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# Frequency-Based Regularization for Improved Reliability Optimization of Antenna Structures

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Abstract—The paper proposes a modified formulation of antenna parameter tuning problem. The main ingredient of the presented approach is a frequency-based regularization. It allows for smoothening the functional landscape of the assumed cost function, defined to encode the prescribed design specifications. The regularization is implemented as a special penalty term complementing the primary objective and enforcing the alignment of the antenna responses with the target operating frequency (or frequencies for multi-band antennas). The result is an improved reliability and reduced cost of the optimization process, both highly desirable from the point of view of the efficacy of EM-driven design procedures. Furthermore, regularization makes the use of local routines sufficient even in situations where global search is otherwise imperative (e.g., due to poor initial design). Our methodology is demonstrated using three microstrip antennas. The superior performance of the approach, both in terms of design reliability and in terms of the computational cost of the optimization process, is corroborated by comparisons with a conventional formulation.

Index Terms— Antenna optimization, gradient-based search, frequency-based regularization, EM analysis, EM-driven design.

## I. Introduction

Ever-increasing performance requirements, the emergence of new application areas (5G [1], internet of things [2], medical imaging [3]), the need for implementing various functionalities (circular polarization [4], MIMO operation [5], pattern diversity [6]), as well as the constraints on physical dimensions, are among those factors that make the design of modern antennas a challenging endeavor. To conform to the industry and consumer demands, contemporary antenna structures become more and more complex [7], described by multiple parameters [8], and—for reliability reasons—have to be evaluated using full-wave electromagnetic (EM) simulation tools [9], [10]. The latter may become a serious bottleneck whenever massive evaluations are required. A representative example of such an expensive procedure is numerical optimization [11], [12], which is otherwise imperative to boost the antenna performance beyond what is possible using parameter sweeping or theoretical models. Other tasks, e.g., uncertainty quantification [13], [14], or global optimization [15]-[17], entail even higher expenses.

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Expediting EM-driven optimization has been an important research topic, leading to numerous techniques that include adjoint sensitivities [18], [19], gradient-based procedures with sparse sensitivity updates [20], [21], surrogate-assisted algorithms employing both the approximation [22]-[24] and physics-based models [25]-[27] with a notable example of space mapping [28]. Data-driven metamodels and machine learning methods [29] are popular solutions for globalized search (e.g., efficient global optimization [30]). Yet another possibility is utilization of variable-fidelity EM simulations [31] along with the appropriate correction techniques (e.g., [32]). All of these methods have certain advantages but also drawbacks. In particular, surrogate-based procedures are very much limited by the problem dimensionality (data-driven models) [33], or are difficult to automate and require dedicated low-fidelity representations (physics-based models) [34].

Regardless of a particular optimization task, whether it is design closure [35], dimension scaling for a different operating frequency or substrate [36], or global search conducted to find a better parameter set of a topologically complex antenna, one of the most important issues is an appropriate allocation of the operating band(s) of the structure. From numerical optimization perspective, frequency-wise manipulation of the antenna characteristics is considerably more difficult than the level adjustment, especially for narrow- and multiband antennas. This difficulty renders the application of local routines (e.g., gradient-based [37]) unreliable and computationally inefficient in many real-world cases.

This paper proposes a simple frequency-based regularization technique that allows us to mitigate the aforementioned problems and to improve the efficiency of the optimization process in a significant manner. The regularization is implemented through a reformulation of the cost function pertinent to the design task at hand by adding a penalty term that enforces the alignment of antenna characteristics with the target operating frequency (or frequencies). This does not only smoothen the functional landscape to be handled by the optimization algorithm and may reduce the cost of the parameter adjustment process, but also makes the use of local routines sufficient in cases where handling the task according to the original formulation would call for global search. The operation and performance of our methodology is illustrated using three examples of planar antennas. Benchmarking against conventional optimization is provided as well to demonstrate the advantages of the presented approach.

