



Vilnius Gediminas Technical University



Lithuanian Academy of Sciences

ISSN 1392-3730

Journal of Civil Engineering --- and Management ---

2004, Vol X, No 2

Vilnius „Technika“ 2004

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APPLICATION OF SUPERELEMENTS IN STATIC ANALYSIS OF THIN-WALLED STRUCTURES

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Received 16 Dec 2003; accepted 15 March 2004

Abstract. A concept of a beam superelement is suggested as a new tool in the static analysis of structures made of thin-walled members. This proposal seems to be especially attractive for treating the problems where the existing one-dimensional models do not provide proper solutions. This class of problems includes, for instance, the torsion of thin-walled beams with battens and the determination of the bimoment distribution at the nodes of frames made of thin-walled members. The entire segment of the thin-walled beam with warping stiffener or the whole node of the frame is modelled with shell elements. The stiffness matrix of such thin-walled beam superelement can be estimated according to the standard procedure of the enforced unit displacements. The accuracy of the proposed one-dimensional model has proved to be comparable to that offered by the detailed FEM model where the whole structure is represented by a very large number of shell elements.

Keywords: thin-walled structures, beams, frames, stiffeners, static analysis.

1. Introduction

Beams and frames assembled of thin-walled members are very often used in civil engineering structures and in various machines and vehicles. The proper methods of mathematical modelling of these structures are of great importance for simulations of their behaviour. Every real structure of this type is subjected to loads that produce torsion in its members. However, due to presence of warping in beam elements, it is necessary to solve the problem of bimoment distribution in the frame nodes. In the literature and engineering practice there are various concepts of establishing the bimoments distribution [1–2], but none of them gives the general solution to this problem. The scope of this paper is limited to the beams and frames composed of thin-walled members with the bisymmetrical open cross-section. Unfortunately, the members of this kind have a small torsional stiffness and sometimes to increase it additional stiffeners like battens, transverse plates or cross trusses are necessary [3]. Similarly, as in the case of the frame node, a deformation of the member cross-section in vicinity of the stiffener location is observed.

In the present research we propose to model the structure using one-dimensional finite elements as follows:

- a) in the region between nodes or stiffeners we use thin-walled elements [4] based on the classical as-

sumptions of the theory of thin-walled beams of non-deformable cross-section [5];

- b) in the region of nodes and stiffeners we apply superelements composed of flat shell elements. The stiffness matrix for the superelement is determined using the method of unit displacements [6] with the help of the FEM computer system MSC/NASTRAN [7], by treating the nodal zone as a complex system of plates divided into a large number of QUAD4 shell elements.

A numerical model of the analysed structure consisted of an appropriate assembly of beam elements and superelements. All calculations following the standard FEM procedures are carried out by a computer program for matrix operations, PRISM [8].

The algorithm described above has been applied to analyse several problems for beams and frames made of thin-walled members [9]. The obtained results have been positively verified with the detailed FEM model, in which the whole structure is represented as an assemblage of flat shell finite elements (MSC/NASTRAN QUAD4 shell elements). In the following two selected examples are described in detail; they are the torsion analysis of a simply supported thin-walled beam and the steel frame under transverse force.



2. Torsion of thin-walled beams with warping stiffeners

2.1. Concept of superelement

Thin-walled beams with open cross-section can be very efficiently analysed numerically with the use of one-dimensional beam model [4] based on the classical theory of thin-walled bars with non-deformable cross-section [5]. The main idea of the proposed concept is to construct an analogous one-dimensional model for a thin-walled beam segment containing warping stiffeners. The whole segment is represented as one big superelement – an assemblage of shell type finite elements QUAD4 available in the system MSC/NASTRAN (Fig 1a¹). A proper representation of beam boundary conditions in the detailed model is obtained using the technique of rigid elements. The stiffness matrix of the 2-node beam-like element is calculated according to the common procedure of the unit enforced displacements where the resultant 14 reaction forces (shown in Fig 1b) for each enforced unit displacement form the corresponding column of the stiffness matrix.

After positive verification in the analysis of I-beams without any stiffeners [5, 9] the proposed procedure has been applied for I-beams with warping stiffeners.

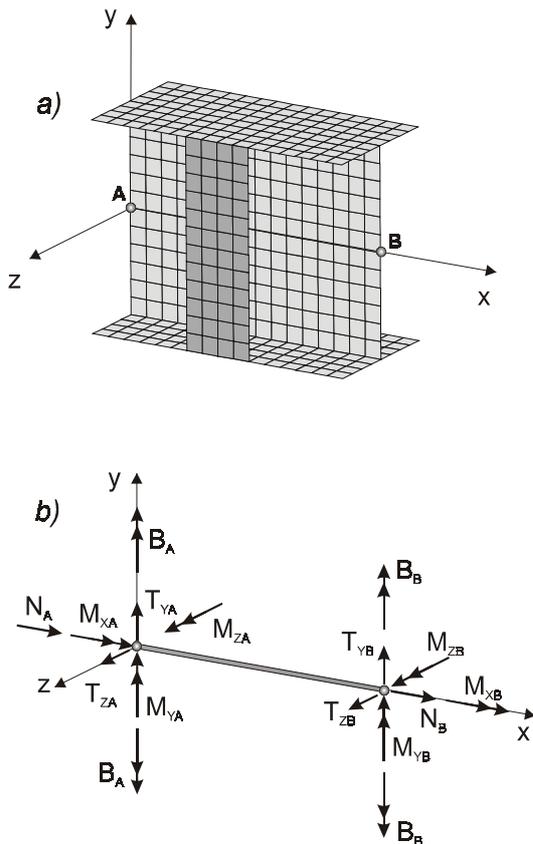


Fig 1. Thin-walled beam superelement: a) 3-D segment b) 1-D element with 14 degrees of freedom

¹ The FE mesh used in computations was much more dense than that shown in Fig 1.

2.2. Torsion of a simply supported I-beam

2.2.1. I-beam without warping stiffeners

First the I-beam without any warping stiffeners is considered. The analysed I-beam is built out of 10 mm thick steel panels ($E = 205 \text{ GPa}$, $J = 0,3$) with the height of the web equal 30 cm and flanges 20 cm wide. A simply supported beam is subjected to the torque of 1 kNm as shown in Fig 2.

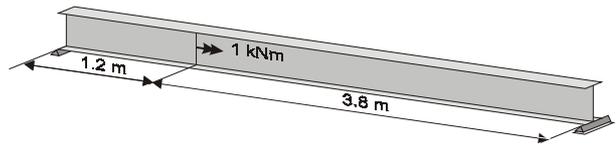


Fig 2. Simply supported I-beam undergoing torsion

The analytical one-dimensional model of the I-beam consists of seven standard I-beam elements [4]. Due to the loading conditions the number of degrees of freedom in the present analysis can be reduced to 2 DOFs per each nodal point. The second one-dimensional model has been constructed of seven superelements ($3 \times 0,6 \text{ m} + 4 \times 0,8 \text{ m}$). All calculations for both one-dimensional models have been carried out with the computer program for matrix operations, PRISM [8]. To provide a reference solution for the analysed problem a detailed FEM model has been applied where the whole beam has been represented as the assemblage of over twenty two thousand QUAD4 shell elements of the system MSC/NASTRAN. The graphs of the torsion angle, bimoment and the warping distribution obtained with both those models are given in Fig 3, 4 and 5, respectively.

