

A method for selection of parameters of ship propulsion system fitted with compromise screw propeller

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ABSTRACT



This paper concerns an algorithmic method for preliminary selection of parameters of ship propulsion system fitted with fixed screw propeller in the case when the ship's operation is associated with significant changes of waterway depth and width, hull resistance of the ship and its service speed. Mathematical model arguments of the considered design problem are main ship design parameters identified in the preliminary design stage. Structure of the formulated model complies with formal requirements for continuous- discrete mathematical optimization problems. The presented examples of application of the method concern an inland waterways ship fitted with compromise screw propeller optimized in the sense of minimization of fuel consumption for passing a given route distance within a given time. The elaborated method may be especially useful in designing such ships as : coasters, inland waterways ships, tugs, pushers, trawlers, mine sweepers, icebreakers etc.

Keywords : design of inland waterways ships, ship propellers, ship propulsion

INTRODUCTION AND PROBLEM DESCRIPTION

A method for selection of rational, or optimum in a given sense, technical solutions of a ship should take into account, already in the preliminary design stage, both obligatory and crucial design conditions and constraints. This paper concerns a method for determining, in the preliminary design stage, optimum values of the parameters of ship propulsion system fitted with fixed screw propeller in the case where hull resistance and service speed of the ship significantly varies during operation, that often takes place in the case of inland navigation.

Design process of inland navigation ships should takes into account the demand of adjusting the ship to future real service tasks including ship operation at significantly variable propulsion performance characteristics of the ship, whose variability results from :

- ★ changeable hydrographic conditions in water area of ship operation – shallow waters, narrow canals of variable width, winding river bends
- ★ significant changes of ship draught and displacement during voyage
- ★ frequent events of ship running aground and re-floating – unavoidable in shallow waters
- ★ hull resistance changes at various hull configurations – in the case of multi-hull arrangement.

Polish inland waterways are of small depth and often have the form of unregulated narrow river beds. In such case are fully justified the reasons for the application to inland navigation ships the propulsion systems with fixed screw propellers as they, in comparison with those with controllable pitch propellers, are characterized by :

- ◆ low manufacturing, assembling and possible repair costs of the propellers
- ◆ higher reliability and resistance against failure during stranding
- ◆ higher power conversion efficiency.

For operators of inland navigation ships the high reliability of propulsion system and easiness of its repair possible to be done even in almost any conditions along trip route are of crucial importance.

CLASSICAL PROBLEM STATEMENT

In the standard design method of preliminary selection of ship propulsion system parameters the following phases can be distinguished :

- ★ 1st phase of the approximate determining of nominal hull resistance characteristics in function of the speed v , ship and waterway parameters \bar{p}

$$R = R(v, \bar{p})$$

as well as the hull-propeller interaction coefficients, i.e. the wake fraction $w = w(v, \bar{p})$ and thrust deduction $t = t(v, \bar{p})$

- ★ 2nd phase of the determining of demanded power characteristics as well as geometrical parameters of screw propeller including its diameter, pitch, number of blades, and expanded blade area coefficient in function of ship speed and number of revolutions of propeller and engine; this is a basis for rational choice of an engine (-s) from producer catalogues.

In the subject-matter literature the above described design procedure is called „thrust approach” or „naval architect’s approach”; it leads to selection of propeller parameters and a specific engine of determined rated power and rotational speed. The ship’s designer – in cooperation with the ship’s owner and engine producer – determines permissible values of the engine’s operation parameters, in particular its continuous rating, rotational speed and supercharging parameters. The selection of continuous rating parameters of the chosen engine in the form of its torque Q and rotational speed n makes it possible to select values of parameters of power transmission devices and screw propeller itself.

The above presented classical design problem may have an unambiguous solution in the case of taking the simplifying assumption consisting in an arbitrary determination of hull resistance characteristics. To this end are assumed the nominal (design) hull resistance characteristics relevant to predicted conditions, i.e. the most probable service conditions of designed ship. Hence an unambiguous value of hull resistance corresponds to the ship speed given in the ship’s design assumptions, that forms the basis for the selection of parameters of propulsion system of maximum efficiency which is usually limited by necessity of satisfying a given set of design constraints.

If real ship service conditions appear different from those assumed in design procedure then the propulsion system will operate at a lower efficiency, increased specific fuel consumption, not fully utilized engine output, or with the engine overloaded by torque or rotational speed. The method of solving the classical design problems, described e.g. in [2, 3, 4], is used here as a comparative background for further considerations.