The novelty and the technical contributions of the work include: (i) the development of a frequency-based regularization scheme that enables efficient alignment of the antenna operating frequency (or frequencies) with their target values, (ii) reformulation of the objective function and the design optimization task that incorporates regularization and improves of the efficacy of the antenna parameter tuning process over conventional formulation (to the extent of addressing the issue of objective function multi-modality), (iii) the development of the versatile optimization framework demonstrated for various design scenarios (matching improvement, gain maximization, footprint reduction). To the best knowledge of the authors, none of these have been shown so far in the literature.

#### II. OPTIMIZATION BY FREQUENCY-BASED REGULARIZATION

This section outlines the proposed frequency-based regularization technique and places it in the context of antenna design closure using local optimization, here, trust-region gradient search. The latter is used to illustrate the regularization scheme, and can be replaced by other algorithms of choice in practical setups.

## A. Optimization Problem Formulation

The following notation will be used throughout the paper. We denote by R(x) the response of the EM-simulated antenna model, where x is a vector of independent adjustable parameters (typically, antenna dimensions). To quantify the antenna performance, we use a scalar merit function U(R(x)), which is defined so that a better design corresponds to a lower value of U. The design problem is a nonlinear minimization task of the form

$$\mathbf{x}^* = \arg\min_{\mathbf{x}} U(\mathbf{R}(\mathbf{x})) \tag{1}$$

where  $x^*$  is the optimum design to be found. The analytical form of the merit function depends on the problem and the assumed treatment of the design constraints [25].

An example follows. Consider a multi-band antenna to be matched at the target operating frequencies  $f_{0.K}$ , k = 1, ..., N. The minimax merit function is then defined as

$$U(\mathbf{R}(\mathbf{x})) = \max\{|S_{11}(\mathbf{x}, f_{0.1})|, ..., |S_{11}(\mathbf{x}, f_{0.N})|\}$$
 (2)

where  $S_{11}(x,f_{0.k})$  is antenna reflection at the design x and frequency f. As another example, consider an antenna that is to operate within the frequency range defined by its center frequency  $f_0$  and the fractional bandwidth B, so that  $|S_{11}| \le -10$  dB and the realized gain is to be maximized within at  $f_0$ . A possible formulation of the objective function (with implicit constraint handling) is

$$U(\mathbf{R}(\mathbf{x})) = -G(\mathbf{x}, f_0) + \beta c(\mathbf{x})^2$$
(3)

Here, G(x,f) is the realized gain at the frequency f, whereas  $\beta c(x)$  is a penalty term (with  $\beta$  being a penalty coefficient) introduced to enforce  $|S_{11}| \le -10$  dB over the bandwidth B. The penalty function may be defined to quantify a relative violation of the matching condition, e.g.,  $c(x) = \max\{\max\{f_0(1 - B/2) \le f \le f_0(1 + B/2) : |S_{11}(x,f)| + 10\}, 0\}$ .

## B. Frequency-Based Regularization

As mentioned in the introduction, moving the antenna resonances to the intended frequencies is one of the challenging aspects of numerical optimization. This is illustrated in Fig. 1, showing the reflection and realized gain characteristics of a quasi-Yagi antenna considered in Section II. Re-designing the antenna for the target operating frequency of 5 GHz, and starting from the exemplary initial design shown in the picture, requires global search. This is because the initial design and the optimum are separated by a local maximum. Although the picture is a simplified representation of the problem (the initial and the optimum design are connected through a line segment), it gives a flavor of the practical challenges one may face when trying to apply numerical optimization.

To address this issue, we define a regularization function  $f_r(x)$ , which accounts for the discrepancies between the actual operating frequency (or frequencies) of the antenna and the target ones. The frequency-regularized objective function is then defined as

$$U_r(\mathbf{R}(\mathbf{x})) = U(\mathbf{R}(\mathbf{x})) + \beta_r \left[ \max \left\{ \frac{f_r(\mathbf{x}) - f_{r,\text{max}}}{f_{r,\text{max}}}, 0 \right\} \right]^2$$
(4)

where  $f_{r,\text{max}}$  is the maximum acceptable discrepancy between the

actual and target operating frequency (or frequencies). The regularized objective function is defined to increase the original objective by the amount proportional (with the user-defined proportionality factor  $\beta_r$ ) to the discrepancy quantified by  $f_r$ . However, the said contribution is zero if the discrepancy is sufficiently small (i.e., smaller than  $f_{r,\max}$ , also user-defined). This is to ensure that the original objective function is not distorted when the design approaches the optimum, and that the location of the optimum is the same w.r.t. to both U and  $U_r$ , assuming of course that the design for which  $f_r(\mathbf{x}) \leq f_{r,\max}$  is attainable. Furthermore, the regularization factor is smooth (continuously differentiable) with respect to  $f_r$ , which makes it appropriate to work with gradient-based optimization routines.