In all graphs presented in Figs 3 to 5 a very good agreement can be observed between the results of the analytical model and those obtained with superelements. Solutions from both the one-dimensional models have been confirmed additionally by the detailed FEM model. The positive response achieved in this comparative test forms a good foundation for the applying the concept of

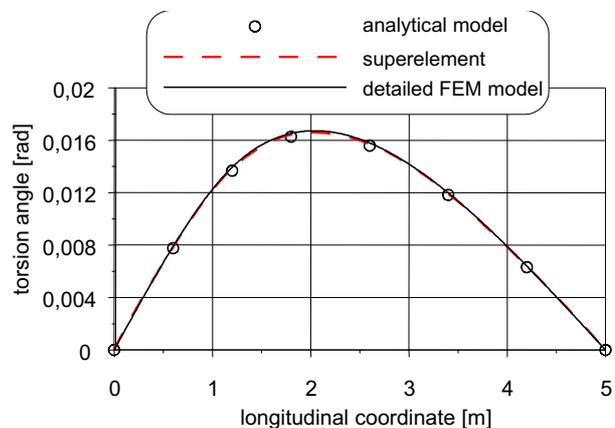


Fig 3. Torsion angle for I-beam without stiffeners

the superelement in the analysis of the I-beam with different warping stiffeners added at the loaded cross-section. In the following calculations the superelements are used to model only the thin-walled beam segments containing stiffeners, assuming that the remaining part of the thin-walled beam can be effectively represented by the one-dimensional beam element [4].

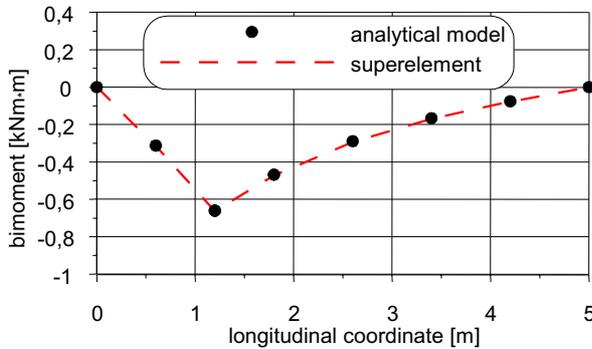


Fig. 4. Bimoment distribution for I-beam without stiffeners

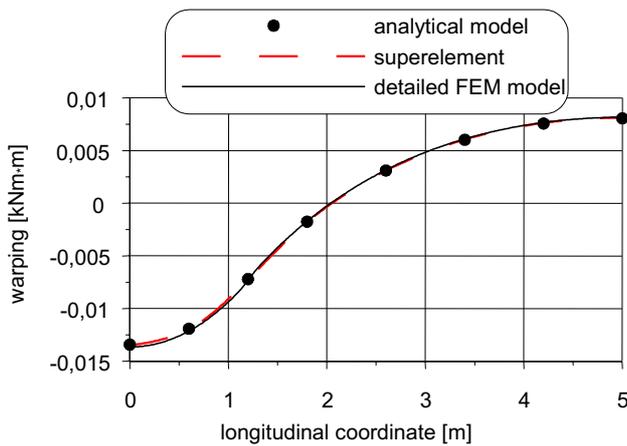


Fig. 5. Warping for I-beam without warping stiffeners

2.2.2. I-beam with lateral diaphragms

The first type of the warping stiffener considered here are lateral diaphragms located in the cross-section at $x = 1,2$ m where the torque is applied. The lateral diaphragms are constructed as two steel panels 10 mm thick located on both sides of the web of the I-beam. The analysed simply supported I-beam with lateral diaphragm is shown in Fig 6.

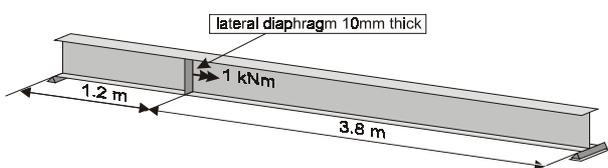


Fig. 6. A simply supported I-beam with lateral diaphragm

The analytical, one-dimensional model of the I-beam with the lateral diaphragm consists of seven standard I-beam elements [4] accompanied by the warping spring with the stiffness estimated according to the formula:

$$k_B = \frac{Gt^3 bh}{3}, \tag{1}$$

where t is the thickness of the diaphragm, b stands for the its width and h for the height with G being the shear modulus.

The second one-dimensional model of the analysed beam is constructed of five standard I-beam elements [4] and one superelement 40 cm long. Here again the detailed FEM model is applied to provide an additional reference solution.

The results obtained with those three models are illustrated by the graphs of the torsion angle, the bimoment and the warping given in Figs 7 to 9.

Examining the presented graphs one can notice a very good agreement of the results obtained with the three models used in the calculations. The analytical formula given in (1) seems to be a good estimation of the warping spring stiffness for the lateral diaphragms. On the other hand, comparing the graphs given in Fig 3 and in Fig 7, someone can notice that the torsion stiffness of the I-beam does not increase significantly after the lateral diaphragm is appended.

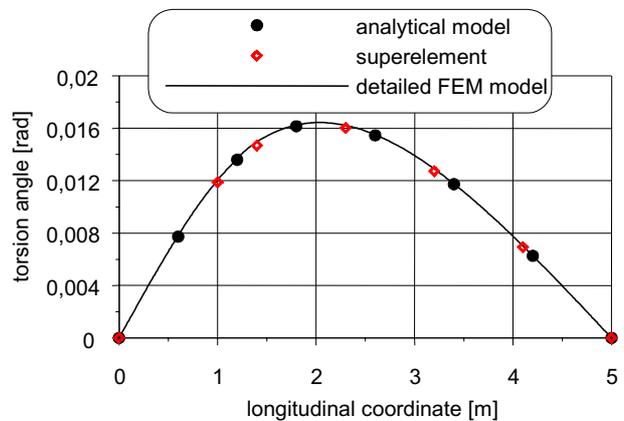


Fig. 7. Torsion angle for I-beam with lateral diaphragm

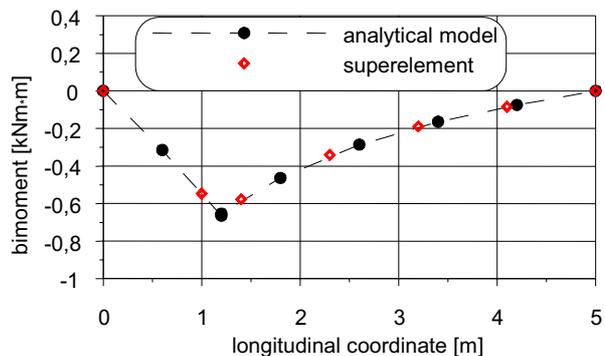


Fig. 8. Bimoment for I-beam with lateral diaphragm

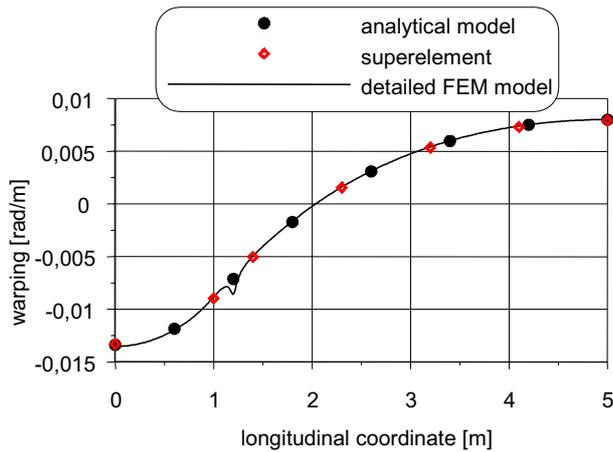


Fig 9. Warping for I-beam with lateral diaphragm

The value of the warping in the detailed FEM model has been calculated as the derivative of the torsion angle taken with the respect to the longitudinal coordinate. A numerical evaluation of the derivative has been performed by the central difference method. A visible disturbance can be observed in the distribution of the derivative of the torsion angle within the region of the diaphragms. Both one-dimensional models give more regular solutions.

