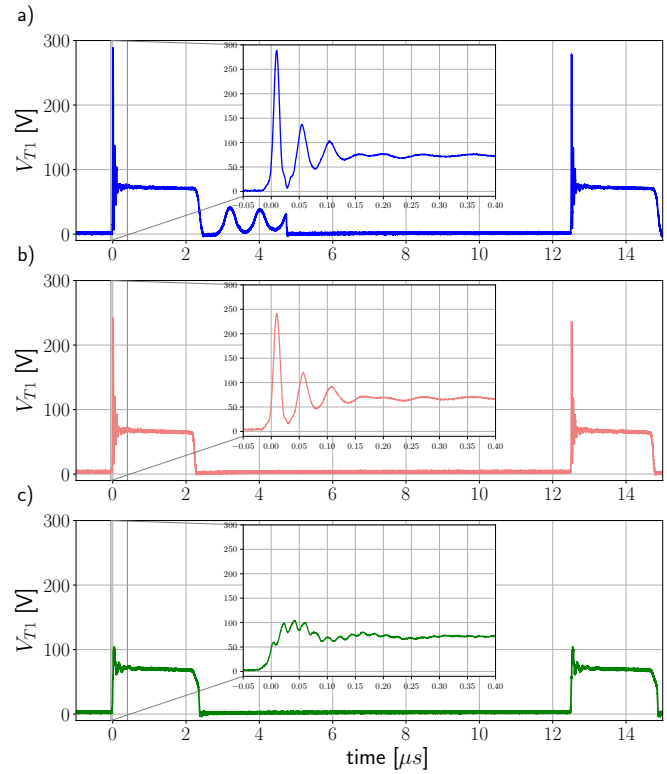


Fig. 8. Voltage waveforms across transistor  $T_1$ ; a) DCM hard switching, b) TCM ZVS, c) TCM ZVS with snubber capacitors  $C_{sn}$

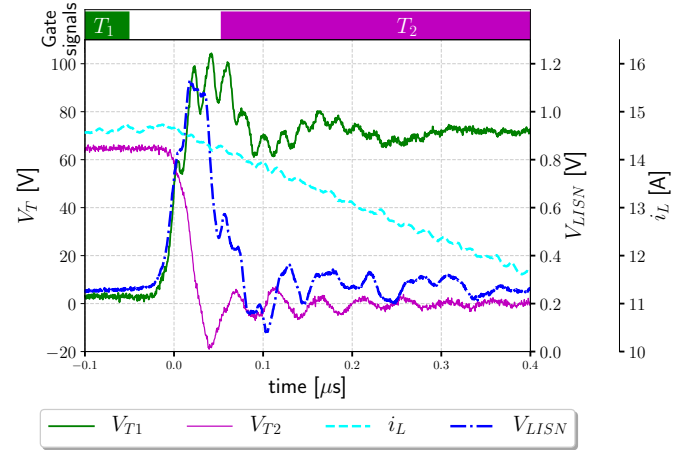


Fig. 9. ZVS of load current  $i_L$  from  $T_1$  to  $T_2$

commutation from  $T_2$  to  $T_1$ . At predetermined  $i_{L(th)} < 0$ , the  $T_2$  was turned off recharging nonlinear capacitances of both transistors. Due to near zero current transients, a lower rate of change of transistor voltages attenuated the LISN perturbation amplitude. At the end of recharging process,  $T_1$  was turned on at ZVS. Comparative timing specification of TCM with and without capacitive snubber is presented in Table II. It is confirmed that the snubber impacts on extension of resonant transition periods ( $t_{d1}, t_{d2}$ ) and  $dV_{T1}/dt$  turn off decrease.