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The effect of regularization is shown in Fig. 1(b): the functional landscape of the objective function is dramatically changed, and the reformulated problem becomes unimodal with the initial design being in the region of attraction of the optimum. Further, the optimum design according to the original objective function coincides with that of the regularized objective.

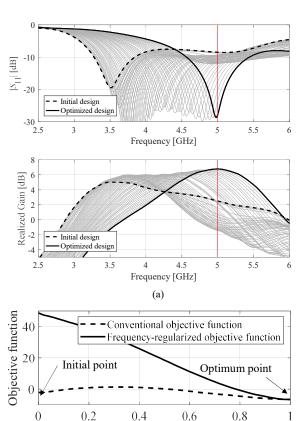


Fig. 1. Conceptual illustration of frequency-based regularization: (a) exemplary initial design for a quasi-Yagi antenna of Section III (thick dashed line), design optimized for the target frequency 5.0 GHz (thick solid line), and the family of antenna characteristics (reflection – top, realized gain – bottom) along the line segment connecting these two designs parameterized by  $0 \le t \le 1$  (grey lines); (b) conventional objective function (3) (- - -) and frequency-regularized objective function (4) with the regularization function (5) (—) versus parameter t. It can be observed that the regularized objective function is monotonic, and the optimum design is attainable from the given initial point using local search routine, which is not the case for the conventional formulation.

(b)

A specific definition of a regularization function depends on a considered antenna structure and the type of response. For the quasi-Yagi antenna considered in Fig. 1, and optimized using the objective function (3), the regularization function can be defined as

$$f_r(\mathbf{x}) = \left| f_0 - \frac{f_{L,1} + f_{L,0} + f_{L,2}}{3} \right| \tag{5}$$

where  $f_{L,j}$ , j=1, 2, are the frequencies corresponding to -10 dB levels of  $|S_{11}|$ , and  $f_{L,0}$  is the frequency of the antenna resonance. If, at a particular design x, the resonance level is above -10 dB, we assign  $f_{L,j} = f_{L,0}$ . In other words, the function  $f_r$  measures the distance between the target operating frequency and the approximate allocation of the antenna bandwidth (the average of the three frequencies mentioned above).

For the multi-band antenna optimized according to the minimax objective function (2), the regularization function can be defined as

$$f_r(\mathbf{x}) = \left\| \left[ f_{0.1} \dots f_{0.N} \right]^T - \left[ f_1(\mathbf{x}) \dots f_N(\mathbf{x}) \right]^T \right\|$$
 (6)

where  $f_k$ , k = 1, ..., N, are the actual resonant frequencies at the design x, extracted from the EM simulation results.

## C. Optimization Algorithm

The problem (1) can be solved using any available routine. Here, we use a trust-region gradient search [37]. The optimum  $x^*$  is approached through a series  $x^{(i)}$ , i = 0, 1, ..., produced as

$$\mathbf{x}^{(i+1)} = \arg\min_{\mathbf{x}: -\mathbf{d}^{(i)} \le \mathbf{x} - \mathbf{x}^{(i)} \le \mathbf{d}^{(i)}} U(\mathbf{L}^{(i)}(\mathbf{x}))$$
(7)

in which  $L^{(i)}(x) = R(x^{(i)}) + J_R^{(i)}(x - x^{(i)})$ . The Jacobian  $J_R$  is estimated using finite differentiation. The size vector  $d^{(i)}$  of the trust region is adjusted after each iteration using the standard rules [37]. Accelerated versions of (7), e.g., using sparse sensitivity updates are available [20], [21]; however, in this work, we focus on demonstrating the benefits of frequency-based regularization with little emphasis on reducing the cost of the optimization process by the algorithmic means.