2.2.3. I-beam with battens

In the second example of the I-beam with the warping stiffeners, the battens have been added in the cross-section loaded with the torque. The battens are constructed as two steel panels parallel to the web of the I-beam and located on both its sides. The thickness of battens is equal to 10 mm. The analysed I-beam with battens is shown in Fig 10.

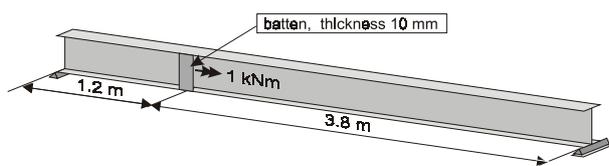


Fig. 10. Simply supported I-beam with battens

The same three models as described in 2.2.2 have been applied in the current analysis with the only difference that the stiffness of the warping spring representing the battens is estimated according to the formula

$$k_B = \frac{Eb_b^3b_1^2t}{2h} \frac{1}{1+1.2\frac{E}{G}\left(\frac{b_b}{h}\right)^2} \quad (2)$$

with h , t and b_b standing for the height, the thickness and the width of the batten, respectively, E being the Young modulus, and b_1 representing the distance between the battens in the beam cross-section.

The graphs of the torsion angle, the bimoment and the warping obtained for the I-beam with the battens are presented in the Figs 11 to 13, respectively.

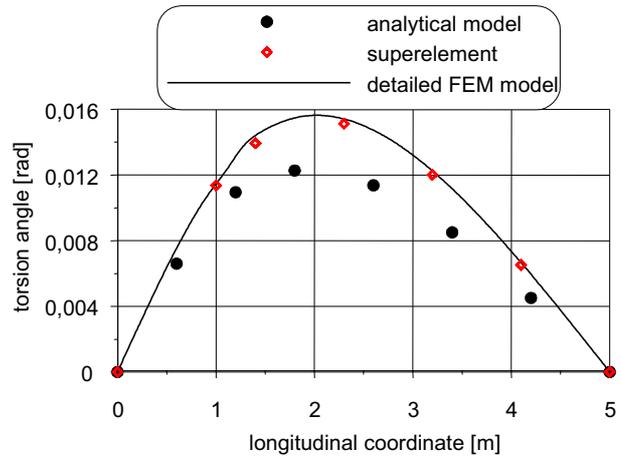


Fig 11. Torsion angle for I-beam with battens

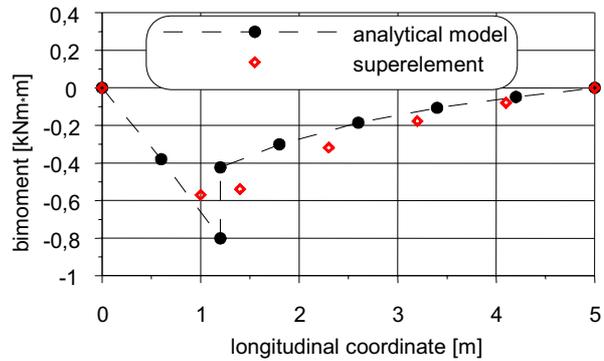


Fig 12. Bimoment for I-beam with battens

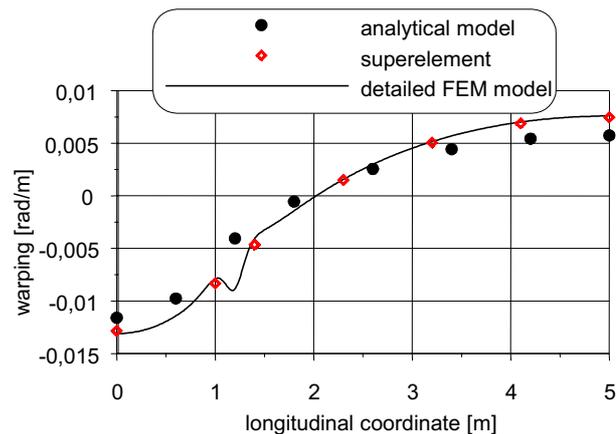


Fig 13. Warping for I-beam with battens

The graphs presented in Fig 10 show that the application of the superelement allows for a very accurate prediction of the torsion angle of the beam as compared with the results obtained with the detailed FEM model. On the other hand, the analytical model utilising the

warping spring is noticeably stiffer. Since the analytical model performed quite well for the I-beam without battens, it is obvious that the spring stiffness is a critical issue of that approach. Relatively big jump in the graph of the bimoment (Fig 12) obtained from the analytical model confirms an opinion that the stiffness of the warping spring is overestimated.

2.2.4. I-beam with box stiffeners

The last warping stiffener considered in this example is constructed as a closed box made of steel panels 10 mm thick. The analysed simply supported I-beam with box stiffeners is presented in Fig 14.

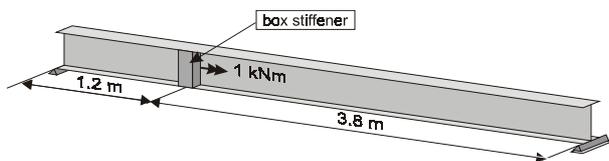


Fig 14. Simply supported I-beam with box stiffeners

In the literature one can find the following suitable formula for the stiffness of the warping spring representing the box stiffener

$$k_B = \frac{2G b_b t b h}{b + b_b} \tag{3}$$

with b_b standing for the width of the panel parallel to the web.

The same 3 models, as in the previous examples, have been applied here to obtain the graphs of the torsion angle, the bimoment and the warping for the I-beam with the box stiffeners presented in the Figs 15 to 17, respectively.

Looking at the graph of torsion angle presented in Fig 15 one can notice that the box stiffener provides much larger increase of the torsional stiffness of the I-beam than any one of the stiffeners considered before.

