

# A Microwave Sensor with Operating Band Selection to Detect Rotation and Proximity in the Rapid Prototyping Industry

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**Abstract**—This paper presents a novel sensor for detecting and measuring angular rotation and proximity, intended for rapid prototyping machines. The sensor is based on a complementary split-ring resonator (CSRR) driven by a conductor-backed coplanar waveguide (CBCPW). The sensor has a planar topology, which makes it simple and cost-effective to produce and accurate in measuring both physical quantities. The sensor has two components, a rotor and a stator: the first of these (the CSRR) can rotate around its axis and translate along the plane normal to the ground of the CBCPW. A detailed theoretical and numerical analysis, along with a circuit model, of the unique sensor design is presented. The proposed sensor exhibits linear response for measuring angular rotation and proximity in the range of 30–60 degrees and 0–200  $\mu\text{m}$ . Another distinctive feature of the rotation and proximity sensor is the wide frequency band of applicability, which is an integral part of its novel design and is implemented through various dielectric material loadings on the CSRR. In the prototype of the proposed device, the stator (CBCPW) was fabricated on a 0.508-mm-thick RF-35 substrate, while the CSRR-based rotor was fabricated on TLY-5 and RF-35 substrates. The angular rotation, the proximity, the operating band selection and the sensitivity were measured using a vector network analyzer, and were found to be good matches to the simulated and theoretical results.

**Index Terms**—Additive manufacturing, conductor-backed coplanar waveguide, dielectric constant, material characterization, microwave planar sensor, proximity sensor, rapid prototyping industry, rotation sensor.

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## I. INTRODUCTION

THE FUTURE OF RAPID PROTOTYPING MACHINES, especially in the electronics industry (including aerospace, defense, and healthcare), depends on the precision obtained in calibration and fabrication. In devices operating in the microwave, THz, and optical ranges, precision is usually sought on the submicrometer scale. The distributed circuits used in radio frequency (RF) usually have thicknesses of substrate and metal layer in millimeters and micrometers, respectively. In line with the definition of penetration depth and the power handling capacity at higher frequencies, the thicknesses of the substrates and metal layers can decrease further to the micrometer and nanometer scales, respectively. Handling and fabricating distributed circuits at higher frequencies using the standard fabrication protocols becomes complex. This is one reason that low-cost fabrication of millimeter-wave and THz devices is quite difficult given the allowable surface roughness and precision. Most low-cost rapid prototyping machines (whether additive or subtractive) and computer numerical control (CNC) machines have problems in precisely calibrating their z-axis (height) [1]–[2], which leads to inaccurate prototypes, which are usually inhomogeneous in thickness. Z-axis calibration becomes more important in the design of multilayer printed circuit boards, where etching or adding an extra layer can create air gaps that may result in the severing of interlayer connections [3]–[4]. Additionally, precise control over the rotation of prototyping tools can be very helpful in controlling speed and position. Angular rotation and control become more important in the fabrication of 3D devices and components when working with different kinds of materials in prototyping industries [5].

Being able to detect rotation is one of the more important requirements in the automation industry; this is why rotation sensors based on capacitive [5], optical [6], and magnetic [7] principles are readily available. Recently, an angular displacement sensor based on the magnetic equivalent loop method is proposed with a shared magnetic field for higher accuracy [8]. A rotation monitoring system based on the wireless power transfer using transmitter and receiver coils equipped with class-E power amplifier and multiple motors is proposed in [9]. The rotation monitoring system is proposed for the prosthetic hands to measure in the angular rotation

from  $-45^\circ$  to  $+45^\circ$ , where the power transfer efficiency records a minimum value for  $\pm 45^\circ$  at a distance of 30 mm. A magnetoresistive sensor combined with permanent magnets is proposed to measure a complete rotation angle with low error for the high amplitude of magnetic field ranging from 100 Oe to over 1 kOe [10].

Proximity detection is another important parameter essential in the automation industry, including mobile communications. Recently, proximity sensors based on capacitive microelectromechanical technology [11], dynamic vision-sensing technology [12], received signal strength indicator (RSSI) [13], laser technology [14], and have been described in the literature. Recently, a proximity sensor based on parallel plate capacitance [15], infrared technology [16], ultrasonic technology [17], and multi-channel fiber optic technology [18], and microwave technology [19] have also been proposed.