## III. VERIFICATION CASE STUDIES

This section demonstrates the operation of the frequency-based regularization using three examples of planar antennas, each exhibiting different characteristics. We compare the efficacy of the optimization process involving the conventional formulation of the objective function and the regularized one in terms of the ability to find the satisfactory design but also the computational cost of the algorithm.

## A. Quasi-Yagi Planar Antenna

The first example is a quasi-Yagi antenna with a parabolic reflector shown in Fig. 2 [38], implemented on FR4 substrate ( $\varepsilon_r = 4.4$ , h = 1.5 mm). The design variables are  $\mathbf{x} = [W \ L \ L_m \ L_p \ S_d \ S_r \ W_2 \ W_d \ g]^T$  (all dimensions in mm). The computational model is implemented in CST Microwave Studio.

The design task is to optimize the antenna for a given center frequency  $f_0$  while ensuring at least 8-percent impedance bandwidth (symmetric w.r.t.  $f_0$ ). Furthermore, the realized gain is to be maximized at  $f_0$ . The conventional formulation of the optimization problem uses the objective function (3). The frequency-based regularization employs the regularization function (5) with  $f_{r.max} = 0.15$  GHz. The antenna was optimized for  $f_0 = 2.5$  GHz,  $f_0 = 4.5$  GHz, and  $f_0 = 5.0$  GHz, in all cases starting from the initial design that corresponds to the antenna operating at the frequency around 3.5 GHz. Figure 3 shows the initial and the optimized designs obtained using the standard and regularized formulations. It can be observed that the algorithm using the standard

formulation was unable to find high-quality designs in neither of the considered cases, whereas applying regularization ensures reaching satisfactory design for all scenarios. The performance comparison has been provided in Table I. Thus, regularization allows for consistently yielding satisfactory design but also, the average optimization cost is lower than for the standard formulation (assuming the same termination criteria, which was  $10^{-2}$  for the convergence in argument and  $10^{-2}$  for for the trust region size).

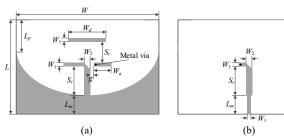


Fig. 2. Quasi-Yagi antenna with a parabolic reflector [38]: (a) top layer, (b) bottom layer.

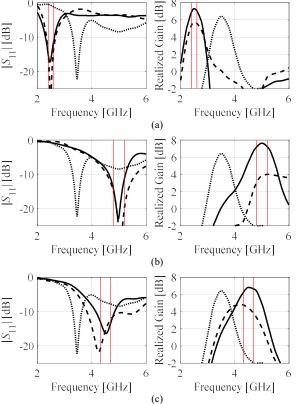


Fig. 3. Quasi-Yagi antenna optimization using standard formulation (cf. (3)), and frequency-based regularization (cf. (4), (5)). Shown are: initial design (····), optimum found using standard formulation (- - -), optimum found with regularization (—). Target frequencies: (a) 2.5 GHz, (b) 4.5 GHz, (c) 5.0 GHz. Vertical lines mark the intended operating bandwidth of the antenna.



Fig. 4. Geometry of the triple-band dipole antenna.

## B. Triple-Band Dipole Antenna

The second example is a triple-band uniplanar dipole antenna shown in Fig. 4 [39], implemented on RO4350 substrate. The adjustable parameters are  $\mathbf{x} = \begin{bmatrix} l_1 & l_2 & l_3 & l_4 & l_5 & w_1 & w_2 & w_3 & w_4 & w_5 \end{bmatrix}^T$ ; other parameters are fixed:  $l_0 = 30$ ,  $w_0 = 3$ ,  $s_0 = 0.15$  and o = 5 (all dimensions in mm). As before, the computational model is implemented in CST. The task is to improve antenna matching at the operating frequencies  $f_{0.1} = 2.45$  GHz,  $f_{0.2} = 3.6$  GHz, and  $f_{0.3} = 5.3$ GHz. The standard (minimax) formulation employs the objective function (2). The frequency-based regularization uses the regularization function (6) with  $f_{r,\text{max}} = 0.15 \text{ GHz}$ .