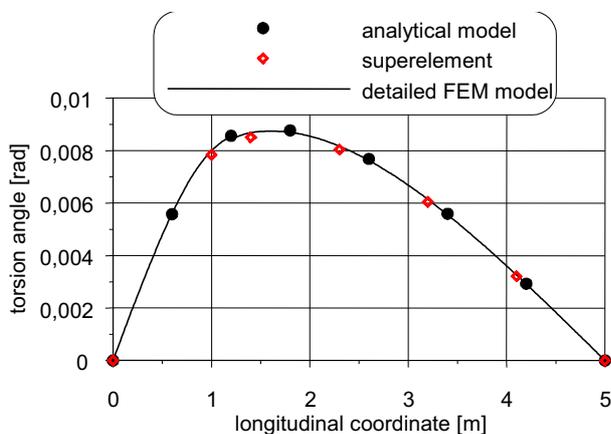


Fig 15. Torsion angle for I-beam with box stiffeners

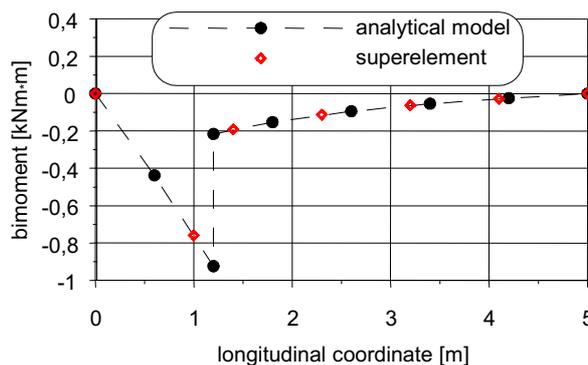


Fig 16. Bimoment for I-beam box stiffeners

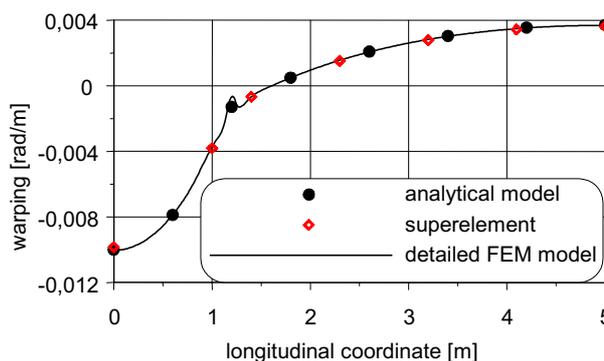


Fig 17. Warping for I-beam with box stiffeners

Since all three models applied in the analysis give similar responses it seems that the stiffness of the warping spring representing the box stiffener can be correctly established by using the formula (3). An additional support for that conclusion can be observed in Fig 16 where the bimoment distribution obtained by the analytical model is in an excellent agreement with the results of the calculations performed with the superelement approach.

Summarising the conclusions for the presented example, it can be stated that the analytical model utilizing the concept of the warping spring gives a correct solution for the pure torsion analysis of the thin-walled beam with lateral diaphragms or with box stiffeners. However, this approach does not provide a right response for the case of the battens. On the other hand, a correct solution can be obtained for any one of the considered stiffeners when the concept of the superelements is applied.

It should be emphasised that the effect of the warping stiffeners depends very much on their location. One can imagine that for the analysed beam the application of warping stiffeners at the supports would significantly increase this effect.

3. Thin-walled frames

Thin-walled frames are common steel constructions in various civil engineering objects, like industrial or shopping halls, island station roofs or high buildings.

Such constructions consist of many beams, columns, lateral or wind bracings connected in nodes. Warping of the member cross-section plays a significant role in stress and deformation distribution. It depends on the frame node construction or the stiffeners located along the beam span.

Presented considerations are restricted to the plane frames. The superelement technique is applied in the modelling of the warping effects in frame nodes and thin-walled bar elements with stiffeners, where the non-deformable cross-section assumption of the classic thin-walled theory is not fulfilled.

3.1. Node superelement

Nodes of thin-walled frames are the most significant elements, where the thin-walled beams are connected at different angles. In this case, within one dimensional classic beam theory, it is impossible to determine the warping distribution and bimoments as internal forces. There are no equilibrium conditions of bimoments in nodes and occurrence of significant deformations of cross section is noted, which is in inconsistency with the assumptions of the thin-walled beam theory – non-deformable cross-section. Also the node construction plays an important role in the warping distribution phenomena. The node superelement is thus a suitable model to take all the effects mentioned into account.

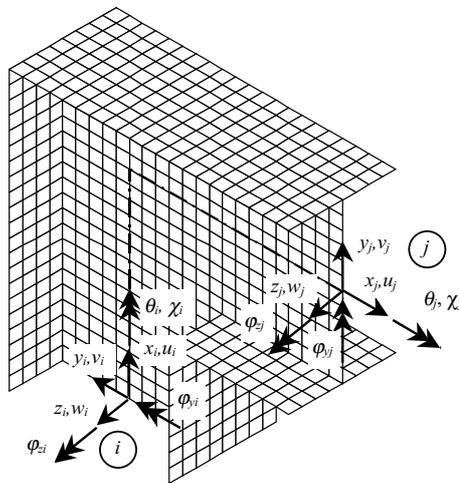


Fig 18. Node superelement, 14 degrees of freedom

The stiffness matrix of the thin-walled node superelement has been calculated according to the common procedure of the unit enforced displacements where the resultant 14 reaction forces (shown in Fig 18) for each enforced unit displacement form the corresponding column of the stiffness matrix. Herein the axial stretching, bending and shearing behaviour of the thin-walled superelement node is coupled with torsional performance.

MSC/NASTRAN for Windows [7] FEM system containing QUAD4 shell elements has been employed in the study of the detailed node superelement model. Four-

teen unit enforced stages have been analysed to obtain 144 stiffness matrix coefficients. Many of them are approached to zero – depending on the nodal force coupling. The 4-node shell elements QUAD4 available in that system have been used to model the entire segment of the thin-walled node.

3.2. Comparative analysis for two-member frame

Let us consider a simple two member frame built of I-beams shown schematically in Fig 19. The frame is subjected to the torque $M = 1$ kNm acting at the midspan of the horizontal beam. There are not stiffeners in the frame.

The numerical static analysis of the frame is carried out using three different models:

- 1) classic beam theory model, where the frame is modelled by standard beam elements with 12 degrees of freedom (6 DOFs per each node), the warping effect is neglected;
- 2) thin-walled beam model [4] based on the classical theory of thin-walled bars with non-deformable cross-section [5] combined with the node superelement described in 3.1. Both element types have 14 degrees of freedom and take into account the warping effects.
- 3) detailed FEM model, where the whole frame is modelled as an assembly of QUAD4 shell elements (Fig 20) available in MSC/NASTRAN. The four-node QUAD4 shell elements have 24 degrees of freedom.

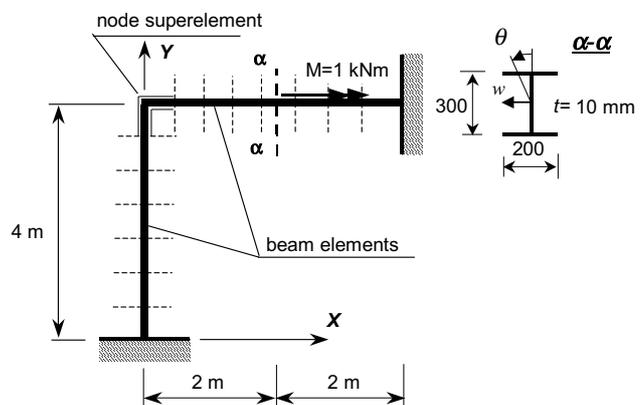


Fig 19. Frame modelled by thin-walled elements with node superelement

In Figs 21 and 22 the distribution of torsion angle along the column and along the horizontal beam obtained with the aid of the models under consideration is shown. The solution of the three-dimensional frame model discretised by shell elements is assumed to be more adequate to the real construction and has been treated as a reference model. The classic beam theory model gives a solution quite different from those of the shell model. The model consisting of the thin-walled beam elements

together with the node superelement provides a solution very close to the comparative shell model. A serious discrepancy between the classic beam theory solution and the results corresponding to more accurate models is observed, especially in the horizontal member.