Although the sensors presented in [6]-[10] offer low-error and good dynamic response, they are bulky due to coils, lenses, and magnets. The amount of coils windings in excitation and pickup coils and the weight of the metal in rotor and stator is a matter of inconvenience. The coil or magnet-based rotation sensors are often suitable for low-frequency operation, and the optics-based rotation sensors need regular maintenance as they suffer mainly in dirty environments and are quite sensitive to the color or the optical transparency of the target. Similarly, sensors presented in [11]-[18] have their own advantages and drawbacks, e.g., The fiber-based proximity sensors provide an excellent resolution in the nm scale; however, the dynamic range is limited in the mm range. The measurement accuracy of the capacitance type sensor varies depending on the dimension and the ground state of the object or material under test; therefore, a calibration method is essential.

In contrast, the microwave sensor is lightweight as compared with the weight of lenses and magnets used in the optics and magnetic sensors, respectively. Besides the planar technology, the small size is another advantage (the sensor is merely a wavelength long at the operating frequency). Microwave sensors are precise, and suitable for harsh environments, and compare favorably with their mechanical or electronic counterparts thanks to their distributed circuit topology and non-contacting methodology. This is the main reason that some groups of researchers have begun working on microwave-based rotation sensors. Detecting angular displacement using these coplanar sensors is done using various methodologies, including electromagnetic bandgap [20], bisymmetric resonators [21], electric-LC type sensors [22], S-type sensors [23], split-ring resonator (SRR) sensors [24], metamaterial-inspired sensors [25], horn-shaped SRRs [26], complementary split-ring resonator (CSRR) [27] and circularly polarized antennas [28].

However, to the best of our knowledge, a compact microwave sensor that would measure both physical quantities (rotation and proximity)—as generally required in the automation industry—is not to be found in the literature. This paper thus focuses on the development of a planar microwave

sensor that can control and measure—rotation and proximity, albeit not a combination of the two.

In this paper, a coplanar microwave sensor for measuring angular rotation and proximity is designed, fabricated, and tested. The sensor is based on a conductor-backed coplanar waveguide (CBCPW) loaded with a complementary split-ring resonator (CSRR), where the CSRR is allowed to rotate around the axis and free to move along the axis of CSRR (Fig. 1). The angular rotation is detected using the cross-coupling between the CBCPW and the CSRR, which varies as the CSRR is rotated. As a result, the effective mutual inductance changes, affecting the resonance. The proximity is detected using the near-field technique. The resonant frequency also changes here, but the change in the resonance of the CSRR is due to the change in the effective capacitance between the transmission line and the CSRR. The theoretical model for calculating the angular rotation and proximity was developed using first principles. The performance of the proposed sensor was checked using numerical simulations, which confirmed that the sensor was a good candidate for measuring both rotation and proximity. Additive manufacturing technology was used to build a fixture that holds the CBCPW and CSRR assembly with a micrometer screw, which can efficiently rotate and move as required with. The measurements were found to be in good agreement with the simulated and calculated data.

This paper is organized as follows: A detailed illustration of the design methodology of the proposed sensor is given in Section II. Section III discusses the multiband rotation sensor, while section IV describes the multiband proximity sensor. Section V describes the measurement carried out using the sensor, section VI discusses the outcomes, and section VII summarizes the conclusions.

