

# Superconductivity in Bismuth Pyrochlore Lattice Compounds RbBi<sub>2</sub> and CsBi<sub>2</sub>: The Role of Relativistic Effects

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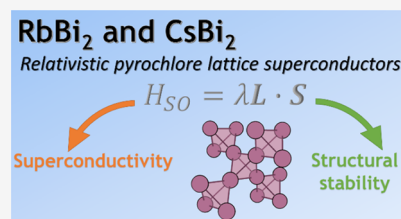


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**ABSTRACT:** Superconducting properties of two bismuthide intermetallic compounds, RbBi<sub>2</sub> and CsBi<sub>2</sub>, were studied by means of experimental measurements and *ab initio* calculations. We show that in both compounds, the superconductivity emerges from the pyrochlore Bi lattice and its formation is heavily influenced by relativistic effects. Based on our analysis of the effect of spin–orbit coupling on the electron–phonon coupling, we suggest a possible criterion for finding new superconducting materials by looking for structures featuring relativistically stabilized hypervalent networks of heavy *p*-block elements.

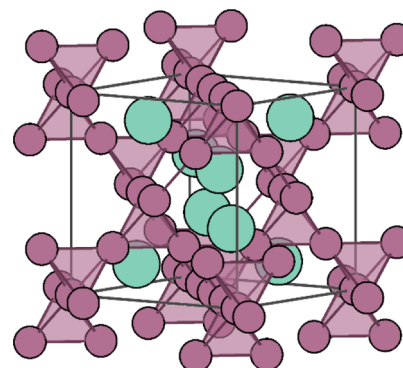


## INTRODUCTION

Bismuth ( $Z = 83$ ) is the heaviest stable element of the periodic table (the half-life of the longest living isotope,  $^{209}\text{Bi}$   $\tau_{1/2} = 2.0 \times 10^{19}$  yr<sup>1</sup> is 9 orders of magnitude longer than the age of the universe,  $t = 1.4 \times 10^{10}$  yr). This property makes it and its compounds interesting for studying effects of strong spin–orbit coupling (SOC) on physical properties of materials. Relativistic effects often result in Bi compounds behaving differently than isoelectronic species. For example, the most common cationic oxidation state of Bi is +3, with +5 compounds being generally unstable toward reduction.<sup>2–4</sup> Bi<sup>3+</sup> cation is very often lone-pair active, leading to complicated coordination environments.<sup>1</sup> Less known are the effects of relativistic phenomena on structural chemistry of Bi intermetallic compounds. Bi is known to form several stable hypervalent polyanions, such as the Bi<sup>−</sup> square network found in LiBi and NaBi but not observed in the isoelectronic NaSb.<sup>5–8</sup> Similarly, CaBi<sub>2</sub> and the recently reported SrBi<sub>2</sub> both host a hypervalent Bi<sup>−</sup> square lattice,<sup>9,10</sup> which is missing in the isoelectronic CaSb<sub>2</sub>.<sup>11</sup>

A number of binary bismuth superconductors are known, including the following: Ca<sub>11</sub>Bi<sub>10–x</sub>,<sup>12</sup> CaBi<sub>2</sub>,<sup>13,14</sup> SrBi<sub>3</sub>,<sup>15,16</sup> BaBi<sub>3</sub>,<sup>17</sup> Ba<sub>2</sub>Bi<sub>3</sub>,<sup>18</sup> LiBi,<sup>8,19</sup> NaBi,<sup>7</sup> KBi<sub>2</sub>, RbBi<sub>2</sub>, and CsBi<sub>2</sub>.<sup>20</sup> The latter three compounds are cubic Laves phases, crystallizing in a relatively simple MgCu<sub>2</sub>-type structure in which Bi atoms form a pyrochlore (vertex sharing tetrahedral) network (Figure 1). Interestingly, while the MgCu<sub>2</sub> is the 5th most common binary intermetallic structure type,<sup>21</sup> only a few of the known compounds feature a *p*-block element occupying the pyrochlore network—besides the three dibismuthides, these are MgIn<sub>2</sub>,<sup>22</sup> SnS<sub>2</sub>,<sup>23</sup> and RAl<sub>2</sub> (R = Sr, Ba, rare-earth metals, Th, and U).

Here, we present the results of our experimental and computational studies on RbBi<sub>2</sub> and CsBi<sub>2</sub>, concentrated on the effects of strong SOC on superconducting properties. We describe the magnetic behavior of single-crystalline samples of



**Figure 1.** Crystal structure of the cubic Laves phases ABi<sub>2</sub> (A = K, Rb, Cs). Bi atoms (drawn in purple) form a vertex-sharing tetrahedral (pyrochlore) lattice with voids filled with alkali atoms (green).

the two compounds, showing that type-I superconductivity is observed in both compounds. Heat capacity measurements show moderate to strong electron–phonon coupling. Based on the results of electronic and phonon structure calculations, we show that in both compounds, superconductivity emerges from the Bi<sub>4</sub><sup>2−</sup> pyrochlore lattice and that the relativistic effects play a complex role in stability and properties of the two phases. We found that strong SOC is crucial for the stability of charged Bi pyrochlore network and discuss the implications of this fact for the search for new heavy element-bearing superconducting materials.

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## MATERIALS AND METHODS

Single crystals of  $\text{RbBi}_2$  and  $\text{CsBi}_2$  were grown using a Bi self-flux method. Pieces of bismuth (Alfa Aesar, 99.99%) and rubidium (Alfa Aesar, 99.9%) were put in an alumina crucible inside an Ar-filled glovebox. Cesium was first heated above its melting point by warming it in hand and then poured dropwise into the crucible and covered with Bi pieces. Crucibles were then put in fused silica tubes along with plugs of quartz wool, and the tubes were subsequently evacuated, back-filled with Ar, and sealed without exposing alkaline metals to air. They were then heated to 550 °C, kept at that temperature for 8 h, and then slowly cooled (5 °C per h) to 310 °C at which temperature the excess Bi was spun off with the aid of a centrifuge. Clusters of tetrahedrally shaped crystals were obtained, with sizes ranging up to ca. 1 mm.

Warning! Rubidium and cesium metals will ignite spontaneously when exposed to air. Special care needs to be taken to avoid fire.  $\text{ABi}_2$  single crystals will decompose in air within minutes and the reaction might be exothermic.

The phase identity of the crystals was examined using powder X-ray diffraction (PXRD) measurements employing a Bruker D8 FOCUS diffractometer with a Cu  $K\alpha$  radiation source and a LynxEye detector. A few single crystals were crushed for the PXRD measurements inside an Ar-filled glovebox and mixed with an Apiezon-N grease or petroleum jelly. Since the powdered samples quickly oxidize, reacting with oxygen and moisture from air, the scanning time had to be reduced to 8 min. PXRD patterns were then analyzed by means of the LeBail method<sup>24</sup> using the FullProf software package.<sup>25</sup> PXRD patterns taken after a prolonged exposition to air show that both compounds decomposed completely yielding weakly crystalline elemental Bi and an amorphous product (most probably a hydrated alkali metal hydroxide), similarly to what was observed in  $\text{CaBi}_2$ .<sup>13</sup>

Heat capacity measurements were performed using the Quantum Design PPMS system by the standard relaxation technique. Magnetic susceptibility measurements were carried out using the ACMS option of the PPMS. Multiple randomly oriented single crystals were put in the standard straw sample holders. Sample preparation was carried out inside a glovebox to prevent oxidation.

*Ab initio* calculations were performed using the Quantum Espresso (QE) package<sup>26</sup> employing ultrasoft Perdew–Burke–Ernzerhof (PBE) GGA<sup>27</sup> pseudopotentials<sup>28</sup> with valence configuration  $4s^25s^14p^6$  for rubidium,  $5s^26s^15p^6$  for cesium and  $6s^26p^35d^{10}$  for bismuth, whereas wave function and charge density energy cutoffs were set to values 50 Ry and 500 Ry, respectively. For the consideration of the influence of the relativistic effects, two types of calculations were performed: scalar-relativistic (neglecting SOC) and fully relativistic (with SOC effect included for Bi). As expected and tested, inclusion of SOC for Rb and Cs does not change the results of calculations; thus, the SOC was included only for Bi in final calculations. In the first step, the lattice constant was optimized using the Broyden–Fletcher–Shanno–Goldfarb (BFGS) method. The electronic structure was calculated at the grid of  $(24)^3$   $k$ -points. Phonon structure and properties of electron–phonon coupling (EPC) were calculated at a grid of  $(6)^3$   $q$ -points.

Chemical bonding was investigated by means of Crystal Orbital Hamilton Population analysis<sup>29,30</sup> using the Stuttgart TB-LMTO-ASA code.<sup>31,32</sup> Calculations were performed using

the experimental cell parameter and  $(32)^3$   $k$ -point mesh and employed the Perdew–Wang GGA<sup>33</sup> exchange–correlation ( $xc$ ) potential.