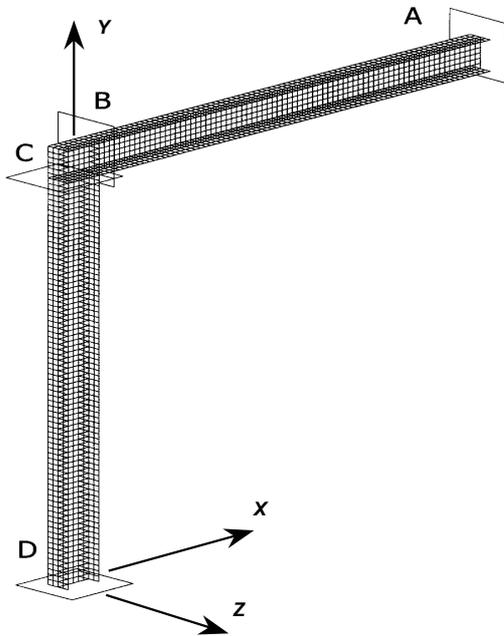


Fig 20. Detailed FEM model, QUAD4 shell elements of MSC/NASTRAN

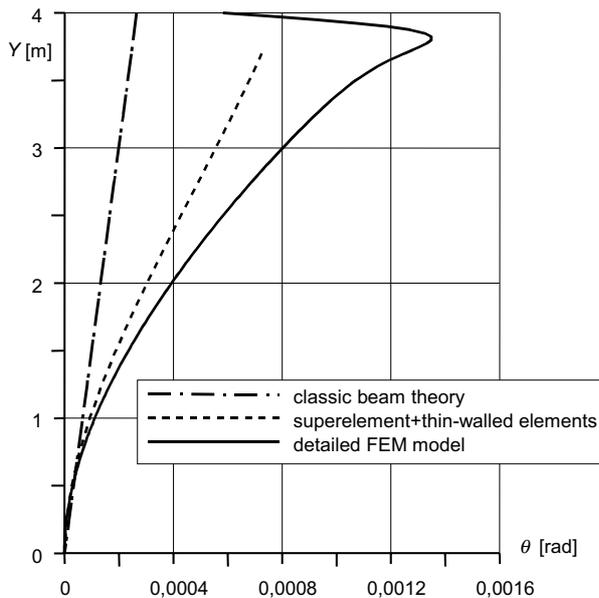


Fig 21. Distribution of torsion angle θ along the frame column

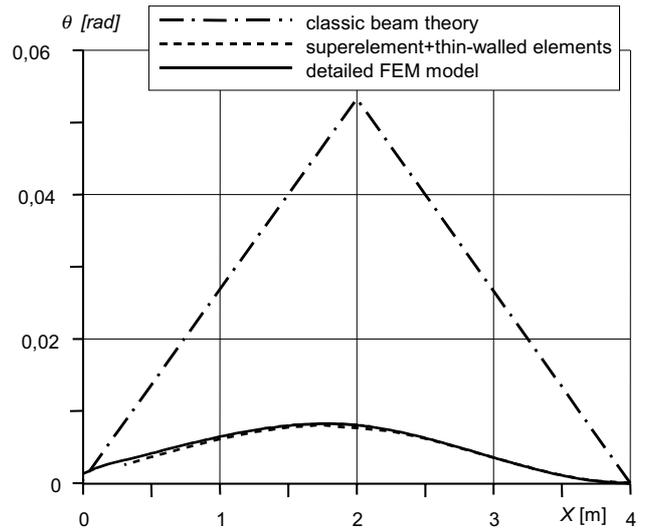


Fig 22. Distribution of torsion angle θ along the horizontal beam

3.3. Plane frame with battens

Warping stiffeners are very often used in thin-walled frames to increase the frame stiffness for torsion. Let us consider a plane frame with three double battens placed along the horizontal beam as presented in Fig 23.

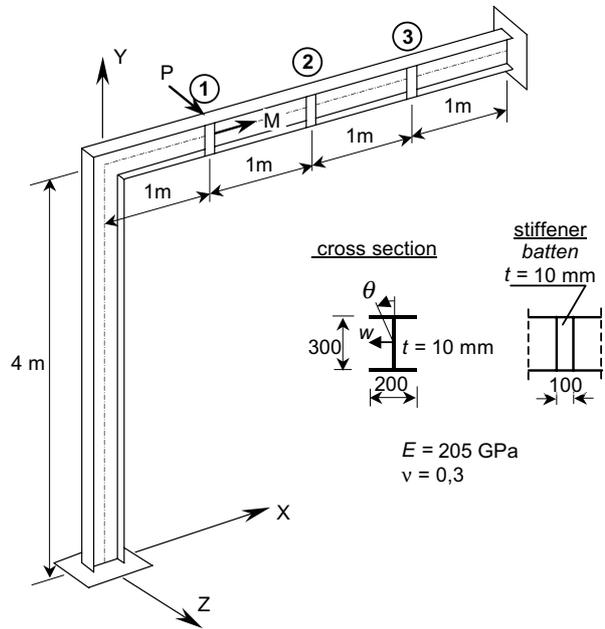


Fig 23. Thin-walled frame with battens

The node and the batten superelements have been implemented using a one-dimensional model shown in Fig 24. Each of the FEM elements used in this model has 14 degrees of freedom: three translations, three rotations and warping at each element node.



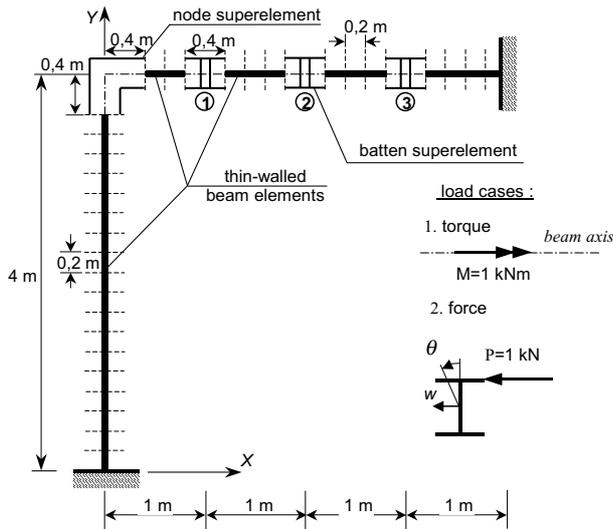


Fig 24. One-dimensional FEM model, frame with node and batten superelements

The results one-dimensional frame model is compared with a detailed FEM model (MSC/NASTRAN, QUAD4 shell elements) where the non-deformable cross section condition is not enforced.

Two load cases are considered:

- 1) torque $M=1$ kNm applied sequentially at points 1, 2 and 3;
- 2) transverse horizontal force $P=1$ kN applied to the upper flange at the point 1.

Both load cases are graphically presented in Figs 23 and 24.

The distribution of the torsion angle θ along the horizontal beam for load case 1 is presented in Figs 25 to 27. The influence of battens responsible for increasing the frame beam torsion stiffness is visualised by reducing the torsion angle θ . The static analysis solutions of the one-dimension frame model with superelements are very close to the results obtained for the shell model.