## II. DESIGN OF THE ROTATION SENSOR

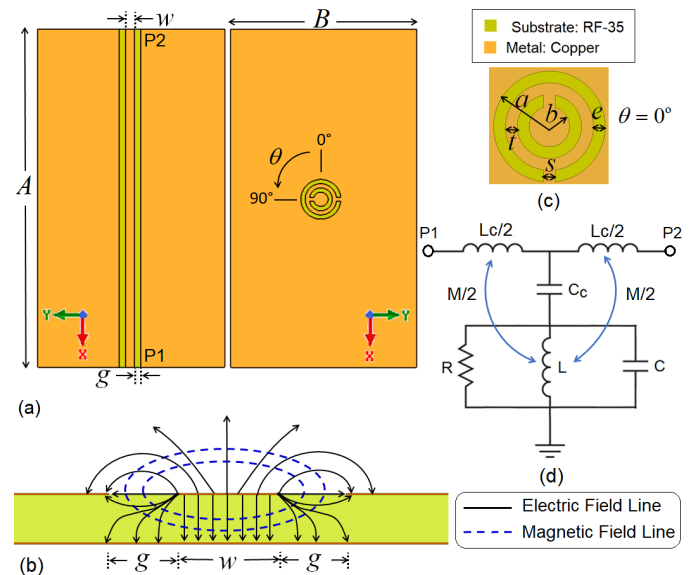


Fig. 1. (a) Top and bottom plane of the CSRR coupled conductor backed CPW, (b) electric and magnetic field lines of the CPW, (c) zoomed view of the CSRR with design parameters, (d) an equivalent circuit representation of the rotatable CSRR with cross-coupling.

### A. Theoretical Design

The sensor was designed using CBCPW technology, which offers better control of ratio between the gap  $g$  and the line-width  $w$  (Fig. 1) compared to standard CPW technology excited using a 50- $\Omega$  SMA connector. CBCPW also provides more mechanical strength and is well-suited to the narrow-band characteristics of a resonator sensor. Before considering the practical design, we investigate a structure consisting of a complementary split-ring resonator etched on the ground plane at the center of the CBCPW, as shown in Fig. 1(a). The CSRR is usually etched on the ground plane, keeping the slit of the CSRR (whose thickness is  $s$ ) transverse to the CBCPW ( $\theta = 90^\circ$ ). In this configuration, where the CSRR is symmetric to port P1 and port P2, the electric field lines of the CBCPW normal to the ground plane (as shown in Fig. 1(b)) excite the CSRR. However, a small axial rotation from  $\theta = 90^\circ$  (clockwise or counterclockwise) perturbs the symmetry of the CSRR, due to the asymmetric positioning of slits with respect to P1 and P2. In the asymmetric condition, the slits of the CSRR, which were parallel to the magnetic field lines of the CPW at  $\theta = 90^\circ$ , now make a finite angle with the magnetic field lines of CBCPW. At  $\theta = 0^\circ$  (as shown in Fig. 1(c)), the linkage of the magnetic field lines of the CBCPW with the slits of CSRR reaches its maximum value. From circuit theory, this induced effect can be explained by the mutual induction between the inductances of the CSRR ( $L$ ) and the CBCPW ( $L_c$ ), as shown in Fig. 1(d) [29]. The mutual inductance can be given as  $M = k\sqrt{LL_c}$ , where  $k$  is the coefficient of mutual induction, which depends on the axial rotation of the CSRR.  $C$  and  $C_c$  represent the effective capacitance of the CSRR and the capacitance due to the electric coupling of the CSRR with the CBCPW, respectively.