NON-STANDARD PROBLEM STATEMENT

In the case of ship propulsion system fitted with fixed screw propeller a non-standard problem of ship design theory is the designing of ship propulsion system at hull resistance characteristics significantly changing during ship service as well as at significantly changing hull -propeller interaction characteristics, w and t . The subject-matter literature does not provide a fully satisfactory algorithmic method useful in solving the so defined design problems.

The presented considerations are thought as an attempt to eliminate the gap by elaborating a method for selecting the propulsion system with fixed propeller, useful in solving design problems of ships intended for operation in the conditions when :

- ★ water area is shallow, of changeable depth and/or width
- ★ immersed part of ship hull undergoes intensive fouling
- ★ ship service is associated with up- and down-stream sailing
- ★ ship displacement significantly changes during voyage
- ★ ship service consists in towing or pushing other objects.

Especially important is the case when the ship has to operate both in deep and shallow or restricted waters as then hull resistance characteristics much differ in each of the

cases. The water area limitations influence both flow velocity distribution around the hull and ship-generated wave system (pressure distribution). Beginning from the limit speed up to critical one, hull resistance suddenly increases [6, 9]. Moreover the change in flow velocity distribution around the hull due to waterway bank effects makes the wake fraction and thrust deduction coefficients changing, thus they become variable, which seriously influences propeller performance.

The above described non-standard problem of determining the designed ship propulsion system parameters is of an utilitarian importance both technical and economical, however so far no fully satisfactory solution has been found for it in spite of the great interest paid to the problem [5, 6, 7].

The method in question exemplifies such a method for selecting the ship propulsion system parameters, which takes into account both changeable operational conditions of screw propeller and changeable hull resistance, and also arbitrary design constraints to be satisfied, and moreover which makes it possible to determine such values of the system’s parameters which optimize the propulsion system in a certain sense.

MATHEMATICAL MODEL OF THE DESIGN PROBLEM

Assumptions of the method for selecting the propulsion parameters

The screw propeller designing in accordance with the classical approach [2, 3, 4] consists in such selection of its geometrical characteristics as to obtain maximum value of propulsion efficiency and full utilization of continuous rating of driving engine at a given rotational speed in ship service conditions complying with its design assumptions. Moreover, the designed screw propeller should fulfill operational reliability criteria both for the propeller itself and elements cooperating with it.

In design practice, fulfillment of reliability requirements is equivalent to selection of a suitable material for the propeller as well as of geometrical parameters of the propeller in such a way as to ensure its sufficient strength and resistance against cavitation erosion.

Continuous service output power of the engine is usually taken as its characteristic power and its relation to engine’s rated power depends on engine’s dynamic performance and a way of determining the rated power, which depends on a type of engine and standards applied by producers of particular engines.

The continuous service output power is assumed a little smaller than, or equal to maximum continuous rating which the engine is capable of developing at a given rotational speed and not exceeding a permissible thermal load. However the so determined output power is usually not acceptable to ship owners for the reason of values of time between engine overhauls demanded by them; hence on ship owner’s request the service output power value is lowered by a few percent, and the lower output has to be developed at rated rotational speed or that somewhat lower.

Decision variables and parameters of the model

In accordance with formulation principles of the mathematical optimization problems the mathematical model of the considered design problem, built under appropriate simplifying assumptions, contains :

- ❖ a target function to be minimized (or maximized)
- ❖ constraints in the form of equalities and inequalities, resulting from technical sense of the design problem

- ❖ a vector of optimized decision variables together with permissible ranges of their determination
- ❖ a set of approximate analytical characteristics of the phenomena taken into account in the model.

The propulsion system with fixed screw propeller is considered as that commonly applied to ships operating in shallow waters [1, 6, 8].

The considered service route of the ship in question consists m waterway sections whose lengths are described by the vector $\bar{r} = (r_1, r_2, \dots, r_m)$. The waterway sections differ to each other by the parameters of water area and of the ship $\bar{p}_i = (p_{i,1}, p_{i,2}, \dots)$, which significantly affect propulsion system's performance.

The hull resistance $R_i(v_i, \bar{p}_i)$ in i -th water area of length r_i depends on the parameters \bar{p}_i and ship speed v_i developed over this section of the route. Moreover the hull resistance characteristics can be corrected by means of the coefficients ξ_i which represent arbitrarily assumed service margins.