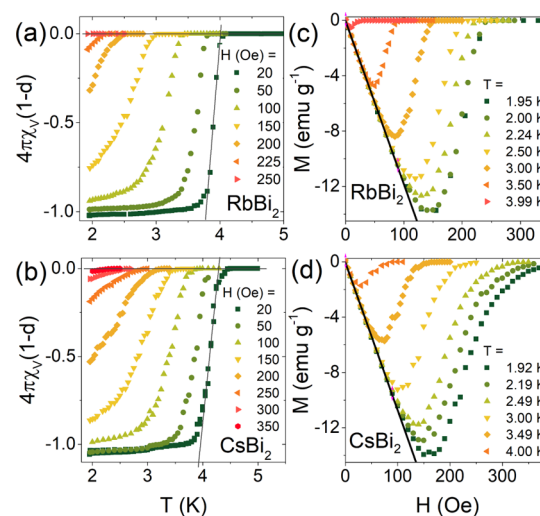
Electronic structure of an isolated tetrahedral  $\text{Bi}_4$  cluster was calculated using the ReSpect 5.1.0 relativistic DFT code.<sup>34</sup> Scalar-relativistic calculations were performed by means of 1-component Kohn–Sham method with one-electron relativistic corrections due to Douglas–Kroll–Hess of the second order (1c KS-DKH2). Fully relativistic electronic structure was calculated using the four-component Dirac–Kohn–Sham Hamiltonian (4c DKS). The Dyll core–valence double-zeta basis set<sup>35</sup> and the PBE  $xc$  potential were used in both cases. Molecular orbitals obtained from the 1c KS-DKH2 calculations were visualized using the IboView program.<sup>36,37</sup>

## RESULTS AND DISCUSSION

Room-temperature PXRD patterns of crushed crystals are presented in Figure S1 of the Supporting Information. All the Bragg lines in the PXRD pattern can be indexed to cubic (space group  $Fd\bar{3}m$ , #227) unit cell of  $\text{ABi}_2$  and elemental Bi (both from leftover flux droplets and decomposition of material). Lattice parameters resulting from LeBail fits are in agreement with previous reports.<sup>38,39</sup> Details of crystal structures are gathered in Table S1 of the Supporting Information.

The Rb–Rb and Cs–Cs distances are 4.20 and 4.26 Å, significantly shorter than in their elemental form (4.89 and 5.29 Å, respectively<sup>40,41</sup>), while Bi–Bi spacing is larger than in elemental Bi (3.47 vs 3.07 Å<sup>42</sup>) and in the  $\text{Bi}_4$  cluster (2.98 Å as obtained by *ab initio* structural relaxation). This highlights the electron transfer from the electropositive alkali metal to the Bi network.

To characterize superconducting transitions of  $\text{ABi}_2$ ,  $dc$  magnetization was measured in the temperature interval  $T = 1.9$ –5 K. The plot of low-field ( $H_{dc} = 20$  Oe) volume susceptibility ( $\chi_V$ ) versus temperature is shown in Figure 2a,b). Sharp transition to a full Meissner state ( $\chi_V$  reaching the value



**Figure 2.** (a,b) Temperature-dependent magnetic susceptibility of  $\text{RbBi}_2$  and  $\text{CsBi}_2$ . A sharp transition to the Meissner state is seen at the  $T_c$ . Susceptibility data were corrected for the demagnetization factor (see the text). (c,d) Field-dependent magnetization curves showing a typical type-I character of superconductivity for  $\text{RbBi}_2$  and an ambiguous type-I/type-II behavior for  $\text{CsBi}_2$ .

of  $-4\pi$  after correcting for the demagnetization effect) was observed in both materials. Very small difference between zero-field cooled and field-cooled (FC) magnetization (not shown) is indicative of high crystal quality.

Field-dependent magnetization below the critical temperature is shown in Figure 2c,d. In the case of RbBi<sub>2</sub>, the shape of the magnetization curve is consistent with a type-I superconducting transition with an influence of the demagnetization effect due to randomly oriented crystalline grains.<sup>13,43</sup> In CsBi<sub>2</sub>, the shape of the  $M$  versus  $H$  curve has a tail-like feature at higher fields, which is more consistent with type-II SC; however, the low critical field suggests type-I behavior. Assuming a perfect diamagnetic linear response to the magnetic field, the  $M_v$  versus  $H$  data at the lowest temperature ( $T = 1.92$  K and  $T = 1.95$  K for Rb- and Cs-bearing compound, respectively) were fitted with a linear function ( $M_{\text{fit}} = aH + b$ ). The value of the demagnetization factor ( $d$ ) is calculated using the equation  $-a = (4\pi(1 - d))^{-1}$ , yielding  $d = 0.676$  for RbBi<sub>2</sub> and  $d = 0.744$  for CsBi<sub>2</sub>.

The fields at which deviations from a linear response occur were taken as thermodynamic critical fields  $H_c^*$ . The  $H_c^*$  values derived for different temperatures are fitted with the equation  $H_c^*(T) = H_c^*(0)[1 - (T/T_c)^2]$ .<sup>44</sup> The values of critical field extrapolated to  $T = 0$  K using the fitted function are  $H_c^*(0) = 127$  Oe for RbBi<sub>2</sub> and  $H_c^*(0) = 146$  Oe for CsBi<sub>2</sub> (see Figure S2 of the Supporting Information). This value has to be corrected for the demagnetization factor, yielding  $H_c(0) = 188$  Oe and 196 Oe, respectively.

The heat capacity measured through the superconducting transition in ABi<sub>2</sub> is shown in Figure 3. Bulk nature of the superconductivity is confirmed by large, sharp anomalies at  $T_c$

= 4.24 K and 4.65 K for RbBi<sub>2</sub> and CsBi<sub>2</sub>, respectively. It is worth noting that under applied field, the jump at  $T_c$  becomes larger than at zero field in both compounds. A similar effect was observed, e.g., in KBi<sub>2</sub>,<sup>45</sup> ScGa<sub>3</sub>, LuGa<sub>3</sub>,<sup>46</sup> YbSb<sub>2</sub>,<sup>47</sup> ReAl<sub>6</sub>,<sup>48</sup> and LiPd<sub>2</sub>Ge<sup>49</sup> type-I superconductors. This suggests that both RbBi<sub>2</sub> and CsBi<sub>2</sub> can be classified as type-I superconductors. It is worth noting that type-I superconductivity, especially with  $T_c > 2$  K, is rather uncommon among intermetallic compounds.

Figure S3 of the Supporting Information presents the low-temperature  $C_p/T$  versus  $T^2$  plots for both materials. Electronic ( $\gamma$ ) and vibrational ( $\beta$ ) heat capacity contributions were extracted by fitting the data with relation  $C_p/T = \gamma + \beta T^2$ . The fit yields very similar  $\gamma$  values (5.0 and 4.9 mJ mol<sup>-1</sup> K<sup>-2</sup>) for both materials. The normalized heat capacity jumps at  $T_c$  estimated by using the equal entropy construction method (see insets of Figure 5a,b), are  $\Delta C_p/\gamma T_c = 2.03$  for RbBi<sub>2</sub> and  $\Delta C_p/\gamma T_c = 2.63$  for CsBi<sub>2</sub>, both well above the BCS limit for a weakly coupled superconductor (1.43).

The Debye temperature ( $\Theta_D$ ) is calculated from the  $\beta$  specific heat coefficients using the relation

$$\Theta_D = \sqrt[3]{\frac{12\pi^4 nR}{5\beta}}$$

This yields  $\Theta_D = 127(1)$  for RbBi<sub>2</sub> and 123(1) K for CsBi<sub>2</sub>, both values being slightly higher than for elemental Bi ( $\Theta_D = 112$  K). Taking  $\Theta_D$  and  $T_c$  values and assuming the value of the Coulomb pseudopotential parameter  $\mu^* = 0.13$ , the electron–phonon coupling parameter ( $\lambda_{\text{el-ph}}$ ) can be estimated using the modified McMillan formula

$$\lambda = \frac{1.04 + \mu^* \ln\left(\frac{\Theta_D}{1.45T_c}\right)}{(1 - 0.62\mu^*) \ln\left(\frac{\Theta_D}{1.45T_c}\right) - 1.04}$$

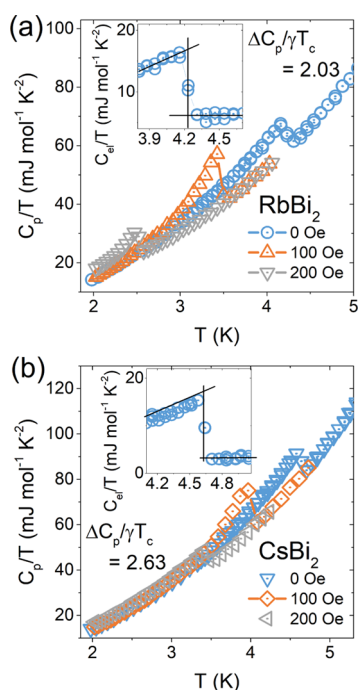
For RbBi<sub>2</sub>, this gives  $\lambda = 0.82$  and for CsBi<sub>2</sub>  $\lambda = 0.87$ , both values being indicative of moderate coupling strength.