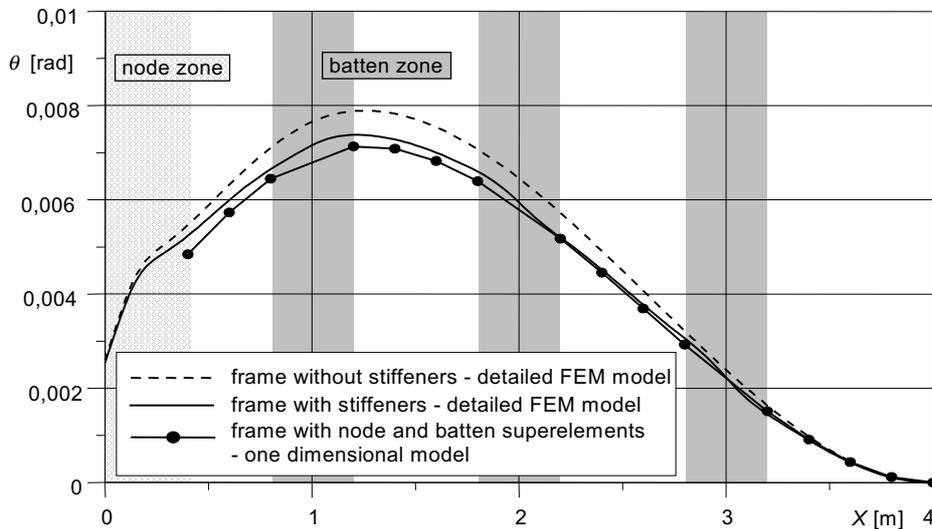


Fig 25. Torsion angle θ distribution along the horizontal beam, load case 1, unit torque $M=1$ kNm acting at point 1

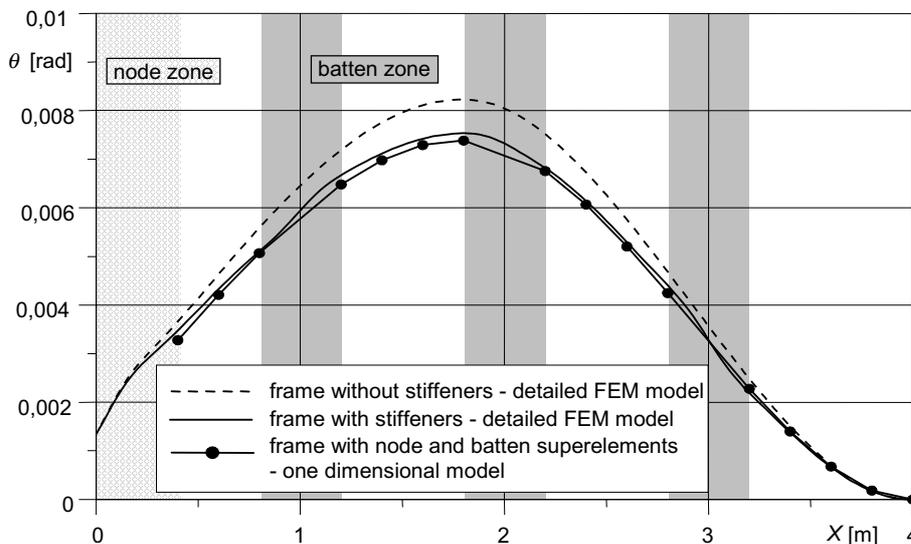


Fig 26. Torsion angle θ distribution along the horizontal beam, load case 1, unit torque $M=1$ kNm acting on point 2

The results for the second load case (transverse horizontal force $P = 1\text{ kN}$ applied at point 1) are presented in the Figs 28 and 29. Here, again, a quite good agreement can be observed between the results of the one-dimensional model with superelements and the detailed FEM model utilising shell elements.

4. Conclusions

The one-dimensional thin-walled beam 2-node element proposed by Barsoum & Gallagher [4] proved to be an efficient tool for the numerical analysis of thin-walled beams. The formulation of this element is based on the classical theory of thin-walled bars with non-deformable cross-section [5]. The warping of the thin-walled beam is included as the seventh degree of freedom at each nodal point, whereas the remaining six DOFs are usual 3 translations and 3 rotations common for the most

space frame formulations. The results calculated with this element are in very good agreement with the reference solutions obtained by means of the detailed FE model where the thin-walled beams were modelled as assemblages of shell elements.

One should notice that the classical theory of thin-walled bars with non-deformable cross-section [5] is not appropriate for modelling the behaviour of the thin-walled beams with warping stiffeners, especially with battens. Due to the specific formulation of the warping DOF, which is defined in the local coordinate system of the beam, considerable problems appear also when the thin-walled beam elements are applied in the analysis of frames built out of thin-walled members. In both cases the one-dimensional model of the thin-walled beam can be effectively upgraded by employing the concept of superelements proposed by the authors of the paper.

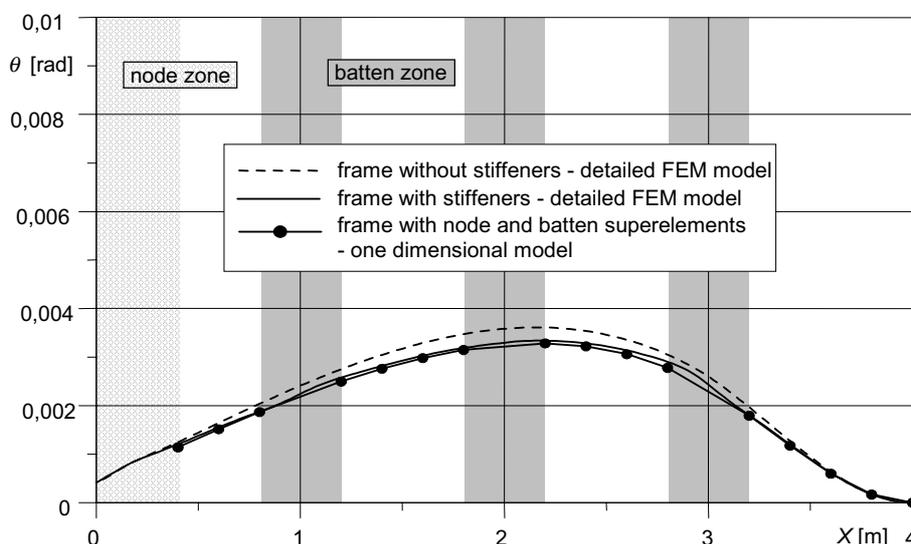


Fig 27. Torsion angle θ distribution along the horizontal beam, load case 1, unit torque $M = 1\text{ kNm}$ acting on point 3

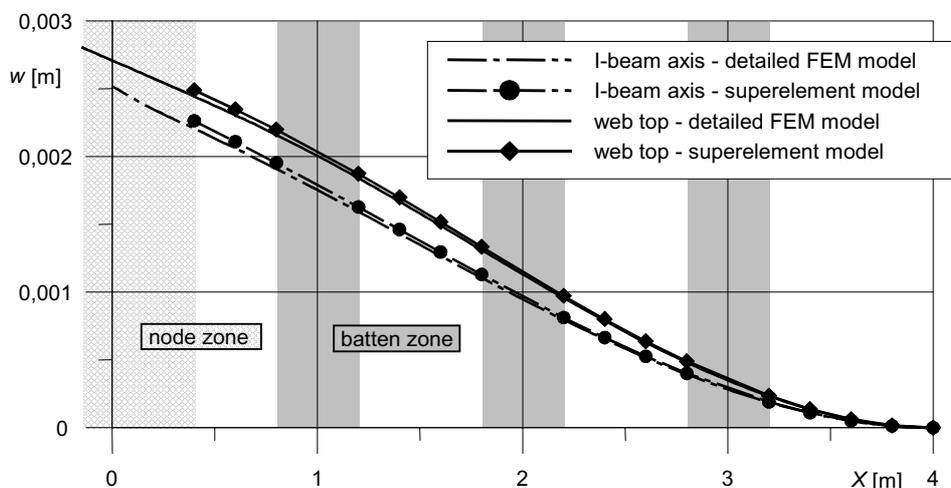


Fig 28. Distribution of displacement w along the horizontal beam, unit force $P=1\text{ kN}$ perpendicular to the frame plane applied at point 1 of the web and the top flange joint