Ship's speeds over particular route sections are described by the vector $\bar{v} = (v_1, v_2, \dots, v_m)$ determined during optimization process, and the propulsion system efficiency $\eta(\bar{v}, \bar{p}, \bar{s})$ over particular route sections depends on the propeller parameters $\bar{s} = (s_1, s_2, \dots)$, waterway parameters, water inflow velocity as well as parameters of ship's hull form assumed here fixed, i.e. not subjected to any correction and optimization.

In the model in question the following was assumed :

$$\bar{p}_i = (p_{i,1}, p_{i,2}, p_{i,3}) \text{ and } \bar{s} = (s_1, s_2, s_3, s_4, s_5)$$

where :

$p_{i,1} = h_i/T$ - ratio of the depth of i -th route section and ship's draught

$p_{i,2} = b_i/B$ - ratio of the width of i -th route section and ship's breadth

$p_{i,3} = v_{s_i}$ - current speed over i -th route section

$s_1 = z$ - number of propeller blades, from the set {3, 4, 5}

$s_2 = S_0/S$ - propeller expanded blade area ratio, from the set {0.55, 0.65, 0.70, 0.75}

$s_3 = D$ - propeller diameter not greater than that maximum permissible $D \leq D_{\max}$

$s_4 = H/D$ - propeller pitch ratio, one of the decision variables of the model, to be determined during optimization process

$s_5 = n$ - number of propeller revolutions, one of the decision variables of the model, to be determined during optimization process.

Target function to be minimized

The demanded propulsion power $P(v_i, \bar{p}_i, \bar{s}_i)$, necessary to obtain the ship speed v_i over the route section r_i , can be expressed as follows :

$$P_i = \frac{\xi_i R(v_i, \bar{p}_i) v_i}{\eta(v_i, \bar{p}_i, \bar{s})} = \frac{\xi_i R(v_i, \bar{p}_i) v_i}{\eta_p(v_i, \bar{p}_i, \bar{s}) \xi_k(v_i, \bar{p}_i, \bar{s}) \xi_r(v_i, \bar{p}_i, \bar{s}) \eta_t(\bar{s})} \quad (1)$$

The fuel cost K_i consumed to cover the distance of the section r_i with the speed v_i is equal to :

$$K_i(v_i, \bar{p}_i, \bar{s}) = k_j g_j(s_5) P(v_i, \bar{p}_i, \bar{s}) \tau(v_i) = \frac{k_j g_j(s_5) \xi_i R(v_i, \bar{p}_i) r_i(\bar{p}_i) [1 - w(v_i, \bar{p}_i, \bar{s})]}{\eta_p(v_i, \bar{p}_i, \bar{s}) [1 - t(v_i, \bar{p}_i, \bar{s})] \xi_r(v_i, \bar{p}_i, \bar{s}) \eta_t(\bar{s})} \quad (2)$$

where :

k_j - unit fuel cost [€/t]

g_j - specific fuel consumption [g/kWh]

τ_i - time period to cover the distance of i -th route section [h]

η_p - open –water propeller efficiency [-]

η_t - power transmission efficiency (from engine to propeller) [-]

ξ_k - hull "efficiency" characteristics [-]

ξ_r - rotational efficiency [-].

In the presented example of the method the total fuel cost K_c necessary the ship to cover voyage distance within the assumed time period τ_z , was taken as the criterion subjected to optimization :

$$K_c(\tau_z) = \sum_{i=1}^m K_i(v_i, \bar{p}_i, \bar{s}, r_i) \quad (3)$$

The set of values of propulsion system parameters, for which the set of model constraints is satisfied (set of permissible solutions) and the target function simultaneously reaches its minimum value, is considered the optimum solution of the model.

Design constraints of the model

The presented model was elaborated under the following assumptions :

- ➔ The voyage route of the total length r is consisted of m sections of given waterway characteristics :

$$r = \sum_{i=1}^m r_i \quad (4)$$

- ➔ The voyage duration time τ is consisted of the ship sailing time as well as the in-advance-estimated time τ_0 – intended for stays in ports, locking operations etc :

$$\tau = \sum_{i=1}^m \tau_i + \tau_0 = \sum_{i=1}^m \frac{r_i}{v_i} + \tau_0 \quad (5)$$