The antenna was optimized using three different starting points. The reflection responses at the designs found using both approaches are shown in Fig. 5. The optimization procedure using the minimax formulation was only able to find a (more or less) satisfactory design for one of the initial designs, whereas the formulation incorporating regularization was successful in all cases. The performance differences between formulations are consistent with the previous example (cf. Table II): the design quality is significantly better, whereas the computational cost is lower when using regularization.

## C. Compact Ultra-wideband Monopole Antenna

The last example is the ultra-wideband monopole [40], implemented on RF-35 substrate ( $\varepsilon_r = 3.5$ , h = 0.762 mm), shown in Fig. 6. The adjustable parameters are  $x = [L_0 dR R r_{rel} dL dw L_g L_1 R_1]$  $dr c_{rel}$ <sup>T</sup>. The EM model is implemented in CST, and incorporates the SMA connector. The operating frequency range of the antenna is 3.1 GHz to 10.6 GHz. The design objective is to minimize the antenna footprint A(x) while ensuring that  $|S_{11}(x,f)| \le -10$  dB within the operating band.

The objective function is defined as

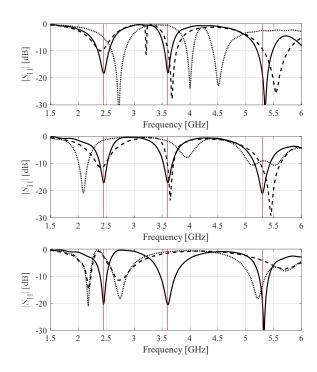
$$U(\mathbf{R}(\mathbf{x})) = A(\mathbf{x}) + \beta c(\mathbf{x})^{2}$$
(8)

where the penalty function takes the form  $c(x) = \max{\max{3.1 \text{ GHz}}}$  $\leq f \leq 10.6 \text{ GHz}: |S_{11}(x,f)| + 10\},0\}$ . The regularization function is defined as

$$f_r(\mathbf{x}) = \left| f_L - f_{r,1} \right| \tag{9}$$

where  $f_L = 3.1$  GHz and  $f_{r,1}$  is the lowest frequency corresponding to −10 dB level of reflection (or the frequency of the first antenna resonance if the resonance level is above -10 dB). The reason for this setup is that the minimum-size design is normally such that the matching condition is barely met (or slightly violated when using implicit constraint handling as in (8) [41]), with the first antenna resonance close to the lower edge of the operating band (here, 3.1 GHz). By enforcing this resonance to be close to that frequency, the problem of reducing the antenna size becomes numerically more tractable.

For the sake of demonstration, we optimize the antenna using three different starting points, as illustrated in Fig. 7. Regularization (4), (9) leads to considerably better results than the standard formulation (8), cf. Table III. In all cases, the condition  $|S_{11}(x,f)| \le -$ 10 dB is satisfied in a satisfactory manner, but the obtained footprint area is smaller for the algorithm using regularization. It should be emphasized that optimization-based size reduction is a challenging problem from the numerical perspective because the reflection constraint is active at the optimum. Locating it requires traversing the boundary of the feasible region, and the results are typically dependent on the starting point, partially due to numerical noise



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Fig. 5. Triple-band antenna optimization using standard formulation (cf. (2)), and frequency-based regularization (cf. (4), (6)). Shown are: initial design (...), optimum found using standard formulation (- - -), optimum found with regularization (--) for three different initial designs. Target frequencies are 2.45 GHz, 3.6 GHz, and 5.3 GHz.

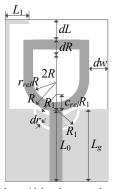


Fig. 6. Geometry of the ultra-wideband monopole antenna [40]. The ground plane marked using the light gray shade.