At first, the CSRR fed with the CBCPW (as shown in Fig. 1) is designed on RF-35 substrate with a dielectric constant  $\epsilon_s = 3.5$ , a loss tangent  $\tan \delta = 0.0018$ , height  $h_s = 0.508$  mm, and copper thickness  $T = 18$   $\mu\text{m}$ . The scattering coefficients are numerically computed for various combinations of the design parameters, where the resonant frequency of CSRR is estimated from the transmission coefficient data. To determine the characteristics of the CSRR under rotation—namely, the resonant frequency  $f$ , the bandwidth BW, and angular rotation—the CSRR is rotated from  $\theta = 0^\circ$  to  $360^\circ$ ; the results are given in Fig. 2. Since CBCPW technology offers flexibility in designing a 50- $\Omega$  transmission with adequate combinations of  $g$  and  $w$  values,  $f$  and BW are also calculated for various combinations of  $g$  and  $w$ . The dominant parameter in controlling the resonant frequency of CSRR, its outer radius  $a$  [Fig. 1(c)], is varied to obtain the desired characteristics, while keeping  $e = s = t = 0.5$  mm. To determine the design parameters at the central frequency of operation, the CSRR is simulated at  $\theta = 45^\circ$ ; the results are given in Fig. 2(a). In Fig. 2(a), the value of  $f$  increases as  $a$  decreases; however, it is interesting to note that, for a fixed value of  $a$ , the value of  $f$  increases as  $g$  and  $w$  increase. From Fig. 2(a), it is evident that the design of the CSRR-based sensor on CBCPW technology grants more degrees of freedom than microstrip technology. To feed the CBCPW directly from a 50- $\Omega$  subminiature A (SMA) connector, and to obtain the resonant frequency at 5.8 GHz on the ISM band, the value of  $g$  was taken as 0.7 mm, resulting in  $w = 1.1$  mm and  $a = 4.7$  mm. A similar observation was made for BW; Fig. 2(b) shows that increasing  $g$  and decreasing  $a$  gives a larger BW. Fig. 2(c) shows that the simulated locus of  $f$  is nearly sinusoidal with respect to  $\theta$ , and a 450 MHz BW is achieved at the 5.8 GHz in the ISM band. It may be noted that, with the help of additional circuitry capable of envelope detection, the angular velocity with respect to time can be estimated. However, the aim of this paper is to detect only the axial rotation and the proximity.

### B. Practical Design

The CSRR should be free to rotate around its axis if the design of the rotatable sensor is to be practical. A concentric gap of thickness  $t_g$  is thus etched out around the CSRR at a distance  $t_c$  from the outer ring [Fig. 3(a)]. An equivalent circuit of the rotatable CSRR-based sensor cross-coupled to the CBCPW is given in Fig. 3(b), where  $C_g$  represents the capacitance between the gap  $t_g$  of the two concentric cylinders of thickness  $t$  [30], whereas the equivalent inductance of the CSRR,  $L_m$ , which considers the cross-coupling effect, can be given as

$$C_g = 2\pi\epsilon_{eff}t \left[ \ln \left( 1 + \frac{t_g}{b+t_c} \right) \right]^{-1}; \quad L_m = L - k\sqrt{LL_c} \quad (1)$$

where  $\epsilon_{eff}$  is the effective permittivity. The resonant frequency of the rotatable CSRR-based sensor can be given as

$$f^{-2} = 4\pi^2 \left( \frac{CC_c + CC_g + C_cC_g}{C_c + C_g} \right) L_m \quad (2)$$

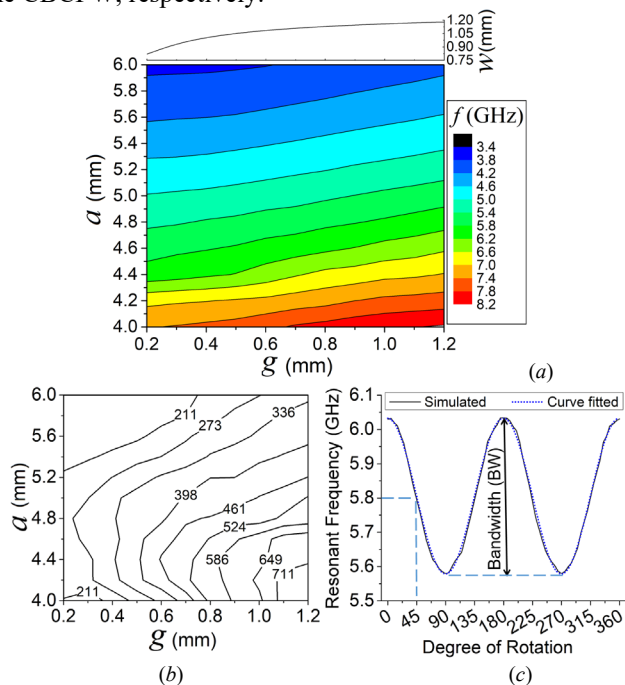


Fig. 2. (a) Color-filled contour plot of the resonant frequency; (b) contour lines labeled with bandwidth (in MHz) with respect to the change in  $a$  and  $g$ ; and (c) the locus of resonant frequency for one complete rotation of the CSRR