Table 1 summarizes the normal and superconducting state parameters derived from experimental measurements.

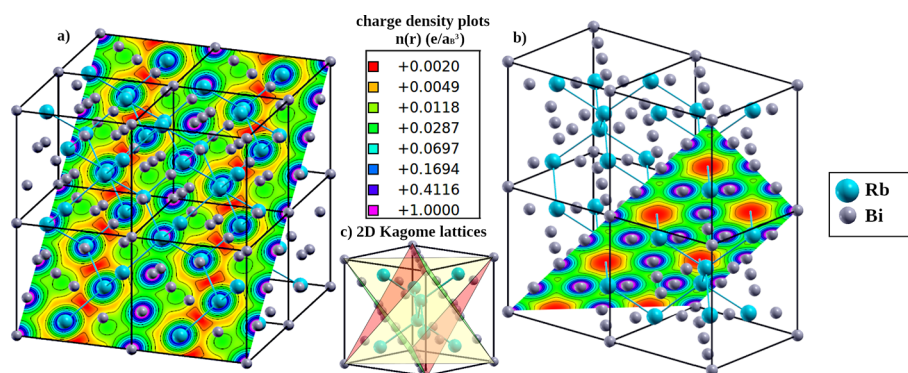
In order to gain insight into the role played by relativistic effects in the formation of superconducting state in the two compounds, we analyzed their electronic and phonon structure by means of *ab initio* calculations.

Charge transfer from the Rb/Cs to Bi is evident from the electronic density of RbBi<sub>2</sub> and CsBi<sub>2</sub> (Figure 4), and the Bader charge analysis yields Rb<sup>+0.71</sup>(Bi<sub>2</sub>)<sup>-0.71</sup> and Cs<sup>+0.64</sup>(Bi<sub>2</sub>)<sup>-0.64</sup>. This is consistent with electronegativity difference (0.82/0.79 vs 2.02 for Rb/Cs and Bi in the Mulliken scale, respectively) and the observed shortening of Bi–Bi bonds with respect to the elemental Bi. The density distribution along the Bi–Bi bonds has a strongly delocalized, metallic character. Since charge density is concentrated on the Bi framework, both compounds can be viewed as pyrochlore metals. As we will further show, the electron–phonon coupling resulting in superconductivity in ABi<sub>2</sub> ( $A = \text{Rb, Cs}$ ) also stems from the Bi pyrochlore sublattice.

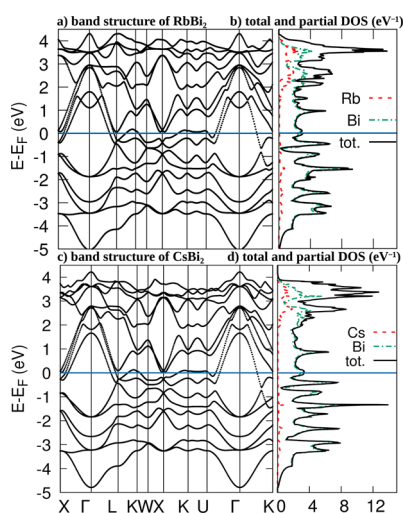
The electronic band structure and electronic density of states (DOS) for both compounds are shown in Figure 5. The band structure around the Fermi level is similar in both cases. The Fermi level lies within a peak of DOS; thus, even a small difference of band structure detailed below, lead to higher DOS at Fermi level in the case of CsBi<sub>2</sub> ( $\text{DOS}(E_F) = 1.51$



**Figure 3.** Low-temperature heat capacity of (a) RbBi<sub>2</sub> and (b) CsBi<sub>2</sub>, showing an anomaly at the superconducting critical temperature (enlarged in insets). The normalized heat capacity jump  $\Delta C_p/\gamma T_c$  is calculated using  $\gamma$  values estimated from a fit presented in Figure S2 of the Supporting Information. Note that in both cases, the jump under an applied magnetic field is found to be larger than at zero field, which is a typical behavior for type-I superconductors (see, e.g., refs 45–49).



**Figure 4.** Charge density of supercell of  $\text{RbBi}_2$  plotted in the (110) plane (a) and (111) plane (b); the charge density in (111) plane is similar to 2D kagome lattice marked; however, there are many of such planes in the unit cell (c) resulting in 3D character of electronic bonds.



**Figure 5.** Fully relativistic electronic band structure (a,c) and DOS (b,d) of  $\text{RbBi}_2$  and  $\text{CsBi}_2$ , respectively. Atomic contributions to DOS are marked with green (Bi) and red (Rb/Cs) lines.

**Table 1. Normal and Superconducting State Parameters for  $\text{RbBi}_2$  and  $\text{CsBi}_2$**

	$\text{RbBi}_2$	$\text{CsBi}_2$
$\gamma$ ( $\text{mJ mol}^{-1}\text{K}^{-2}$ )	5.0(4)	4.9(2)
$\beta$ ( $\text{mJ mol}^{-1}\text{K}^{-4}$ )	2.83(3)	3.11(5)
Debye temp. $\Theta_D$ (K)	127(1)	123(1)
critical temp. $T_c$ (K)	4.25	4.65
$\Delta C_p/\gamma T_c$	2.03	2.63
$\lambda$	0.82	0.87
$H_c(0)$ (Oe)	188(1)	196(5)

$\text{eV}^{-1}/\text{f.u.}$ ) than  $\text{RbBi}_2$  ( $\text{DOS}(E_F) = 1.31 \text{ eV}^{-1}/\text{f.u.}$ ), which is correlated with a higher transition temperature  $T_c$ , as discussed below.

The plot of DOS shows that the  $p$ -states of Bi contribute the majority of the total DOS around the Fermi level, being only slightly hybridized with  $s$  states of Rb/Cs. Bi  $6s$  states are positioned well below the  $E_F$  due to (scalar) relativistic effects.<sup>3</sup> Thus, both the metallic state and superconductivity in  $\text{ABi}_2$  arises from interacting  $6p$  states of Bi atoms. In the energy range from  $-2.5$  to  $3 \text{ eV}$  (with respect to  $E_F$ ) the shape of DOS is similar to the one of elemental bismuth. Particularly, the minimum at  $-0.8 \text{ eV}$  is similar to the one at Fermi level of pure Bi. Around the  $E_F$  the peak of DOS arises similarly to the

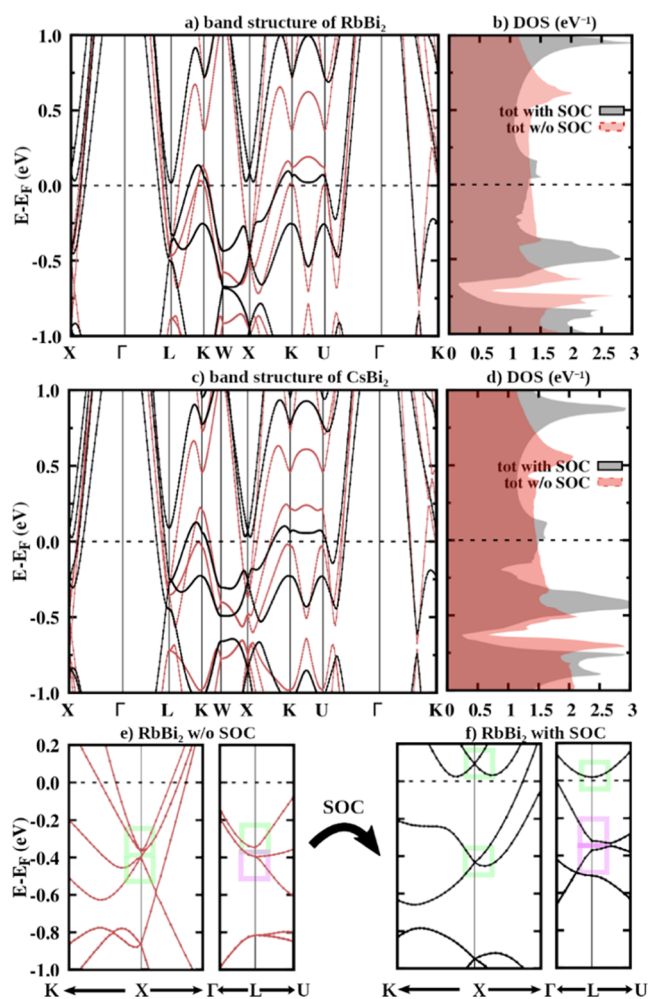
case of elemental Bi under pressure  $p = 2.7 \text{ GPa}$ , at which a phase transition to a monoclinic structure is observed and Bi becomes superconducting below  $T_c = 3.9 \text{ K}$ .<sup>50</sup> In this sense, the presence of Rb/Cs atoms impose a chemical pressure on the lattice of Bi atoms, leading to stronger  $6p$  orbital overlap and metallic bonding of the Bi framework.