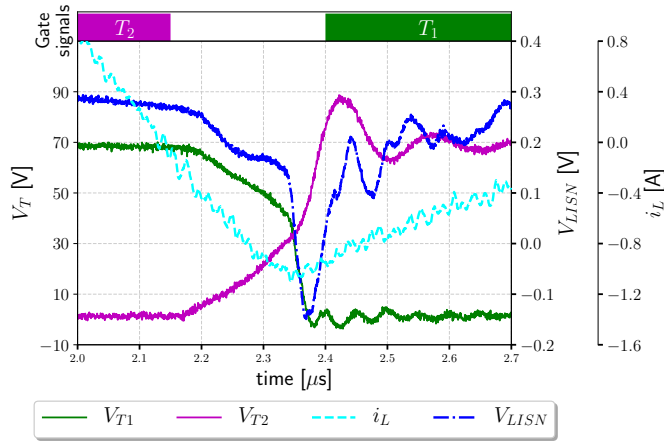


Fig. 10. ZVS of load current  $i_l$  from  $T_2$  to  $T_1$

TABLE II  
TCM OPERATION WITHOUT AND WITH  $C_{sn}$

	without $C_{sn}$	with $C_{sn}$ (3.2nF)
$T_1$ on time ( $t_{on-state}(T_1)$ )	10.2 $\mu$ s	10.125 $\mu$ s
Dead time 1 ( $T_1$ off and $T_2$ on) ( $t_{d1}$ )	40ns	125ns
$T_2$ on time ( $t_{on-state}(T_2)$ )	2.05 $\mu$ s	2.0 $\mu$ s
Dead time 2 ( $T_2$ off and $T_1$ on) ( $t_{d2}$ )	210ns	250ns
Max. $\frac{dV}{dt}$ of $V_{T1}$ during turn on	1.3 $\frac{V}{ns}$	1.3 $\frac{V}{ns}$
Max. $\frac{dV}{dt}$ of $V_{T1}$ during turn off	25.1 $\frac{V}{ns}$	5.6 $\frac{V}{ns}$
$V_{T1}$ falling time during turn on ( $t_f$ )	122ns	218ns
$V_{T1}$ rising time during turn off ( $t_r$ )	30ns	48.5ns

### B. Efficiency

Comparative experimental results of buck converter efficiency excluding the gate driving power are depicted in Fig. 11 for varying loads. An efficiency increase for ZVS TCM schemes over conventional DCM operation is evident. The highest (almost 1%) efficiency elevation was measured in the case of the TCM with capacitive snubber.

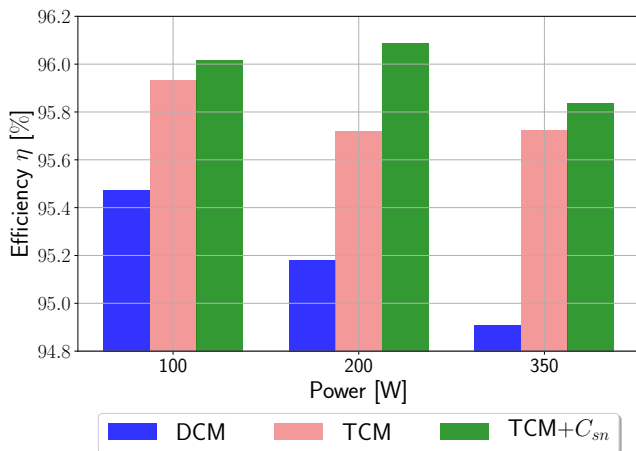


Fig. 11. Efficiency indexes

The results of analytical computation (as in [19]) of conductive and switching losses of the considered buck converter schemes are presented in Fig 12 for the rated output power.

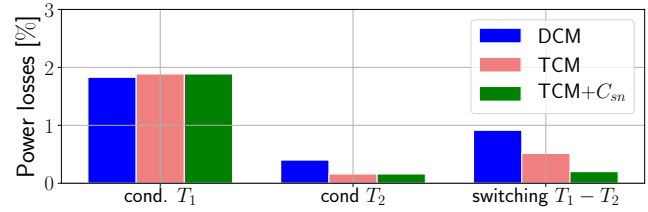


Fig. 12. Power loss distribution ( $P_o=350W$ )

The  $T_1$  conduction loss is approximately constant due to comparable transistor current waveforms in the DCM and TCM operation. The  $T_2$  conduction loss is decreased in the TCM because of synchronous rectification mode of operation. Main part of switching loss is caused by  $T_1$  turn off. This is the energy lost in the resistance  $R_s$  of the charging path of  $C_{T1}$  capacitance and during the resonant turn off oscillations. In the DCM operation during turn on, the energy stored in the transistor capacitance is lost in the transistor on-resistance. During TCM operation, switching power loss is reduced due to resonant transition of the energy accumulated in transistor capacitances at the ZVS between  $T_1$  and  $T_2$ .