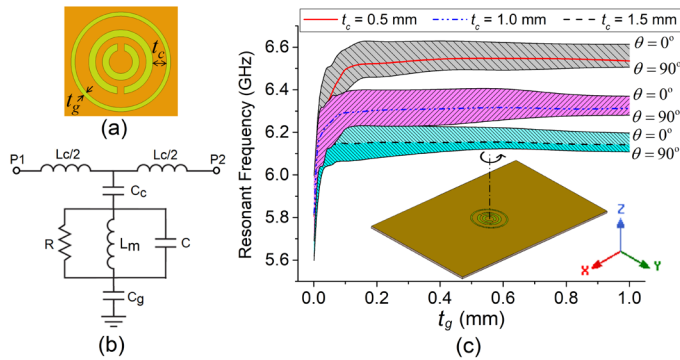


Fig. 3. (a) CSRR with a concentric gap for free rotation around the axis; (b) Equivalent circuit representation; (c) plot of resonant frequency at  $\theta = 45^\circ$  and bandwidth of the CSRR sensor with respect to variation in  $t_c$  and  $t_g$ , and 3D structural view indicating the location and operation of the rotor in the inset.

A parametric numerical study was performed to check the effects of  $t_c$  and  $t_g$  on the  $f$  and BW of the rotation sensor. From the results in Fig. 3(c), it can be observed that  $t_g$  strongly affects the resonant frequency of CSRR for values smaller than 0.1 mm. For  $t_g > 0.1$  mm, the resonant frequency of CSRR mostly depends on the value of  $t_c$ . This particular response can be explained from (2), where the logarithmic variation in  $C_g$  dominates at smaller values of  $t_g$ . It should be noted that BW is lower at higher values of  $t_g$  and  $t_c$ —that is,  $t_g$  changing from 0 to 1 mm results in BW decreasing; BW from 450 MHz to 91 MHz, 85 MHz, and 81 MHz for  $t_c = 0.5$  mm, 1 mm, and 1.5 mm, respectively. It is interesting to note from Fig. 3 that, for  $t_c = 1$  mm, the value of the resonant frequency at  $\theta = 45^\circ$  appears to be the center frequency of BW up to  $t_g = 0.4$  mm. The value of  $t_c$  is taken so as to achieve the maximum BW (170 MHz) with the smallest machinable dimension (= 0.3 mm), in order to result in a practical design. The design parameters of the CBCPW-driven CSRR-based rotation sensor is given in Table I.

TABLE I.

DESIGN PARAMETERS OF THE ROTATION SENSOR AND THEIR VALUES

Parameters	$A$	$B$	$w$	$g$	$a$	$b$	$e$	$t$	$s$	$t_c$	$t_g$
Values (mm)	40	25	1.1	0.7	4.7	3.2	0.5	0.5	0.5	1	0.3

### C. Extraction of Circuit Parameter

First, the CSRR was placed inside an air-filled rectangular cavity (10 mm  $\times$  10 mm  $\times$  10 mm), operating in TE<sub>101</sub> mode at 21.21 GHz (much higher than the fundamental frequency of the CSRR), and eigenmode analysis was performed using HFSS software. The results are displayed in Figs. 4(a) and (b), which show the electric and magnetic fields of the fundamental mode, along with the unloaded resonant frequency  $f_0 \sim 10.65$  GHz and the quality factor  $Q_0 \sim 483$ . Later, the CSRR was excited using CBCPW without a gap ( $t_g = 0$  mm) and with a gap ( $t_g = 0.3$  mm), as discussed earlier and shown in Figs. 4(c) and (d); the resonant frequencies were recorded as  $f_L = 5.64$  GHz and  $f_{Lg} = 6.22$  GHz, respectively. Based on the simulation data for  $\theta = 90^\circ$ , the value of the lumped circuit parameters were calculated using (3)–(6). Since there were five unknowns and four equations, a unique solution of the nonlinear system of equations (3)–(6) was

achieved, using the condition that the loaded quality factors calculated by numerical simulation and the circuit approach were the same.