- ➔ The voyage duration time, τ_z , determined by the design assumptions is connected with the speeds v_i for covering distance of particular route sections, by the following relation :

$$\sum_{i=1}^m \frac{r_i}{v_i} + \tau_0 \leq \tau_z \quad (6)$$

- ➔ The permissible limits for ship's maximum speed over i -th route section were assumed as follows :

$$0 < v_i \leq v_i^{\max} \quad i = 1, 2, \dots, m \quad (7)$$

- ➔ Optimum propeller diameter is not to exceed that maximum permissible :

$$D(\bar{x}) \leq D_{\max} \quad (8)$$

- ➔ The range of permissible values of the propeller pitch H is as follows :

$$0.6 \leq \frac{H}{D} \leq 1.4 \quad (9)$$

- ➔ Minimum value of the expanded blade area ratio S_0/S of the propeller has to satisfy the Keller's cavitation criterion [10] :

$$\left(\frac{S_0}{S}\right)_{\min} \geq \frac{(1.3 + 0.3z) T_r}{(p_0 - p_d) D^2} + k \quad (10)$$

where :

z - number of propeller blades

p_0 - water pressure at propeller axis

p_d - saturated water vapour pressure

T_r - propeller thrust

$k = 0.1$

D - propeller diameter.

- ➔ Number of propeller rotations is not to exceed that maximum permissible :

$$n \leq n_{\max} \quad (11)$$

- ➔ Solution of the problem is searched for within the set of propellers having their hydrodynamic characteristics approximated by continuous analytical relationships. In the computer implementation of the model the characteristics of Wageningen propellers of *Ka* series intended for operation within 19A nozzles, are included [11] :

$$K_T \left(J, \frac{H}{D}, \frac{S_0}{S}, z \right) \in \{K_T(Ka3-65), K_T(Ka4-55), K_T(Ka4-70), K_T(Ka5-75)\} \quad (12)$$

$$K_Q \left(J, \frac{H}{D}, \frac{S_0}{S}, z \right) \in \{K_Q(Ka3-65), K_Q(Ka4-55), K_Q(Ka4-70), K_Q(Ka5-75)\} \quad (13)$$

APPROXIMATED CHARACTERISTICS OF THE MODEL

The presented method requires to determine in advance analytical relationships which approximate selected hydrodynamic characteristics of propulsion system, and are expressed in function of the variable design arguments \bar{x} ; in particular, it is necessary to have at one's disposal analytical representations of :

- the hydrodynamic characteristics $K_T(\bar{x})$, $K_Q(\bar{x})$, $\eta_p(\bar{x})$ of propellers
- the hull resistance characteristics $R(\bar{x})$ for particular route sections
- the hull-propeller interaction characteristics $w(\bar{x})$ and $t(\bar{x})$ for particular route sections
- the driving engine performance characteristics $P(\bar{x})$.

Analytical hydrodynamic characteristics of propellers

Making use of the data included in [11] one elaborated computer procedures for determining the analytical characteristics $K_T(\bar{x})$, $K_Q(\bar{x})$, $\eta_p(\bar{x})$ whose example graphical representation concerning *Ka3-65* propeller ducted in 19A nozzle is shown in Fig.1.

Hydrodynamic characteristics of ducted propellers *Ka 3-65* in nozzle 19A

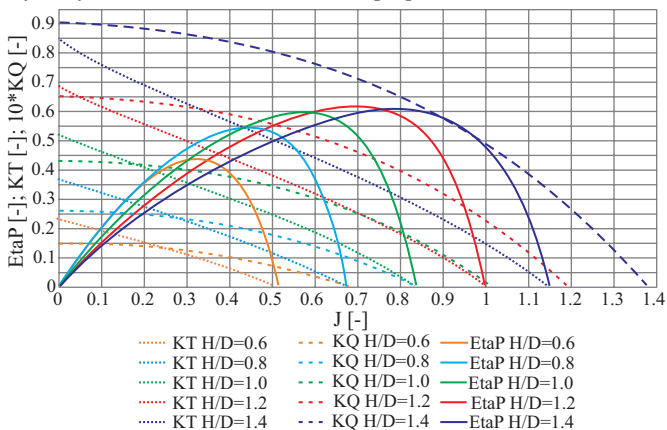


Fig. 1. Example graphical representation of analytically approximated characteristics of propellers .

Analytical hull resistance characteristics

On the basis of the results of hull resistance model tests [12] their analytical approximation was performed and as a result the continuous hull resistance characteristics versus ship speed and water area parameters [13] were achieved. The graphical representation of the approximated hull resistance curves is shown in Fig. 2.