Since the density of states is around the Fermi level is dominated by the  $\text{Bi}_4$  pyrochlore lattice, relativistic effects have a profound effect on the electronic structure. In Figure 6, the scalar and fully relativistic band structure is shown in a narrow energy range around  $E_F$ . In the case of  $\text{RbBi}_2$ , when SOC is not included, the Fermi level is positioned in the flat part of DOS, while with SOC, the local maximum appears and the Fermi level is situated on its slope.

The parabolic bands around  $\Gamma$  point with a large ( $3 \text{ eV}$ ) energy gap around the Fermi level are not affected by SOC. At many points of  $k$ -space (for example between  $K$  and  $U$  or  $X$  and  $\Gamma$  points), mainly below the Fermi level, the band crossings are removed by SOC.

Figure 7 shows the Fermi surface (FS) of  $\text{RbBi}_2$  and  $\text{CsBi}_2$  calculated with and without SOC. Since the differences in FS between the two compounds are negligible, we will discuss the  $\text{RbBi}_2$  case only. The only difference between the two compounds lies in the Fermi velocity which is slightly smaller in the case of  $\text{CsBi}_2$  in the  $[100]$  direction. This is consistent with a less dispersed character of bands around  $E_F$  and a higher DOS at the Fermi level of this compound.

In the scalar relativistic case, there are four bands per spin crossing the  $E_F$ , and thus four FS branches. First one (I in Figure 7a,d) has a dodecahedral shape with almost completely flat faces. It is similar to the Fermi surface of polonium which was concluded to lead to strong nesting.<sup>51–53</sup> The hybridization causes the presence of cone-like corners. Additionally, there are small pockets around  $K$  and  $U$  points. This part of the Fermi surface is associated with the band which is approximately parabolic around the  $\Gamma$  point. The second branch (II) contains many cylinders and is associated with a flat band at the  $K-U$  line. The third and fourth branches of the Fermi surface (III and IV in Figure 7a,d) consist of small pockets centered at  $X$  and  $L$  points. At the  $X$  point, all four bands degenerate to two points, both ca.  $0.5 \text{ eV}$  below the Fermi level. The SOC shifts them leaving one below and one above the  $E_F$ . In the fully relativistic case, the Fermi surface is reduced to just two branches: the dodecahedral and the cylindrical one, both centered at  $\Gamma$ . Small conical pockets of branch I are removed.



**Figure 6.** Electronic band structure (a,c) and DOS (b,d) of RbBi<sub>2</sub> and CsBi<sub>2</sub>, respectively, calculated in a scalar- (without SOC; red line) and fully relativistic approach (with SOC; black). Panels (e,f) show the band structure around the Brillouin zone center (Γ) for RbBi<sub>2</sub>. At the X point, the degeneracy is symmetry-protected, so the inclusion of SOC results only in shifting the band energies (points marked with green rectangles), while at L-point they are additionally split (purple rectangles).

The degeneracy of bands at X-point is symmetry-enforced and leads RbBi<sub>2</sub> and CsBi<sub>2</sub> to be classified topologically as ESFD (enforced semimetals with Fermi degeneracy).<sup>54</sup> The two compounds might be interesting for studying the interplay of superconductivity and topologically nontrivial states. Despite the vanishing FS pockets and the change in the general shape of DOS function around the Fermi level, the value of DOS at the E<sub>F</sub> of RbBi<sub>2</sub> is almost unchanged by SOC (a negligible decrease from 1.35 to 1.31 eV<sup>-1</sup>/f.u. is seen). The reduction of the number of FS branches is compensated by the reduction of the Fermi velocity (see Figure 7a,b), as lower velocity leads to a higher density of states.

Since the electronic structure is strongly affected by the inclusion of the spin-orbit coupling, it is interesting how the changes are reflected in the vibrational structure. Calculated phonon band structures of RbBi<sub>2</sub> and CsBi<sub>2</sub> are shown in Figure 8 and 9. In contrast to the electronic structure, the phonon dispersion curves (Figures 8a,d and 9a,d) and density of states (Figures 8c,f and 9c,f) of the two compounds differ significantly.

The SOC has a major influence on phonons. When it is not taken into account, the vibrational structure of RbBi<sub>2</sub> is rich in softened modes, suggesting the instability of the structure. When SOC is included, the softening of modes disappears, indicating a stabilization by relativistic effects. This is consistent with the lack of period 5 pyrochlore analogues of RbBi<sub>2</sub> and CsBi<sub>2</sub> (e.g., RbSb<sub>2</sub> is a semiconductor with a monoclinic structure<sup>55</sup>), as relativistic effects, stabilizing the perfect pyrochlore lattice, are much weaker in Sb.

The phonon spectrum contains 18 modes, as the primitive cell of RbBi<sub>2</sub> contains six atoms (2 formula units). Phonon modes coming from Bi and Rb atomic vibrations are not strongly separated from each other as it is, e.g., in the case of LiBi<sup>8</sup> or CaBi<sub>2</sub>.<sup>14</sup> However, the three acoustic modes and low-frequency optic modes (up to  $\omega = 1.7$  THz) are mainly associated with Bi atoms vibrations, while high-frequency modes (in the range  $\omega = 1.7$ –2.5 THz) come mostly from Rb. Transverse acoustic (TA) modes degenerate along the X–Γ–L path and split in the *xy* plane along W–Γ–K. The optical modes coming from Bi lie within a narrow frequency range  $\omega = 1.1$  to 1.4 THz and a part of them is almost flat, resulting in a peak in the phonon DOS. The exception is the highest mode, which is the breathing mode of a pyrochlore network<sup>56–59</sup> associated with a movement of Bi atoms toward the center of the tetrahedron and breaking of the inversion symmetry of the lattice (see Figure 9e).

The vibrations of atoms along the line, as in case of this mode is only a special case of trajectory of atoms, generally described by formula

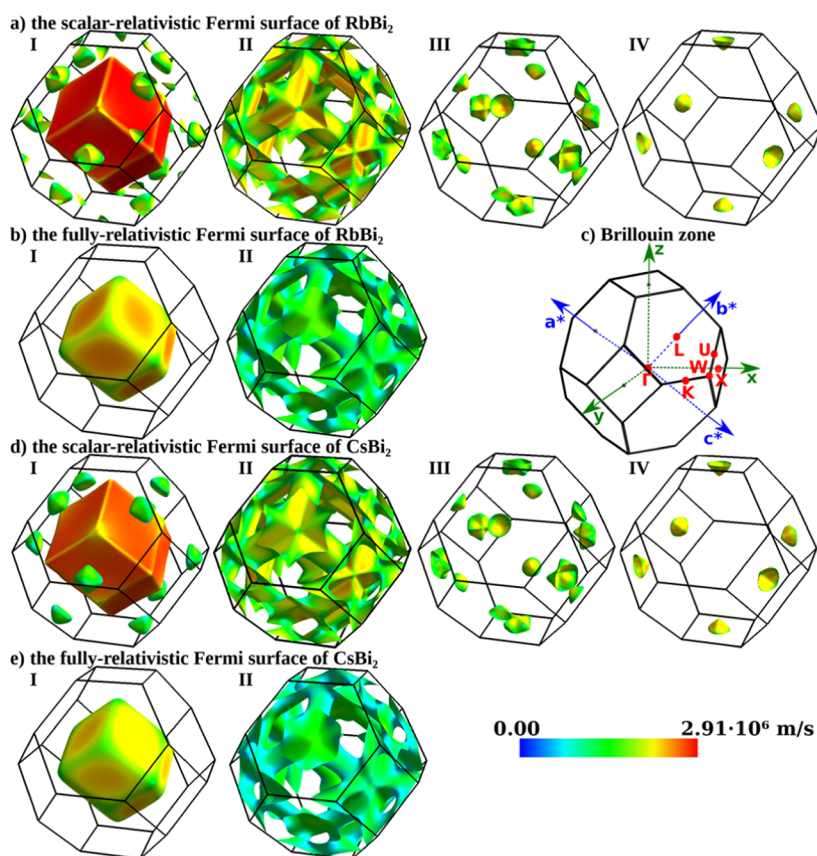
$$\begin{aligned} \mathbf{r}_s(t) &= \text{Re}(\widehat{\epsilon}_{\nu s} \exp(i(\mathbf{q} \cdot \mathbf{R} - \omega_\nu t))) \\ &= \text{Re}(\widehat{\epsilon}_{\nu s}) \cdot \cos(\omega_\nu t + \mathbf{q} \cdot \mathbf{R}) + \text{Im}(\widehat{\epsilon}_{\nu s}) \cdot \sin(\omega_\nu t + \mathbf{q} \cdot \mathbf{R}) \end{aligned}$$

where  $\mathbf{r}_s(t)$  is the position of atom *s* in time *t*, with crystallographic position  $\mathbf{R}$ ,  $\widehat{\epsilon}_{\nu s}$  is its polarization vector associated with phonon mode  $\nu$  with frequency  $\omega_\nu$  and all is considered in the  $\mathbf{q}$ -point of the space of wave vectors.