It is interesting to observe from Fig. 4(c) and (d) that, although the overall size of the CSRR with a gap of  $t_g$  increases, the resonant frequency increases above that seen in the CSRR without a gap. Further, the confinement of the electric field is more pronounced in the CSRR with the gap, mainly on account of the increase in the quality factor. The CSRR with gap may thus also be an interesting design for high-frequency applications, while keeping the overall design relatively large.

$$f_0^{-2} = 4\pi^2 LC \quad (3); \quad Q_0 = \frac{R}{2\pi f_0 L} \quad (4)$$

$$f_L^{-2} = 4\pi^2 L(C + C_c) \quad (5); \quad f_{Lg}^{-2} = 4\pi^2 L \left( C + \frac{C_c C_g}{C_c + C_g} \right) \quad (6)$$

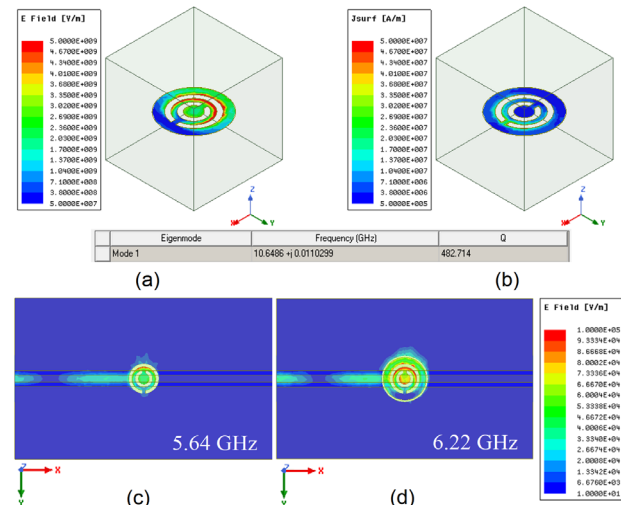


Fig. 4. (a) Electric field and (b) magnetic field of the CSRR using eigenmode analysis; Electric fields of the CSRR (c) without a gap and (d) with a gap, using frequency domain analysis.

The transmission coefficients calculated using the numerical simulation and circuit approaches are plotted in Fig. 5(a), and the extracted circuit parameters for the proposed CSRR at  $\theta = 90^\circ$  are given as  $C = 0.043$  pF,  $C_c = 0.109$  pF,  $C_g = 0.335$  pF,  $L = 5.25$  nH,  $R = 169.68$  k $\Omega$ , and  $L_c = 0.8$  nH.

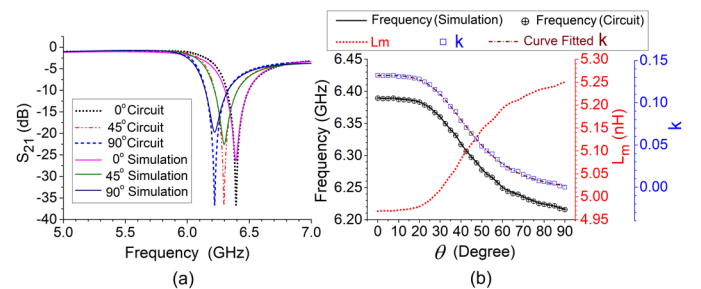


Fig. 5. (a) Comparison of transmission coefficients obtained from the numerical and circuit approaches, (b) response of the rotation sensor over an angular span of  $90^\circ$  with the values of their variable parameters.

It can be observed from Fig. 5(a) that the loaded quality factor of the sensor increased as  $\theta$  decreased from  $90^\circ$ , which is equivalent to a drop in the value of  $L$  of a parallel resonator

due to mutual induction from the CBCPW inductance. A detailed observation was carried out for a fine angular step of  $2.5^\circ$ . The results in Fig. 5(b) show that the coefficient of coupling  $k$  increased from 0 to 0.13, while the value of  $L_m$  decreased from 5.25 nH to 4.97 nH as the sensor was rotated from  $\theta = 90^\circ$  to  $0^\circ$ . To represent the angular rotation in terms of mutual induction, the calculated value of  $k$  was used with the dose–response curve fitting algorithm, giving an excellent fit with Pearson’s chi-squared test value of  $9.1 \times 10^{-7}$ . The relation can be given as