Incowatrans pusher + barge approximated experimental resistance characteristics

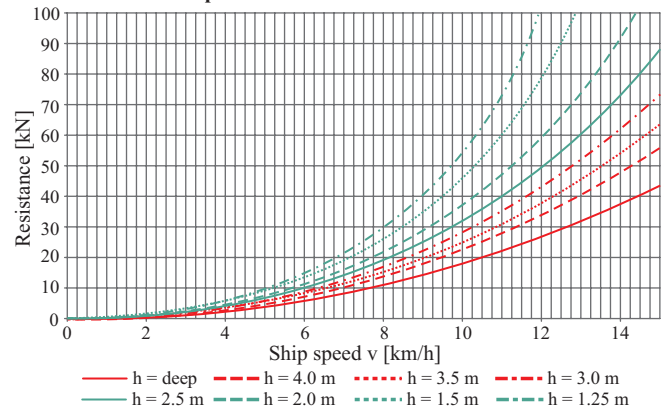


Fig. 2. Graphical representation of the approximated hydrodynamic characteristics of hull resistance .

Analytical characteristics of hull - propeller interaction

By making use of the elaborated method for determining the hull-propeller interaction characteristics in restricted waters [14] the characteristics of the coefficients $w(\bar{x})$ and $t(\bar{x})$ for the hull in question and particular route sections, were determined. The so obtained characteristics are presented in Fig.3 and 4, respectively.

Distribution of wake characteristics in shallow water

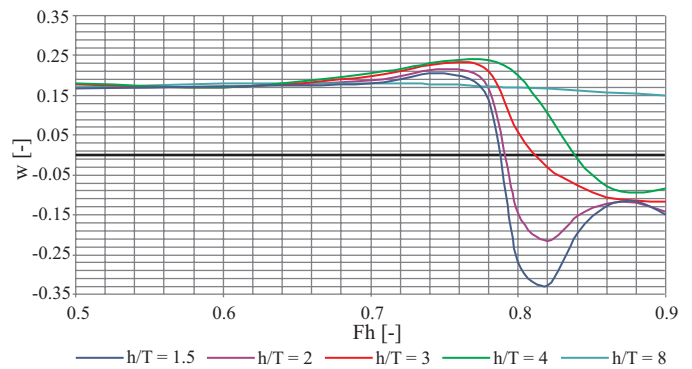


Fig. 3. Graphical representation of the approximated hydrodynamic characteristics $w(\bar{x})$.

Distribution of thrust characteristics in shallow water

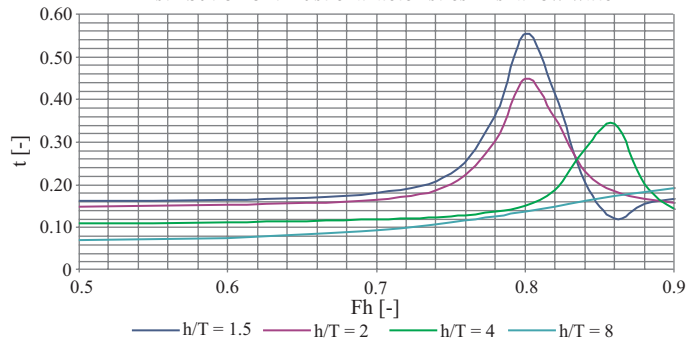


Fig. 4. Graphical representation of the approximated hydrodynamic characteristics $t(\bar{x})$.

Example of application of the method

The below presented numerical calculations were performed by means of the computer software [15]. Their results concern searching for optimum values of propulsion system parameters and speed of the ship designed within the frame of the **EU Eureka E!3065 InCoWaTranS** Project, and intended for tourist traffic along Polish inland waterways on the route Berlin - Królewiec.

The set of input parameters for the example task

Main particulars of two-segment ship :

- Ship's name 'M/v Eureka InCoWaTranS'
- Total length of the train (55m +55m) 110.00 [m]
- Ship breadth 9.00 [m]
- Ship draught 1.00 [m]
- Ship mass displacement 840.00 [t]
- Margin factor 1.15 [-].

Route parameters :

- Length of deep-water part of the route 250 [km]
- Depth of deep-water part of the route 5.0 [m]
- Length of shallow-water part of the route 315 [km]
- Depth of shallow-water part of the route 2.0 [m]
- Length of canals on the route 280 [km]
- Canal water depth 1.5 [m].

Screw propeller parameters :

- Characteristics of the propellers {Ka 3-65; Ka 4-55; Ka 4-70; Ka 5-75}
- Kort nozzle {No 19A}
- Maximum diameter of the propeller 1.0 [m]
- Maximum rotational speed of the propeller 600 [rpm]
- Minimum value of H/D ratio 0.6 [-]
- Maximum value of H/D ratio 1.4 [-]
- Rotational efficiency 1.05 [-]
- Power transmission efficiency 0.90 [-]
- Water density 1.0 [t/m³]
- Immersion depth of propeller axis 0.5 [m]
- Keller's criterion constant 0.1 [-].