With one of the part (real or imaginary) of polarization vector equal to zero, atoms vibrate along the line with frequency  $\omega$  and direction given by the polarization vector. When both parts are non-zero, the atomic trajectory is an ellipsoid. If additionally both parts are equal, the ellipsoid becomes a circle. Such a case has been found in many  $\mathbf{q}$  points of phonon dispersion of RbBi<sub>2</sub>. Two examples are shown in Figure 8h,i. At the K point, Rb atoms are moving circularly, while Bi atoms move along a line. At the W point, all atoms are moving along a circle/ellipse (see the animation of the atomic vibrations in the Supporting Information). These modes might be candidates for chiral phonons which arise due to symmetry of the crystal structure and have been recently found in ABI compounds, including RbBi and CsBi<sup>60</sup> (the occurrence of chiral phonons in ABI<sub>2</sub> compounds is discussed in more detail in ref 61).

The phonon spectrum of CsBi<sub>2</sub> is qualitatively different from RbBi<sub>2</sub>. When SOC is neglected, the modes are not only softened as it is in the case of RbBi<sub>2</sub> but the spectrum is also rich in imaginary frequencies, suggesting structural instability. Inclusion of the SOC removes the imaginary frequencies; thus, the relativistic effect of SOC is crucial for the stability of the cubic Laves structure of CsBi<sub>2</sub>.

As visualized in Figure 9, the soft mode is associated with a movement of Bi atoms toward the center of faces of tetrahedron. As is highlighted in the electronic charge density



**Figure 7.** Fermi surface of RbBi<sub>2</sub> (a,b) and CsBi<sub>2</sub> (d,e) calculated without SOC (a,d) and with SOC (b,e), colored according to Fermi velocity. The Brillouin zone with high symmetry points is shown in panel (c).

plot (Figure 4b), this point is characterized by large electronic charge density associated with metallic bonds of close-packed Bi tetrahedron. Thus, this mode may be seen as movement of positively charged Bi ions, which are attracted to the region of a large, negative charge density, leading to lowering of frequency.

When SOC is included, the p orbital is contracted; thus, the metallic bonds are slightly weakened and the electronic density on the faces of tetrahedra is reduced (see Figure S6 of the Supporting Information, where the difference of electronic charge density, calculated with and without SOC, is presented). This leads to the changes in the vibrational structure: the Bi atoms move in different direction and the imaginary frequencies disappear. As we checked, similar change of displacement vectors of atoms is associated with the disappearance of softened modes of RbBi<sub>2</sub>. This behavior may suggest that the softening arises from a Kohn anomaly caused by an electronic effect of nesting of the Fermi surface, which would be an interesting matter of further studies.

The influence of electronic surrounding on phonons is highlighted by a large phonon linewidth of discussed modes, shown in Figures 8a and 9a in a fat band representation. It is defined as

$$\gamma_{q\nu} = 2\pi\omega_{q\nu} \sum_{ij} \int \frac{d^3k}{\Omega_{\text{BZ}}} |g_{q\nu}(\mathbf{k}, i, j)|^2 \times (E_{k_j} - E_F)\delta(E_{k+\mathbf{q},i} - E_F)$$

where electron–phonon coupling matrix element

$$g_{q\nu}(\mathbf{k}, i, j) = \sum_s \sqrt{\frac{\hbar}{2M_s\omega_{q\nu}}} \langle \psi_{i,\mathbf{k}+\mathbf{q}} \left| \frac{dV_{\text{SCEF}}}{d\hat{u}_{\nu s}} \cdot \hat{\epsilon}_{\nu s} \right| \psi_{jk} \rangle$$

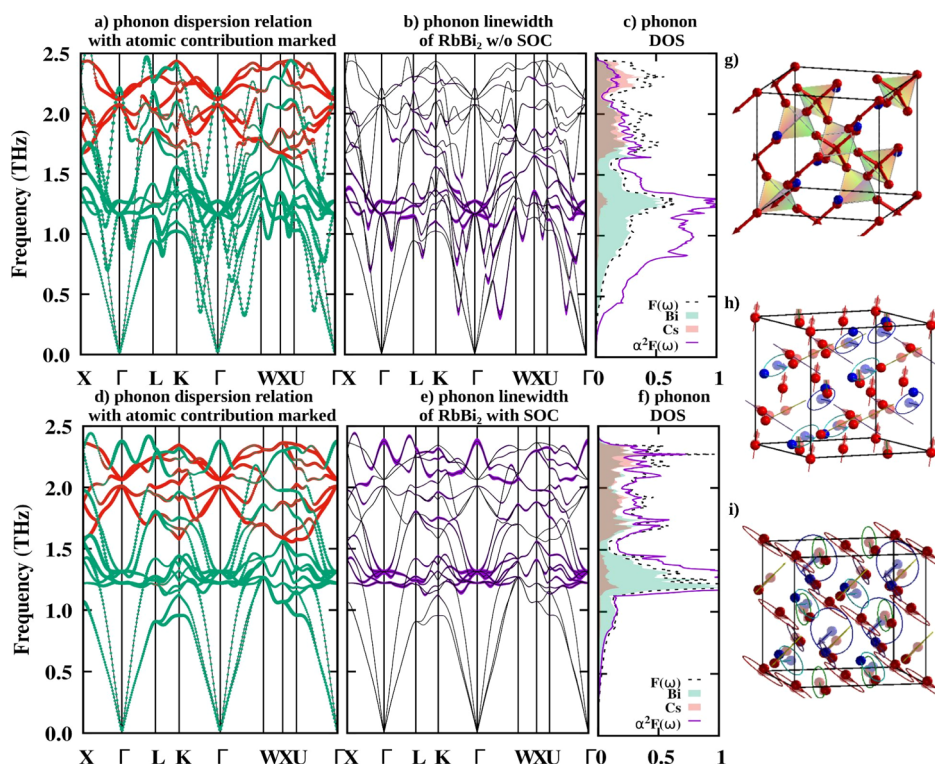
describes how the electronic potential is changed by an atomic displacement,  $\omega_{q\nu}$  is a frequency of the  $\nu$ -th mode with a wave vector  $\mathbf{q}$  (equal to a difference of wave vectors of two electronic states  $\psi_{i,\mathbf{k}+\mathbf{q}}\psi_{jk}$ ) with a polarization vector  $\hat{\epsilon}_{\nu s}$ , associated with a displacement  $\hat{u}_{\nu s}$  of  $s$ -th atom of a mass  $M_s$ . Dirac delta functions ensure that only the electronic states near the FS are included in calculation.

On the other hand, the EPC matrix influences the electron–phonon part of dynamical matrix, given by<sup>62</sup>

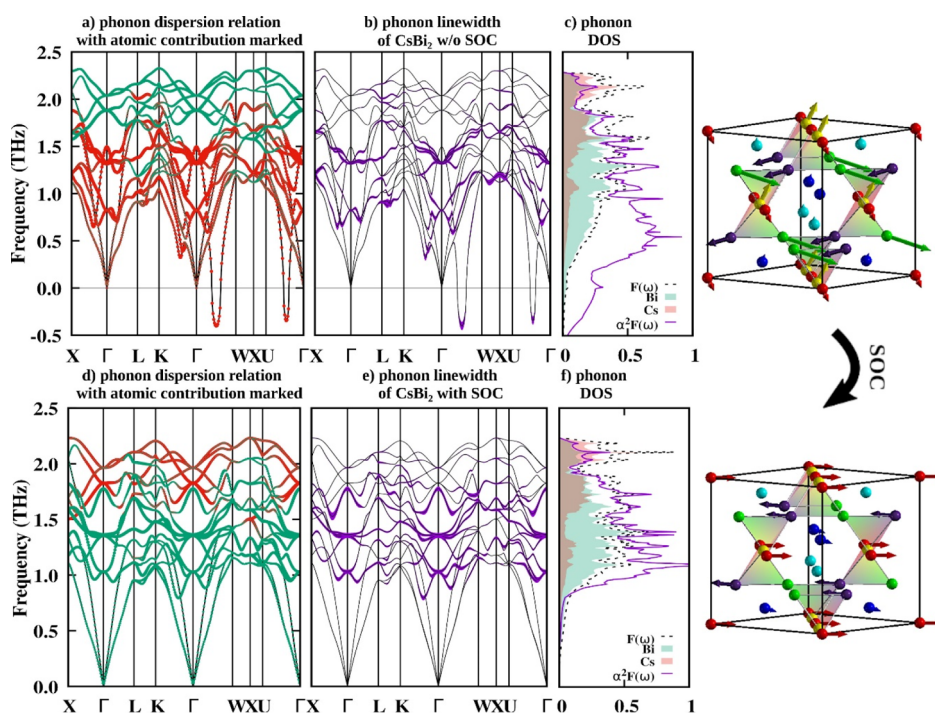
$$\Phi^{\text{EP}}(q)_{\kappa\kappa'\alpha\alpha'} = \frac{2}{N} \sum_{mnk} \frac{f_{k+\mathbf{q},n} - f_{k,n}}{E_{k+\mathbf{q},n'} - E_{k,n}} (g_{q\nu}(\mathbf{k}, i, j))^*{}^{\kappa\alpha} (g_{q\nu}(\mathbf{k}, i, j))^{\kappa'\alpha'}$$

where  $E_{k,n}$  and  $f_{k,n}$  are energy and occupancy of the  $n$ -th band at  $k$ -th point,  $N$  is a number of unit cells. The phonon frequencies are the eigenvalues of the dynamical matrix normalized by atomic masses. In consequence, the higher value of the EPC matrix leads to lower frequency. As a consequence, the phonon softening and phonon linewidth are associated with each other, as both depend on the EPC matrix and geometry of FS. It is visible in Figures 8a and 9a, where the softened modes are characterized by large phonon linewidth.