### C. EMI attenuation

In Figures 13-14 the spectra of common and differential modes are respectively presented for three switching strategies. The signals have been registered using LISN and separated offline for common and differential modes [20] using (7) and (8)

$$|V_{CM}| = \left| \frac{V_{LISN2} + V_{LISN1}}{2} \right| \quad (7)$$

$$|V_{DM}| = \left| \frac{V_{LISN2} - V_{LISN1}}{2} \right| \quad (8)$$

Both CM and DM EMI spectra indicate significant peaks of the switching frequency  $f_s$  harmonics, that are related to the triangular inductor current waveforms of converter operation.

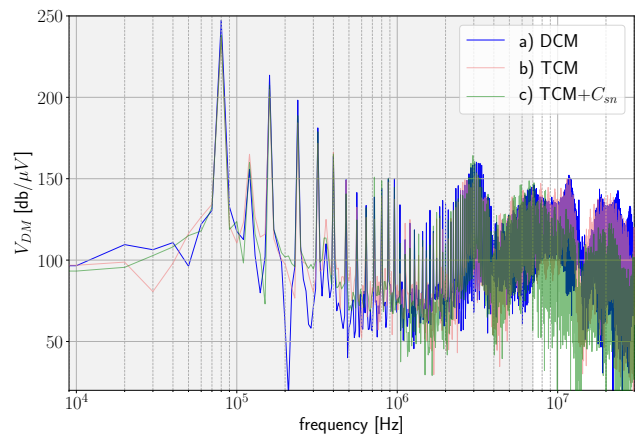


Fig. 13. EMI differential mode spectra

In order to analyze CM current loops during switching from  $T_1$  to  $T_2$ , based on the buck converter test scheme from Fig 1, an equivalent circuit is derived as in Fig 16. The CM interference is propagated to the LISN RC branches in the loop containing parasitic capacitances between the heat-sink and the drain node  $T_1$  :  $C_{t-h}$ , the drain node  $T_2$  :  $C_{m-h}$ , the source node  $T_2$  :  $C_{b-h}$  and the ground  $C_{h-gnd}$  which affect the CM level. Since CM perturbation propagate by parasitic capacitances  $C_{t-h}$ ,  $C_{m-h}$ ,  $C_{b-h}$  and  $C_{h-gnd}$ , the envelope spectra obtained for CM emission are higher than for the DM emission. In the range above 10MHz an impact of overvoltage peaks with ringing effects when  $T_1$  turns off is observed (as was depicted by large scale voltage transients in Fig 15). To be noticed, emission levels are comparable for the DCM operation and for the TCM without snubber operation. But in the case of the TCM+ $C_{sn}$ , attenuation of the CM interference in the range starting from 7MHz reached almost -40dB at 20MHz.