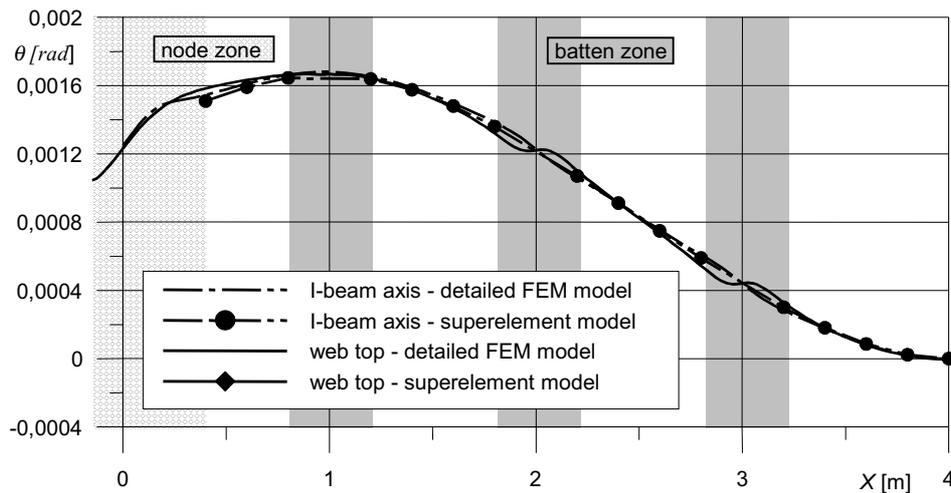


Fig 29. Distribution of torsion angle θ along the horizontal beam, unit force $P=1\text{kN}$ perpendicular to the frame plane applied at point 1 of the web and the top flange joint

The presented numerical examples have shown that the one-dimensional beam and frame models utilising the concept of the superelement for the segments containing warping stiffeners and for frame nodes offers the accuracy which is comparable to that of the detailed FEM model, with an additional remark that the numerical size of the former is just a fraction of the size of the latter.

Although the superelement offers an equivalent precision in the thin-walled beams analysis as the mentioned above element of Barsoum & Gallagher [4], they are not recommended in the analysis of straight thin-walled beams without any stiffeners – one should remember that the stiffness matrix of the B&S thin-walled beam element is given in explicit form [4] whereas a rather complex FEM analysis is required to establish the stiffness matrix of the superelement.

The positive results of the numerical studies carried out by the authors proved that frames constructed of thin-walled members can be very effectively analysed with the combined one-dimensional model where the superelements are applied only to model frame nodes or beam segments containing stiffeners with the remaining part of the structure represented by the one-dimensional beam element [4]. The approach recommended in the present paper has been successfully applied also in the sensitivity analysis of thin-walled structures [9, 10].

Acknowledgements

The financial support of the State Committee for Scientific Research (KBN, Poland) under Grant No 7 T07E 01519 is gratefully acknowledged.

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SANTRAUKOS

J. Hildebrand, F. Werner. Virintinių jungčių tarp stipriųjų smulkiagrūdžių plienų ir statybinių plienų būklės kaita // Journal of Civil Engineering and Management. Vilnius: Technika, 2004, t. X, Nr. 2, p. 87–95.

Apžvelgtas smulkiagrūdžių statybinių plienų gamybos procesas. Šiluminio skaičiavimo, kuris yra ir suvirinimo modeliavimo dalis, rezultatai palyginti su matavimų duomenimis ir gautas geras jų atitikimas. Analizuojant kietumo kreivę buvo rastas nedidelis kietumo pasikeitimas, vadinamasis vietinis kietumo sumažėjimas. To priežastis – sandaros transformacija, sukelta šiluminių veiksnių. Turimos TTA (laiko-temperatūros-austenito) ir TTT (laiko-temperatūros-transformacijų) diagramos neatspindi šio grūdinimo proceso, kuris turi įtakos struktūrinio grūdinimo per mikrostruktūros dedamąsias – martensitą ir bainitą – sąlygai. Sprendimo metodas taikytas blogai derančios jungties pavyzdžiui. Gautas geras rezultatų sutapimas.

Raktažodžiai: skaitmeninis modeliavimas, stiprieji smulkiagrūdžiai plienai, metalo suvirinimas aktyviomis dujomis, šiluminis laukas, kietumas, grūdinimas, vietinis kietumo sumažėjimas.

R. Karkauskas. Tampriai plastiškų geometriškai netiesinių santvarų optimizacija, įvertinant standumo ir stabilumo apribojimus // Journal of Civil Engineering and Management. Vilnius: Technika, 2004, t. X, Nr. 2, p. 97–106.

Santvaros tipo lengvosios konstrukcijos optimalus projektas turi atitikti stiprumo, standumo ir stabilumo sąlygas ir būti ne tik saugus išorinių poveikių atžvilgiu, bet ir tenkinti optimalumo kriterijų, išreiškiantį tam tikrus ekonominius reikalavimus. Čia susiduriame su optimizavimo uždavinio skaitmeninės realizacijos sunkumais, kai minėtas sąlygas sujungiamo į bendrą uždavinio formuluotę. Pasiūlyta originali optimizavimo uždavinio 3 pakopų realizavimo metodika, kuri leidžia išvengti sunkumų sprendžiant uždavinį vienu etapu. Kiekvieno optimizavimo ciklo metu išrašos, nustatytos prieš tai vykusio optimizavimo ciklo tampriai plastinės netiesinės analizės metu, yra naudojamos naujiems optimaliems projektuojamiems parametrams nustatyti. Tamprumo netiesinei analizei taikomas tangentinis standumo metodas. Tamprumo ir plastiškumo analizė atliekama taikant papildomos energijos ekstremumų principą. Laikoma, kad optimizacijos proceso metu konstrukcijos tempimų strypų kritiniai įtempiai yra proporcingi takumo ribos įtempiams. Gniuždomieji strypai gali būti apkrauti iki kritinių įtempių, kurių dydžiai nustatomi įvertinant strypų klupdymą. Konstrukcijos standumas yra ribojamas jos mazgų poslinkiais. Pateikti skaitiniai eksperimentai.

Raktažodžiai: optimizacija, tampriai plastinė sistema, standumo ir stabilumo sąlygos, geometrinis netiesiškumas, tangentinis standumas, baigtinių elementų diskretinis modelis.

R. Kliukas, A. Kudzys. Esamų statybinių elementų tikimybinio ilgalaikiškumo prognozavimas // Journal of Civil Engineering and Management. Vilnius: Technika, 2004, t. X, Nr. 2, p. 107–112.

Nagrinėjama eksploatacinio ir bandymo poveikių įtaka esamų atitvarinių ir laikančiųjų konstrukcijų komponentų ir elementų tikimybiniam patikimumui (tinkamumui, saugai ir ilgalaikiškumui). Pateikti modeliai, kurie laikui bėgant kinta, ilgalaikiais kintamaisiais ir cikliniais poveikiais deformuojamų medžiagų, komponentų ir elementų patikimumui vertinti. Aptariami eksploataciniais nuolatiniais ir kintamaisiais poveikiais deformuojamų esamų medžiagų, komponentų ir elementų tiksliniam patikimumo indeksams. Siūloma atsižvelgti į nematomų defektų įtaką medžiagų, komponentų ir elementų ilgalaikio patikimumo indeksams. Atsižvelgiama į nematomų defektų ir medžiagų bei elementų atspario nupjautinio tikimybės skirstinio įtaką patikimumo indeksų vertinimui. Analizuojami metodologiniai statybinių komponentų ilgalaikiškumo prognozavimo ypatumai ir nepagrįsti nelaiku atlikti remontai bei keitimai. Blogėjančio apsauginio betono sluoksnio tikimybinio patikimumo prognozavimas iliustruoja pateikto metodo taikomąją vertę.