It is worth noting that not all softened modes disappeared with SOC. Many of softened optical modes survived and their large phonon linewidth demonstrates that their softening is



**Figure 8.** Panels (a,b,d,e): phonon dispersion relation of  $\text{RbBi}_2$  with phonon linewidth proportional to the thickness of the purple line. Panels (c,f) show the phonon DOS (dashed black line) with atomic contribution marked in green (Bi) and red (Rb) and the Eliashberg function (purple line) normalized to  $3N$  ( $N$  being a number of atoms per unit cell), calculated without SOC (a–c) and with SOC (d–f). In panel (g), the vibrational direction associated with the highest mode at  $\Gamma$  is marked with arrows attached to atoms of elementary crystal cell (in real space). Similarly, the trajectory of atoms associated with two examples of possible chiral modes: second mode at  $K$  and fifth at  $W$  are shown in panels (h,i). The Rb and Bi atoms are marked with blue and red spheres, respectively.



**Figure 9.** Phonon dispersion relation of  $\text{CsBi}_2$  together with phonon linewidth (a,b,d,e) and its phonon DOS together with atomic contribution to phonon DOS and Eliashberg function, calculated w/o SOC (a–c) and with SOC (d–f). The color scheme is the same as in Figure 8. The soft mode, which appears along  $\Gamma$ – $W$  in the scalar-relativistic case, is marked in real space with arrows (yellow, red, green, and purple balls are Bi, and light and dark blue are Cs).

due to strong EPC, showing their importance for superconductivity. This is an important factor in the formation of the superconducting state, as the inclusion of SOC stabilizes the phonon structure to the point where the compound becomes dynamically stable, but softened modes provide a sizable contribution to the electron–phonon coupling.

The influence of SOC on  $ABi_2$  family is similar to the case of other family of Bi-rich superconductors,  $ABi_3$ , which crystallize in a simple cubic  $AuCu_3$ -type structure, within which all the  $A$ –Bi and Bi–Bi distances are equal. In the case of lighter  $SrBi_3$ , the SOC only removes softened modes with large phonon linewidth, while in the case of heavier  $BaBi_3$ , it also stabilizes the structure. In addition, both Ba- and Bi-derived modes of  $BaBi_3$  are lower than in the case of  $SrBi_3$ , leading to nearly 30% larger value of EPC constant, which is equal to 1.43 and 1.11, respectively.<sup>16</sup> In the  $ABi_2$  family, the substitution of lighter Rb with heavier Cs leads to only about 10% larger EPC constant.

Modes associated with Cs atoms have lower frequency than those associated with Rb (average frequency of Cs is 9% lower than that of Rb, see Table 2). This is expected since Cs is over

**Table 2. Summary of Calculated Properties of  $RbBi_2$  and  $CsBi_2$  Compared to Experimental Results (Marked with Label Expt)<sup>a</sup>**

	$RbBi_2$		$CsBi_2$	
	w/o SOC	w. SOC	w/o SOC	w. SOC
$N(E_F)/f.u.$	1.35	1.31	1.46	1.51
$\lambda_{\text{expt}}$		0.82		0.87
$\lambda$	2.06	0.81		0.92
$\bar{\omega}$	1.59	1.61		1.51
	Rb: 1.91	Rb: 1.85		Cs: 1.69
	Bi: 1.36	Bi: 1.45		Bi: 1.38
$\omega_{\text{in}}$	0.85	1.74		1.27
$T_c$	6.18	3.31		3.85
$T_c$ (expt.)		4.24		4.65

<sup>a</sup>The density of states is given in units of  $eV^{-1}/f.u.$ , both mean frequency  $\bar{\omega}$  and logarithmic frequency  $\omega_{\text{in}}$  in units of THz and critical temperatures in K.

55% heavier than Rb. The average frequency of Bi is of 5% lower in  $CsBi_2$  than in  $RbBi_2$ . Surprisingly, not all modes of Bi are lowered leading to a completely different shape of phonon DOS, where the peak around 1.3 THz is spread out.

In order to better describe the difference between the phonon structures of  $CsBi_2$  and  $RbBi_2$ , dispersion relations around the  $\Gamma$  point are plotted and the modes associated with similar movement of atoms are marked with the same color in Figure 10. Additionally, modes associated with the movement of Bi atoms are visualized in Figure 10c–f and force constants between atoms are shown in Figure 10g. The modes associated with a movement of both Bi (along Bi–Bi bond) and Cs/Rb (Figure 10d) are lowered from 1.31 in the case of  $RbBi_2$  to 1.03 THz in  $CsBi_2$ , while the frequency of modes associated with a movement of Bi toward the empty space around Cs/Rb (Figure 10c,e) are increased from 1.22 THz and 1.32 THz in  $RbBi_2$  to 1.36 THz in  $CsBi_2$ .

This may be caused by a difference in the unit cell size, which is larger in the case of  $CsBi_2$ ; thus, the Bi–Bi metallic bonding is slightly weaker leading to smaller force constants of Bi–Bi pairs (see Figure 10h) and lower frequencies of modes associated with a movement of Bi along Bi–Bi bonds. For the

same reason, the highest optical mode associated with a movement of Bi toward the center of tetrahedron (Figure 10f) is lowered from 2.37 THz in the case of  $RbBi_2$  to 1.78 THz in  $CsBi_2$ . It is similar to the case of soft mode shown in Figure 9e and explains why the effect of softening is stronger in the case of  $CsBi_2$ . On the other hand, the force constants of Bi–Cs pairs are larger than of Bi–Rb pairs, leading to a higher frequencies of modes associated with movements of Bi toward the space around Cs. These changes show that the substitution of Rb by Cs not only lowers the frequency due to a larger mass but also influences the size of the unit cell and modifies the bonding of the Bi network.

In both compounds, the phonon linewidths are large only in case of Bi modes. Since the FS is also dominated by  $6p$  states of Bi, the superconductivity in  $ABi_2$  is driven by the Bi pyrochlore lattice, as the electron–phonon coupling in both electronic and phonon ways is almost exclusively contributed by Bi.

On the basis of the phonon linewidth, the Eliashberg function is calculated

$$\alpha^2F(\omega) = \frac{1}{2\pi N(E_F)} \sum_{\mathbf{q}\nu} \delta(\omega - \omega_{\mathbf{q}\nu}) \frac{\gamma_{\mathbf{q}\nu}}{\hbar\omega_{\mathbf{q}\nu}}$$

The Eliashberg function is effectively the phonon DOS weighted by a phonon linewidth divided by phonon energy and density of electronic states at the Fermi level.

Eliashberg function of  $RbBi_2$ , calculated without SOC, is the highest at low frequencies (up to 1.5 THz) due to the presence of softened acoustic modes and low-frequency optical modes. When SOC is included, the Eliashberg function becomes similar to phonon DOS, which means that electron–phonon coupling only weakly depends on phonon frequency. The largest contribution to Eliashberg function comes from highly degenerate and partially flat Bi modes in the narrow frequency range.