The constraints imposed upon permissible values of ship speed and trip duration time :

- Maximum ship speed in deep water 15.0 [km/h]
- Maximum ship speed in shallow water 10.0 [km/h]
- Maximum ship speed in canals 7.0 [km/h]
- Voyage duration time 144 [h]
- Duration time of locking operations and port stays 24 [h].

Engine parameters :

- Specific fuel oil consumption 220 [g/kWh].

Financial parameter :

- Unit fuel oil cost 325 [€/t].

Results of optimization calculations

The results obtained from the first and last iteration of optimization calculations with the use of the above given task input data, are included in Tab.1, where the first row are results of the **first iteration** (fuel cost = 1462 €), and the second row are the results of the **last iteration** (fuel cost = 877 €), and the comprehensive full report from the calculations is included in [15].

The convergence process of selected results of optimization calculations in successive iteration steps is presented in Fig.5.

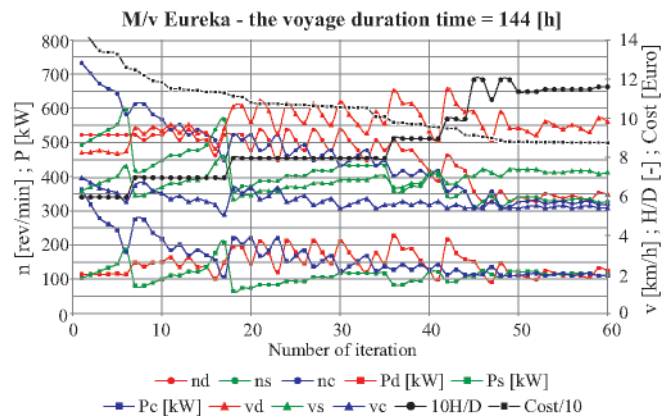


Fig. 5. Graphical representation of convergence process of selected results of optimization calculations

Tab. 1. Numerical results from the first and last iteration of optimization calculations.

Type	H/D	nd	ns	nc	vd	Eta0d	EtaPd	Rd	TNd	Pd	vs	Eta0s	EtaPs
[-]	[-]	[1/min]	[1/min]	[1/min]	[km/h]	[-]	[-]	[kN]	[kN]	[kW]	[km/h]	[-]	[-]
4	0.60	525	495	735	8.28	0.376	0.273	13.8	14.9	118	6.32	0.251	0.238
3	1.164	350	330	321	9.87	0.569	0.413	20.3	20.4	128	7.27	0.495	0.334
Rs	TNs	Ps	vc	Eta0c	EtaPc	Rc	TNc	Pc	Cavit	Jd	Js	Jc	Cost
[kN]	[kN]	[kW]	[km/h]	[-]	[-]	[kN]	[kN]	[kW]	[-]	[-]	[-]	[-]	[€]
14.7	15.1	106	7.00	0.209	0.198	38.4	39.3	365	1.01	0.30	0.24	0.18	1462
20.3	20.3	116	5.45	0.413	0.274	21.4	21.5	113	0.53	0.54	0.42	0.33	877

Description of selected items of Tab. 1. The following notation was applied : indices :

- d** - parameters concerning deep water
- s** - parameters concerning shallow water
- c** - parameters concerning canals.
- Type:** 1=Ka 3-65; 2=Ka 4-55; 3=Ka 4-70; 4=Ka 5-75;
- n** - rotational speed of propeller
- v** - ship speed
- Eta0** - open -water propeller efficiency

- EtaP** - behind-the-hull propeller efficiency
- R** - hull resistance in a given water area
- TN** - propelling force developed by propeller
- P** - demanded output power of the engine in a given water area
- Cavit** - index of Keller's cavitation criterion (Cavit<1 - no cavitation)
- J** - propeller advance ratio
- Cost** - total cost of fuel oil consumed to cover voyage distance within a given time period.