TABLE I QUASI-YAGI ANTENNA: OPTIMIZATION PERFORMANCE

Problem formulation	Target frequency	Results			
		Individual Case		Average	
		Cost#	$U(\mathbf{R}(\mathbf{x}))^{\$}$	Cost#	$U(\mathbf{R}(\mathbf{x}))^{\S}$
Standard (cf. (3))	2.5 GHz	165	-5.7 dB		
	4.5 GHz	123	$-3.7~\mathrm{dB}$	171	-4.6 dB
	5.0 GHz	224	-4.4 dB		
Regularization (this work, cf. (4), (5))	2.5 GHz	147	-7.2 dB		
	4.5 GHz	135	−7.5 dB	131	−7.1 dB
	5.0 GHz	110	−6.7 dB		

<sup>\*</sup>Cost expressed in the number of EM simulations of the antenna.

SObjective function value according to the function (3).

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TABLE III UWB ANTENNA: OPTIMIZATION PERFORMANCE

-20.5 dB

135

Problem formulation	Initial Design	Results			
		Individual Case		Average	
		Cost#	Area <sup>\$</sup>	Cost#	Area <sup>§</sup>
Standard (cf. (8))	1	93	261 mm <sup>2</sup>		
	2	101	$401 \text{ mm}^2$	113	$293\;mm^2$
	3	146	$216\;mm^2$		
Regularization (this work, cf. (4), (9))	1	125	238 mm <sup>2</sup>		
	2	151	$201 \text{ mm}^2$	138	$219 \text{ mm}^2$
	3	138	$219 \text{ mm}^2$		

<sup>\*\*</sup>Cost expressed in the number of EM simulations of the antenna.

<sup>\$</sup> Footprint area of the optimized antenna

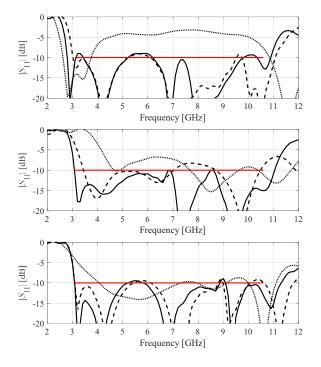


Fig. 7. Ultra-wideband monopole antenna optimization using standard formulation (cf. (8)), and frequency-based regularization (cf. (4), (9)). Shown are: initial design (....), optimum found using standard formulation (- - -), optimum found with regularization (---) for three different initial designs. Target operating band 3.1 GHz to 10.6 GHz is marked using the horizontal line.

Notwithstanding, regularization noticeably improves repeatability of the results compared to the standard formulation because it allows for quick adjustment of the lower edge of the operating bandwidth, which yields a better position before further tuning. At the same time, the optimization cost with regularization is slightly higher as the algorithm using the standard formulation often converges prematurely.

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### IV. CONCLUSION

This communication proposed a frequency-based regularization approach for reliable parameter tuning of antennas. It is incorporated into the objective function through a penalty term that quantifies the discrepancy between the target and the actual operating conditions of the antenna in terms of the relevant frequencies (e.g., allocation of the antenna resonances). The regularization function is formulated to be smooth (i.e., continuously differentiable) and only contributes to the primary objective if the aforementioned discrepancies are beyond the acceptance limit decided by the user. It has an effect of smoothing out the functional landscape to be optimized, and mitigates the multi-modality issues, but it does not modify the original objective when close to the optimum.

Our methodology has been validated using three planar structures, optimized under different scenarios (matching improvement, gain maximization, size reduction). A significant improvement of the search process efficacy has been demonstrated over the conventional design closure task formulations. This includes reducing the sensitivity of the optimization outcome to the initial design, a possibility of re-designing antenna structures for the operating frequencies significantly different from those at the starting point, as well as improving repeatability of solutions. An additional benefit resulting from regularization-based problem reformulation is that local methods may be sufficient in the cases that otherwise require global search. In other words, regularization may alleviate the difficulties pertinent to a possible presence of multiple local minima of the standard objective functions. Overall, the presented approach can be a useful algorithmic tool for handling problems where the standard setup (e.g., a minimax objective function) is prone to a failure. It may also alleviate the difficulties originating from poor initial designs.

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<sup>#</sup>Cost expressed in the number of EM simulations of the antenna.

<sup>\$</sup> Objective function value according to the function (2).

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