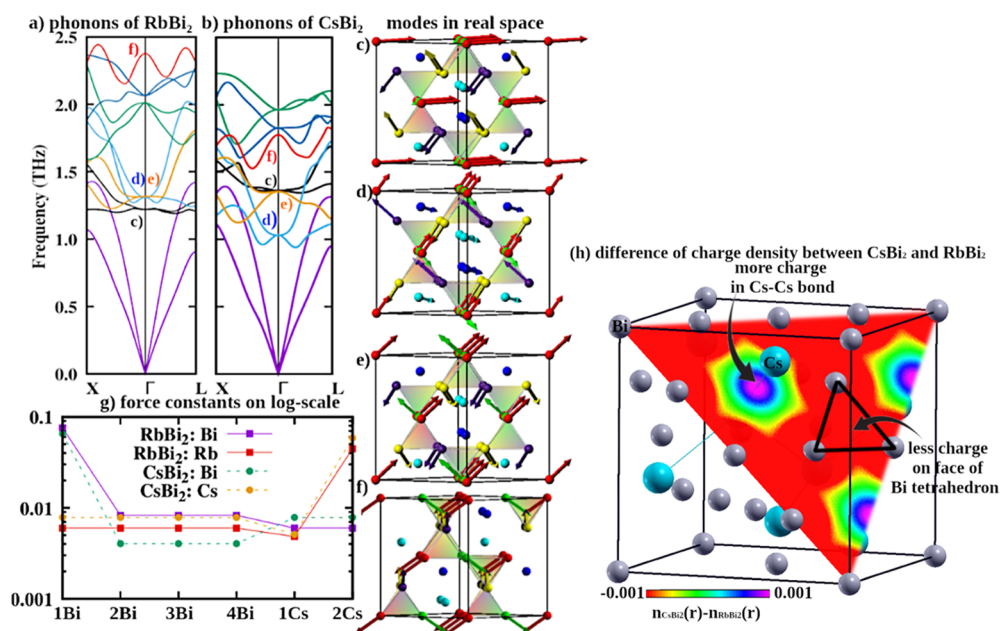
Having the Eliashberg function, we can calculate the electron–phonon coupling constant

$$\lambda = 2 \int_0^{\omega_{\text{max}}} \frac{\alpha^2F(\omega)}{\omega} d\omega$$

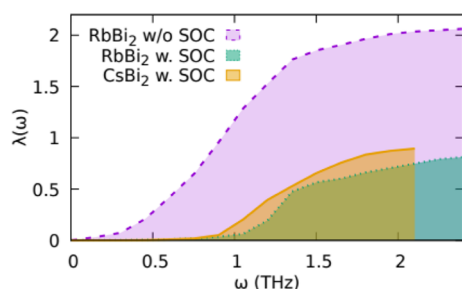
It is essentially proportional to phonon linewidth divided by frequency squared; thus, the low frequency modes contribute more than higher ones. Obtained values are shown in Table 2. When SOC is not included, the EPC constant of  $RbBi_2$   $\lambda = 2.06$ , is more than twice larger than the experimental value (Table 1). The cumulative EPC constant shown in Figure 11 clearly shows that such a high value is caused by softened modes, having low frequency and large phonon linewidth. When SOC is included, the softening disappears and the EPC constant decreases to  $\lambda = 0.81$  in excellent agreement with the value estimated from the experiment  $\lambda = 0.82$  and is mostly delivered by acoustic and optical Bi modes, as  $\lambda = 0.82$  and is mostly delivered by acoustic and optical Bi modes, as the phonon linewidth is the highest for these modes. The calculated EPC constant of  $CsBi_2$   $\lambda_{\text{ep}} = 0.92$  is also in a good agreement with the experimental value  $\lambda_{\text{ep}} = 0.87$ . It is slightly larger than in case of  $RbBi_2$  due to a shift of part of modes to lower frequencies and slight changes in band structure.

The impact of the electronic structure on EPC can be measured using the integral





**Figure 10.** Phonon dispersion relation of RbBi<sub>2</sub> (a) and CsBi<sub>2</sub> (b) calculated with SOC and visualization of modes at  $\mathbf{q} = (0, 0, 0)$  in real space (c–f) using the same color scheme as in Figure 9. Additionally, the force constants between nearest pairs of atoms are shown in panel (g). The unit cell contains two formula units; thus, there are four atoms of Bi and two atoms of Cs. The force constants of Bi–Bi pairs are weaker in CsBi<sub>2</sub> than RbBi<sub>2</sub>, while Cs–Cs force constants are stronger than Rb–Rb. In panel (h), the difference of electronic charge density between the case of CsBi<sub>2</sub> and RbBi<sub>2</sub> is shown and the strengthening of the Cs–Cs bond in comparison to Rb–Rb together with weakening of Bi–Bi bonding in CsBi<sub>2</sub> in comparison to RbBi<sub>2</sub> is visible. As argued, it is a result of a larger unit cell, which leads to weaker Bi–Bi bonding, while Cs atoms, being larger than Rb, are bonded stronger in agreement with Bader analysis, which shows weaker ionization of Cs atoms than Rb atoms [Rb<sup>+0.71</sup>(Bi<sub>2</sub>)<sup>-0.71</sup> vs Cs<sup>+0.64</sup>(Bi<sub>2</sub>)<sup>-0.64</sup>].



**Figure 11.** Cumulative EPC constant of RbBi<sub>2</sub> and CsBi<sub>2</sub>.

$$I = \int_0^{\omega_{\max}} \alpha^2 F(\omega) \cdot \omega \, d\omega$$

Which does not depend on phonon frequency, as

$$I = \frac{1}{N(E_F)} \sum_{i,j} \int \frac{d^3k}{\Omega_{\text{BZ}}} \left| \sum_s \frac{1}{\sqrt{2M_s}} \left\langle \psi_{i,k+q} \left| \frac{dV_{\text{SCF}}}{d\mathbf{u}_{vs}} \right| \psi_{j,k} \right\rangle \right|^2 \cdot \delta(E_{k_i} - E_F) \delta(E_{k+q,j} - E_F)$$

In a monoatomic case, this integral is closely related to the McMillan–Hopfield parameter. The calculated values of the integral are 0.90 and 1.26 THz<sup>2</sup> for RbBi<sub>2</sub> and CsBi<sub>2</sub>, respectively. This suggests that, in addition to the lowering of frequency, the slight changes of the electronic structure resulting in lowering the Fermi velocity and increased DOS( $E_F$ ) strengthen the EPC.

On the basis of calculated EPC constant the critical temperature can be calculated with the help of the Allen–Dynes equation<sup>63</sup>

$$T_c = \frac{\omega_{\text{ln}}}{1.20} \exp\left(-\frac{1.04(1 + \lambda)}{\lambda - \mu^*(1 + 0.62\lambda)}\right)$$

where

$$\omega_{\text{ln}} = \exp\left(\frac{\int_0^{\omega_{\max}} \alpha^2 F(\omega) \ln(\omega) \frac{d\omega}{\omega}}{\int_0^{\omega_{\max}} \alpha^2 F(\omega) \frac{d\omega}{\omega}}\right)$$

is a logarithmic average of frequency. In the case of RbBi<sub>2</sub>,  $\lambda = 0.81$  and  $\omega_{\text{ln}} = 1.74$  THz (equivalent to 83.5 K) leading to  $T_c = 3.23$  K (the standard value of  $\mu^* = 0.1$  is assumed), reasonably close to the measured value 4.24 K, considering that even a small underestimation of the electron–phonon coupling parameter has a profound effect on the estimated  $T_c$ . In the case of CsBi<sub>2</sub>, EPC constant in larger  $\lambda = 0.92$  leading to higher  $T_c = 3.85$  K despite of lower logarithmic frequency. The estimated critical temperature is reasonably close to the experimental value  $T_c = 4.65$  K. Both experimental and calculated values lead to a conclusion that CsBi<sub>2</sub> has higher critical temperature than RbBi<sub>2</sub> due to slightly stronger electron–phonon coupling.

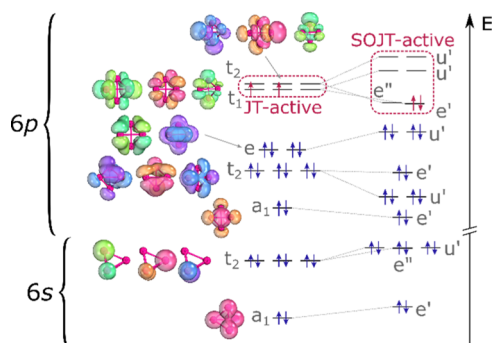
In summary, the structural arrangement of Bi atoms into a pyrochlore network of Bi tetrahedra intercalated with alkali metal atoms, resulting in a relatively high electron–phonon coupling constant. This emerges as a combination of both aforementioned factors: the large electronic density within the close-packed Bi atoms in Bi<sub>4</sub> tetrahedra allows for the strong interaction of phonon modes with electrons (large phonon linewidths), whereas the tetrahedra themselves are relatively loosely packed within the unit cell with a large amount of “free space” filled only by Rb/Cs atoms. This, in combination with high atomic mass of Bi, results in relatively low Bi phonon

frequencies, enhancing the EPC. Recently, we discussed a similar situation in isostructural Laves phase superconductors:  $\text{SrRh}_2$  and  $\text{SrIr}_2$ , where the pyrochlore lattice or Rh/Ir was found to be responsible for the emergence of strong-coupling superconductivity.<sup>59</sup>

On the other hand,  $\text{RbBi}_2$  and  $\text{CsBi}_2$  are in contrast with  $\text{CaBi}_2$ , which crystallizes in an orthorhombic structure that can be viewed in a distorted Laves phase structure, in which tetrahedra are broken to Bi–Bi and Ca–Bi planes separated from each other. Here, the phonon linewidths are smaller and average Bi frequencies are higher, leading to the EPC constant  $\lambda_{\text{ep}} = 0.54$ , much lower than  $\lambda_{\text{ep}} = 0.82$  and  $\lambda_{\text{ep}} = 0.87$  for  $\text{RbBi}_2$  and  $\text{CsBi}_2$ , respectively, despite the value of  $I = 1.17 \text{ THz}^2$  lying between  $\text{RbBi}_2$  and  $\text{CsBi}_2$  cases. This results in a lower critical temperature ( $T_c = 2.0 \text{ K}$  for  $\text{CaBi}_2$ ).<sup>13,14</sup>