SCREW THRUST PROPULSION CHARACTERISTICS
 Delivered Engine Power $P_d=2 \times 135$ kW
 Screw K_a 3.65; Duct 19A - $n=475$ rev/min; $D=1.0$ m; $H/D=1.07$
 Twin Screws Inland Vessel *M/V EUREKA* InCoWaTranS Eureka Project E13065

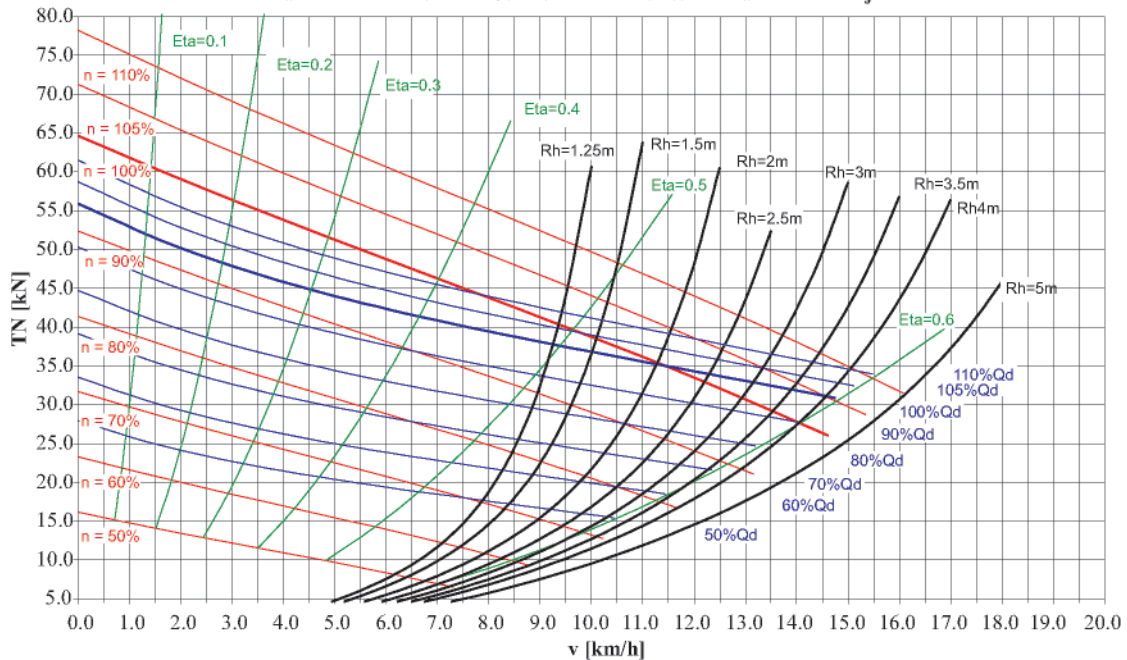


Fig. 6. Graphical representation of example characteristics of the propulsion force T_N developed by the designed propulsion system.

The obtained results of optimization calculations can be used to select values of propeller parameters and an engine of appropriate output power and rotational speed, that makes it possible to elaborate characteristics of the engine and propeller and to analyze this way their interaction in changeable service conditions; so obtained characteristics are shown in Fig.6 in the form of the computer-processed diagram [15].

SUMMARY

- The computer implementation of the calculation algorithm realizing the presented mathematical model, makes it possible to effectively solve the design problem consisting in selection of optimum (here in the sense of minimizing fuel consumption cost) parameters of ship propulsion system fitted with fixed propeller, in the case of ship operating at changeable hull resistance characteristics, on a voyage route in waterways of changeable depth and width.
- The presented results concern the example in which the designed ship has to cover its assumed voyage distance within 144 h including the duration time of port stays and locking operations equal to 24 h. By changing the effective voyage duration time, different optimum values of design parameters of the propulsion system can be respectively obtained.
- The presented design method is fully algorithmic and it does not require to appeal to designer's experience and intuition, hence it can serve to objectively, effectively and immediately find complex, difficult for intuitive assessment, solutions for propulsion system design problems.
- The method may also serve as a useful tool in aiding the design process in the phase preceding model tests as well as in determining the scope of model test program.

NOMENCLATURE

- b - route section width
- B - ship breadth
- D - propeller diameter [m]
- F_h - Froude number related to depth of water area
- g_j - specific fuel oil consumption [g/kWh]
- h - route section depth
- H - propeller pitch [m]
- J - propeller advance ratio [-]
- $k = 0.1$ - constant in Keller's cavitation criterion
- k_j - unit fuel oil cost [€/t]
- K - fuel cost
- K_T - propeller thrust coefficient characteristics [-]
- K_Q - propeller torque coefficient characteristics [-]
- m - number of route sections
- n - number of propeller rotations
- \bar{p} - vector of water area parameters
- p_d - saturated water vapour pressure
- p_i - parameter of a water area and ship
- p_o - water pressure at propeller axis
- P - propulsion power [kW]
- r - route section length
- R - hull resistance [kN]
- R_i - hull resistance in i -th water area [kN]
- \bar{s} - vector of propeller parameters
- t - thrust deduction characteristics [-]
- T - propeller thrust, ship's draught
- v - ship speed [km/h]
- v_i - ship speed developed in i -th water area [km/h]
- vs - route section current speed
- Q - engine torque
- w - wake fraction characteristics [-]
- \bar{x} - in general, vector of variable design arguments
- z - number of propeller blades [-]
- η - propulsion system efficiency [-]
- η_p - efficiency of open - water propeller [-]
- η_t - power transmission efficiency, from engine to propeller [-].
- τ - voyage duration time [h]