Raktažodžiai: statybiniai elementai, patikimumas, ilgalaikiškumas, eksploatacinė bandymo apkrova, apsauginis sluoksnis.

I. Kreja, T. Mikulski, C. Szymczak. Superelementų taikymas plonasienių konstrukcijų analizėje // Journal of Civil Engineering and Management. Vilnius: Technika, 2004, t. X, Nr. 2, p. 113–122.

Pasiūlyta sijos modeliavimo superelementais koncepcija. Tai nauja priemonė analizuojant konstrukcijas, sudarytas iš plonasienių elementų. Pasiūlytas algoritmas ypač tinka sprendžiant uždavinius, kai vienmačių konstrukcijų modelių taikymas neužtikrina teisingų sprendinių gavimo. Tokie uždavinių klasei priklauso plonasienių sijų su juostomis sukimo uždavinys bei dviejų krypčių momentų pasiskirstymo iš plonasienių elementų, sudarytų rėmų mazguose, radimo uždavinys. Plonasienė sija su standumo briauna arba rėmo mazgas modeliuojami kevaliniais elementais. Tokios plonasienės sijos standumo matrica gali būti sudaryta naudojant vienetinių poslinkių standartines procedūras. Pasiūlyto vienmačio modelio tikslumas parodė, kad jis yra konkurencingas, palyginti su detalioju baigtinių elementų metodu, tuo atveju, kai visai konstrukcijai modeliuoti taikomas labai didelis kevalinių elementų skaičius.

Raktažodžiai: plonasienės konstrukcijos, sijos, rėmai, standumo briaunos, statinė analizė.

I. Povilaitienė, A. Laurinavičius. Išorinio bėgio dilimo mažinimas kreivėse // Journal of Civil Engineering and Management. Vilnius: Technika, 2004, t. X, Nr. 2, p. 123–130.

Geležinkelio linijų kreivės riboja traukinių važiavimo greičius, be to, jose yra didelis išorinio bėgio galvutės šoninio dilimo intensyvumas. Aptariamos išorinio bėgio pakylės pagrindinės funkcijos. Pateikti eksperimentinių tyrimų, kurie buvo atlikti siekiant nustatyti išorinio bėgio pakylės dydžio ir vėžės pločio paplatinimo kreivėse įtaką bėgio galvutės

РЕФЕРАТЫ

Е. Гильдебранд, Ф. Вернер. Изменение состояния сварных соединений между высокопрочными мелкозернистыми строительными сталями // Journal of Civil Engineering and Management. Вильнюс: Техника, 2004, X т., № 2, с. 87–95

Рассмотрен процесс изготовления мелкозернистых строительных сталей. Результаты теплового расчета, который является также частью моделирования сварки, сопоставлены с измерениями. Достигнуто хорошее соответствие. На основании анализа кривых твердости замечено небольшое изменение в твердости, так называемое местное уменьшение твердости. Причиной этого является трансформация структуры, вызванная тепловыми факторами. Имеющиеся диаграммы ТТА (время-температура-аустенит) и ТТТ (время-температура-трансформации) не отражают процесса закалывания, который влияет на условие структурного закалывания через составляющие микроструктуры – мартенсит и байнит. Метод решения в качестве примера применен в отношении плохо согласующегося соединения. Получено хорошее соответствие результатов.

Ключевые слова: числовое моделирование, высокопрочные мелкозернистые стали, сварка металла в активированном газе, тепловое поле, твердость, закалка, местное уменьшение твердости.

Р. Каркаукас. Оптимизация упругопластических геометрически нелинейных ферм при ограничениях на жесткость и устойчивость // Journal of Civil Engineering and Management. Вильнюс: Техника, 2004, X т., № 2, с. 97–106.

Оптимальный проект легкой конструкции типа ферм должен отвечать не только требованиям прочности, жесткости и устойчивости, но и быть безопасным относительно внешних воздействий и удовлетворять критерию оптимальности, описывающему конкретные экономические цели. В данной ситуации и возникают трудности, связанные с численной реализацией задач оптимизации, объединяющих вышеупомянутые требования в единое целое. Предложена оригинальная трехступенчатая методика задачи оптимизации, позволяющая преодолеть трудности связанные с решением задачи в один этап. На каждом цикле оптимизации используются усилия предыдущего цикла, полученные в результате упругопластического нелинейного анализа. Они используются для определения новых оптимальных параметров. Для нелинейного анализа конструкции в состоянии упругой работы применяется метод касательной жесткости. В процессе оптимизации принято, что напряжения в растянутых стержнях пропорциональны пределу текучести. Напряжения в сжатых стержнях могут достигать критических значений, определяемых из условий устойчивости стержней. Жесткость конструкции ограничена предельными значениями узловых перемещений. Представлены примеры расчета.

Ключевые слова: оптимизация, упругопластическая система, условия жесткости и устойчивости, геометрическая нелинейность касательная жесткость, конечноэлементная дискретная модель..

Р. Клюкас, А. Кудзис. Предсказание вероятностной долговечности существующих строительных элементов // Journal of Civil Engineering and Management. Вильнюс: Техника, 2004, X т., № 2, с. 107–112.

Рассматривается влияние эксплуатационных и опытных воздействий на вероятностную надежность (пригодность, безопасность и долговечность) компонентов и элементов существующих ограждающих и несущих конструкций. Предлагаются переменные во времени модели для оценки надежности материалов, компонентов и элементов, подвергаемых длительным переменным и циклическим воздействиям. Дискутируются поправки индексов надежности существующих материалов, компонентов и элементов, подвергаемых эксплуатационным постоянным и переменным воздействиям. Рекомендуются принимать во внимание влияние скрытых дефектов на длительные индексы надежности материалов, компонентов и элементов. Учитывается влияние скрытых дефектов и усеченных распределений вероятности физико-механических сопротивлений материалов и компонентов на оценку индексов надежности. Анализируются методологические особенности предсказания долговечности строительных компонентов, а также необоснованные несвоевременные ремонты и замены. В качестве примера предлагаемого метода приведено предсказание вероятностной надежности ухудшающихся бетонных защитных слоев.

Ключевые слова: строительные элементы, надежность, долговечность, эксплуатационно-испытательная нагрузка, защитный слой.

И. Крея, Т. Микульски, Ч. Шимчак. Применение суперэлементов для анализа тонкостенных конструкций // Journal of Civil Engineering and Management. Вильнюс: Техника, 2004, X т., № 2, с. 113–122.

Предложена концепция моделирования балки суперэлементами. Это новое средство анализа конструкций из тонкостенных элементов. Предложенный алгоритм наиболее применим для решения задач, в которых применение моделей одномерных конструкций не обеспечивает получения правильного решения. К таким задачам относится задача вращения тонкостенных балок с полосами, а также задача определения распределения моментов двух направлений из рамы, составленной из тонкостенных элементов в узлах. Тонкостенная балка с жесткой кромкой или узел рамы моделируются из элементов оболочек. Матрица жесткости такой тонкостенной балки может быть составлена с использованием стандартных процедур единичных сдвигов. Точность предложенного одномерного элемента свидетельствует о его преимуществе по сравнению с детальным методом конечных элементов в том случае, когда для моделирования всей конструкции используется очень большое количество элементов оболочек.

Ключевые слова: тонкостенные конструкции, балки, рамы, жесткая кромка, статический анализ.

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