Electron population analysis on  $\text{RbBi}_2$  shows that the  $\text{DOS}(E_F)$  is contributed mostly by electrons occupying nearest-neighbor Bi–Bi antibonding states (see Figure S4 of the Supporting Information). A hypothetical neutral Bi pyrochlore lattice would have its  $E_F$  lying close to a pseudogap. The electrons donated by Rb increase the antibonding population, destabilizing the lattice. Unfortunately, with the currently available computational tools (either direct in case of local basis set or indirect—via projection of plane-wave wave functions to a local orbitals set<sup>64–67</sup>), the bonding population analysis can only be performed in a scalar-relativistic case. While for bonding of lighter elements, SR approximation is reasonably applicable, the chemical bonding in 6th and 7th period elements is heavily influenced by SOC effects.<sup>68,69</sup> A possible solution for reliable population analysis of compounds of the heaviest elements is via the localized Wannier spinors.<sup>70</sup>

The calculated electronic structure of the  $\text{Bi}_4$  cluster (shown in Figure 12) are in general consistent with the previous results



**Figure 12.** Molecular orbitals of a tetrahedral  $\text{Bi}_4$  cluster. Note that for clarity of the picture, the energy scale (right) is divided into two parts, as the separation between lower  $t_2$  and higher  $a_1$  levels is on the order of 8 eV, while for comparison the  $t_2$ – $e$  splitting is ca. 0.5 eV.

by Lohr and Pyykkö obtained by means of relativistically parametrized extended Hückel method,<sup>71</sup> although the ordering of virtual orbitals is slightly different. The stabilizing effect of SOC on  $\text{ABi}_2$  can be qualitatively understood by considering the electronic structure of a  $T_d$   $\text{Bi}_4$  cluster. First, in a heavy element, such as Bi, scalar-relativistic effects result in a complete energetic separation of 6s and 6p orbitals.<sup>3</sup> Thus, only the p orbitals participate in the bonding. Second, the SOC splits the 6p atomic level into  $p_{1/2}$  and  $p_{3/2}$  separated by ca. 2 eV in a free atom. In the scalar-relativistic approximation the neutral  $\text{Bi}_4$  cluster is a closed-shell system with four electrons occupying the doubly degenerate  $e$  HOMO level. With two

additional electrons donated by electropositive species, the  $\text{Bi}_4^{2-}$  is first-order Jahn–Teller (JT) active due to two electrons occupying a triply degenerate  $t_1$  level. SOC splits the 6p-derived levels (6s-derived lower  $t_2$  level is also weakly split due to small admixture of the p character), lifting the triple degeneracy of  $t_1$  and  $t_2$ . The two additional electrons now occupy a  $e'$  ( $\Gamma_6$ ) level, quasi-degenerate ( $\Delta E \approx 0.02 \text{ eV}$ ) with the next  $e''$  ( $\Gamma_7$ ) leading to structural stabilization. However, the splitting of the  $e'$  and the two  $u'$  ( $\Gamma_8$ ) levels is relatively small ( $\Delta E \approx 0.9$  and  $1.2 \text{ eV}$ , respectively), resulting in a possibility of a second-order JT instability, as pointed out by Lohr and Pyykkö.<sup>71</sup> While the electronic structure of the crystalline  $\text{ABi}_2$  compound is much more complex than of isolated cluster, the stabilizing effects of SOC similarly stem from the lifted p orbital degeneracy, while the weakened but persistent mode softening can be considered an effect of a second-order JT (SOJT) effect.

This observation suggests a criterion for finding new superconductors: one may look for compounds stabilized by strong SOC, which should show relatively strong electron–phonon coupling while avoiding crystal structure distortion. Examples of such SOC stabilized superconductors can be found among Sb-, Bi-, and Pb-rich intermetallic phases featuring hypervalent polyanions, listed in Table 3. The

**Table 3. Superconductors Featuring Sb-, Te-, Bi-, and Pb-Based Hypervalent Polyanions**

material	hypervalent network	$T_c$
$\text{Ba}_3\text{TiTe}_5$	1d $\text{Te}^-$ chains	6 K ( $p = 37 \text{ GPa}$ ) <sup>75</sup>
$\text{YbSb}_2$	2d $\text{Sb}^-$ square network	1.3 K <sup>47,76</sup>
$\text{LiBi}$	2d $\text{Bi}^-$ square network	2.5 K <sup>8,19</sup>
$\text{NaBi}$	2d $\text{Bi}^-$ square network	2.15 K <sup>7</sup>
$\text{CaBi}_2$	2d $\text{Bi}^-$ square network	2.0 K <sup>13</sup>
$\text{Ba}_2\text{Bi}(\text{Bi}_x\text{Sb}_{1-x})_2$	2d Sb/Bi “square-honeycomb”	max. 4.4 K <sup>18,77</sup>
$\text{LaPb}_3$	3d $\text{Pb}^-$ cubic network	4 K <sup>78</sup>
$\text{LaBi}_3$	3d $\text{Bi}^-$ cubic network	7.3 K <sup>79</sup>

$(\text{Bi}_4)^{2-}$  pyrochlore lattice can be considered as hypervalent based on the valence electron count argument. The neutral Bi atom is three electrons short of octet, and thus, with four covalent bonds in the pyrochlore lattice, it is already electron-rich. The two electrons donated by two Rb/Cs atoms increase the electron count further, resulting in an even more hypervalent anionic network.

$\text{KBi}_2$ ,  $\text{RbBi}_2$ , and  $\text{CsBi}_2$  belong to a large family of cubic Laves (C-15) superconductors. The SuperCon database lists 192 C-15 superconductors, belonging to 16 different chemical systems, with critical temperatures ranging from 0.7 K to 10.7 K. However, the three Bi-based compounds distinguish themselves from the whole family in a number of ways. First, besides  $\text{LaAl}_2$  ( $T_c \approx 3 \text{ K}$ )<sup>72</sup> and  $\text{LaMg}_2$  ( $T_c \approx 1 \text{ K}$ ), they are the only main-group element-based Laves superconductors. Second, we have shown (based on electronic and vibrational structure, and electron–phonon coupling calculations) that in  $\text{RbBi}_2$  and  $\text{CsBi}_2$  systems, the superconductivity clearly emerges from the electron-rich Bi pyrochlore lattice, with Rb and Cs acting predominantly as electron donors to the Bi lattice. Such a clear picture cannot be drawn in the case of transition-metal-based systems, where the bonding between atoms occupying the two crystal sites is expected to be much more metallic. Lastly, Bi is the heaviest stable element ( $Z = 83$ ) and the relativistic effects on electronic properties in  $\text{KBi}_2$ ,

RbBi<sub>2</sub>, and CsBi<sub>2</sub> are the strongest of all of the Laves superconductors, even when compared with Ir- and Au-based systems, such as (La/Lu)Ir<sub>2</sub><sup>73</sup> and (Pb,Bi)Au<sub>2</sub>,<sup>74</sup> since the SOC effect on 5d valence electrons is weaker than that on the 6p shell.

## CONCLUSIONS

We have analyzed the electronic and vibrational properties of two Bi-based cubic Laves phases: RbBi<sub>2</sub> and CsBi<sub>2</sub>. Our results show that the occurrence of superconductivity in these two compounds and an isostructural KBi<sub>2</sub> stems almost exclusively from the heavy element pyrochlore lattice. Both the stability of the phases and their electronic and vibrational properties are heavily affected by relativistic effects. The spin-orbit coupling is crucial for the dynamic stability of CsBi<sub>2</sub>, and to a lesser extent RbBi<sub>2</sub>. The stability enhancement can be explained by considering an isolated Bi<sub>4</sub> cluster and the effects of SOC on its electronic structure. We postulate that crystal structures based on relativistically stabilized hypervalent networks of heavy elements are interesting candidates for finding new superconductors.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.jpcc.3c02176>.

PXRD patterns for RbBi<sub>2</sub> and CsBi<sub>2</sub> samples; crystal unit cell parameters for RbBi<sub>2</sub> and CsBi<sub>2</sub>; plot of critical field versus temperature; low-temperature heat capacity of RbBi<sub>2</sub> and CsBi<sub>2</sub>; crystal orbital Hamilton population (COHP) plot for RbBi<sub>2</sub>; and electronic band structure, charge density, and phonon dispersion plots for elemental Bi (PDF)

Chiral phonon animation (MP4)

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The manuscript was written through contributions of all authors.

## Notes

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## ABBREVIATIONS

COHP, crystal orbital Hamilton population; DKH2, Douglas–Kroll–Hess—second-order Douglas–Kroll–Hess relativistic correction; DOS, density of states; EPC, electron–phonon coupling; GGA, generalized gradient approximation; PBE, Perdew–Burke–Ernzerhof exchange–correlation potential; PXRD, powder X-ray diffraction; QE, Quantum Espresso package; SOC, spin–orbit coupling

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