- τ_0 - duration time of port stays and locking operations [h]
- τ_i - time to cover distance of i-th route section [h]
- τ_z - assumed time period to cover voyage distance
- ξ_k - hull "efficiency" characteristics [-]
- ξ_r - rotational efficiency [-]
- ξ_i - additional resistance factor in i-th water area [-].

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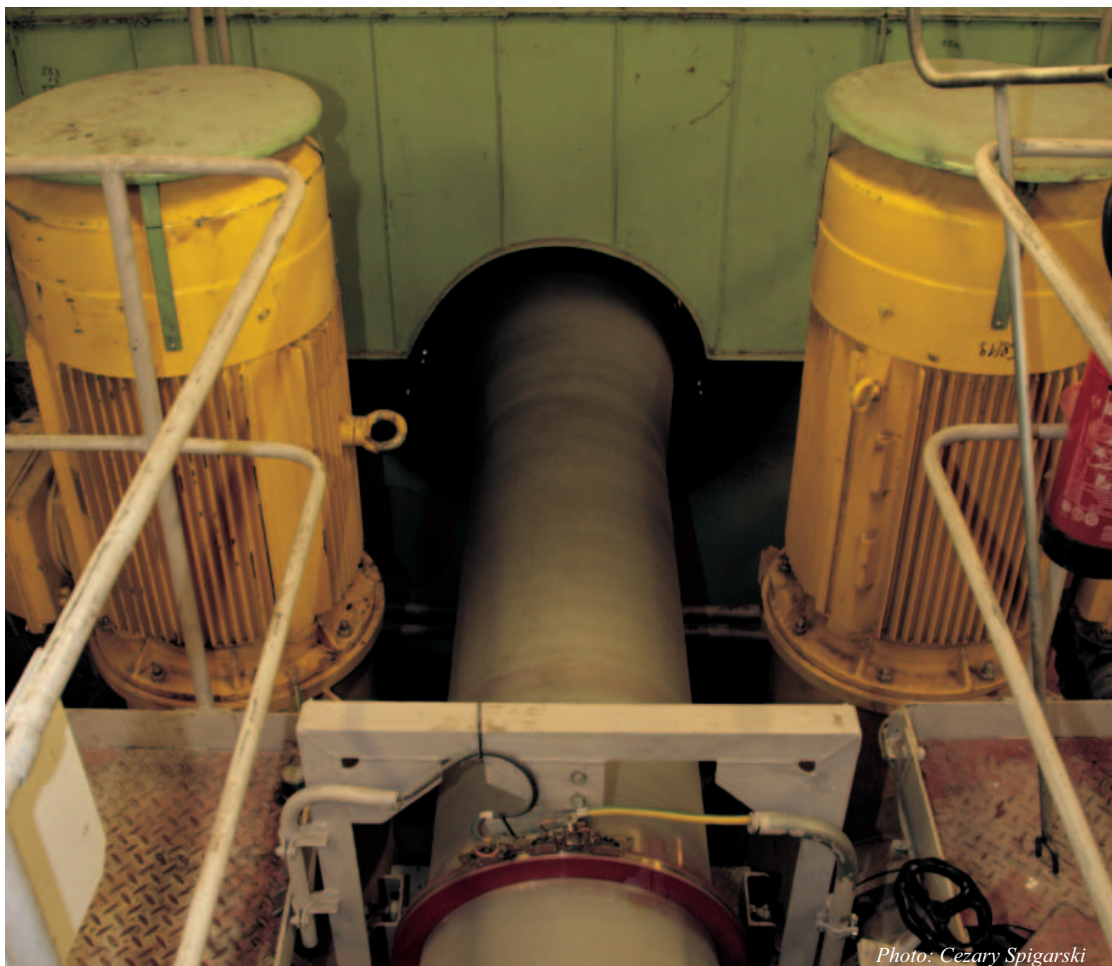


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