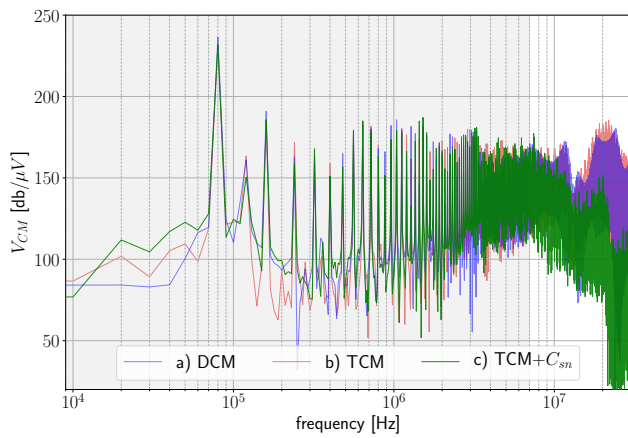


Fig. 14. EMI common mode spectra

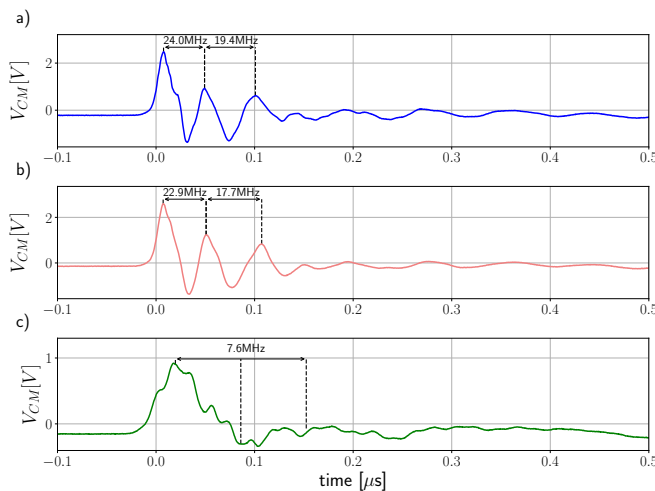


Fig. 15. CM voltage ripples during switching from  $T_1$  to  $T_2$  a) DCM b) TCM c) TCM+ $C_{sn}$

The main components of parallel resonant circuit where the ringing interference is generated are the input stray inductance  $L_s$ , the nonlinear drain-to-source capacitance  $C_{T1}(V_{DS})$  and

the conductive path resistance  $R_s$  that are shunted by input filter capacitor  $C_i$ . Hence, the ringing frequency:

$$f_r \approx \frac{1}{2 * \pi * \sqrt{L_s * C_{T1}(V_{DS})}} \quad (9)$$

Since the nonlinear capacitance depends on drain-to-source voltage, the  $f_r$  varies in the range from 27 MHz for  $C_{T1}(V_{T1(max)})$  to 17 MHz for  $C_{T1}(V_i)$  (Figure 15). The parasitic capacitances to the heat-sink are also part of resonant loop, but their values are relatively much smaller than changes of  $C_{T1}(V_{DS})$ . Augmentation of  $C_{T1}$  by the snubber capacitance  $C_{sn}$  leads to attenuation of the voltage overshoot with frequency decrease of the ringing interference:

$$f_r \approx \frac{1}{2 * \pi * \sqrt{L_s * (C_{T1}(V_{DS}) + C_{sn})}} \quad (10)$$

The frequency  $f_r$  calculated using eq. 10 for parameters from Table I equals 7.64MHz.

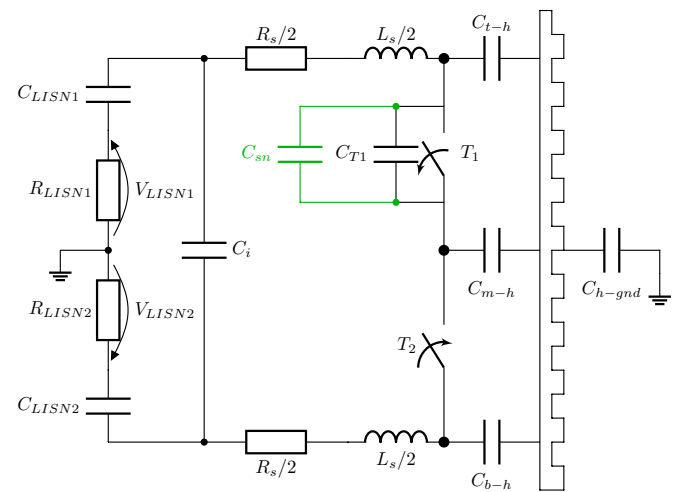


Fig. 16. Equivalent circuit of CM current loops during switching from  $T_1$  to  $T_2$

#### IV. CONCLUSION

In a GaN HEMTs based dc-dc buck converter the EMI conducted emissions were measured for discontinuous current mode and triangular current mode control strategies. Zero voltage switching that was achieved for the TCM operation revealed improvement of power conversion efficiency with the reference to the DCM operation. Implementation of capacitor snubbers across transistors for TCM operation slowed down transistor turn off process clamping voltage spikes. In consequence significant attenuation of common mode EMI emission with slight increase of power conversion efficiency were obtained. In order to fully exploit rapid switching ability of GaN HEMTs, recommendation of ZVS topology cannot be a sufficient condition but it must be accompanied by circuit design layout assuring extremely low parasitic inductances of commutation circuit loop.

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