$$k = A_2 + (A_1 - A_2) / \left[ 1 + (\theta/A_0)^y \right] \quad \forall \theta = [0^\circ, 90^\circ] \quad (7)$$

where  $A_0, A_1, A_2$ , and  $y$  are constants with values  $45.39, 1.32 \times 10^{-1}, -6.73 \times 10^{-3}$ , and 4, respectively. It can be seen from Fig. 5(b) that the proposed rotation sensor has a linear relation with  $\theta$  over the broad angular span from  $30^\circ$  to  $60^\circ$ . Since linearity is required for practical instrumentation reasons, a linear relation between  $k$  and  $\theta$  (in degree) was developed as

$$k = B_0 + B_1\theta \quad \forall \theta = [30^\circ, 60^\circ] \quad (8)$$

where the values of  $B_0$  and  $B_1$  are  $1.94 \times 10^{-1}$  and  $-2.84 \times 10^{-3}$ , respectively. Since most practical sensors in various industrial applications require multiband operation, our rotation sensor offers band selectivity, which is explained in the next section.

### III. OPERATING BAND-SELECTION FOR THE ROTATION SENSOR

In the proposed design, band selectivity is introduced by separating the CSRR from the substrate, while etching it on a separate dielectric puck, as shown in Fig. 6(a). In this design, the dielectric material loading on the CSRR introduces another degree of freedom, as it affects the resonant frequency and the BW. By adopting dielectric pucks of different heights, and permittivities, various bands can be selected. The dielectric puck also increases the mechanical strength and rigidity of the CSRR, to meet the requirements of the rapid prototyping industry. Since the sensor consists of two parts, the movable part (the CSRR on a puck) is called the rotor, while the substrate (the CBCPW) is called the stator. A 3D structure of the assembled stator and rotor is shown in Fig. 6(b).

The introduction of dielectric support can be accounted for in a circuit model by adding a capacitance  $C_m$  in parallel with the capacitance  $C$  of the resonator, as shown in Fig. 6(c). The resonant frequency of the rotation sensor can now be given as

$$f_r = \left[ 2\pi \sqrt{(L - k\sqrt{LL_c}) \left( C + C_m + (C_c^{-1} + C_g^{-1})^{-1} \right)} \right]^{-1} \quad (9)$$

In order to obtain the resonant frequency and BW from (9), we need the values of  $C_m$  with respect to the various design parameters of the dielectric puck. A generalized theoretical model is thus developed here to calculate the values of  $C_m$ . The additional capacitance depends on the design parameters of the CSRR and type of material loading. The dielectric puck is assumed to be a dielectric substrate of finite thickness and diameter. To quantify the effect of the resonant frequency shift

when the puck is placed on the CBCPW, the effective capacitance is calculated as in [23]. However, to develop a precise model of  $C_m$ , the numerical data obtained by varying the dielectric constant  $\epsilon_m$  and the height  $h_m$  of the puck, as shown in Fig. 6(d), are mapped with the theoretical formula [31]. The numerical data of  $C_m$  is obtained for the rotor at  $\theta = 90^\circ$ —i.e., when  $k = 0$ . The generalized theoretical model of  $C_m$  can be given as

$$C_m \text{ (pF)} = 2\pi a \epsilon_0 \left[ m \frac{K(k_a)}{K(k'_a)} + n \sum_{i=m,s} (\epsilon_i - 1) \frac{K(k_i)}{K(k'_i)} \right] - N \quad (10)$$

$$k_a = \frac{t}{t + 2e}; \quad k_{m,s} = \frac{\sinh(\pi e/4h_{m,s})}{\sinh[\pi(t + 2e)/4h_{m,s}]}; \quad k'_{a,m,s} = \sqrt{1 - k_{a,m,s}^2}$$

where  $K$  represents the complete elliptic integral of the first kind,  $m, n$ , and  $N$  are arbitrary constants with values  $1.22 \times 10^{-1}, 8 \times 10^{-1}$  and  $1.72 \times 10^{-1}$ , respectively. To determine the values of these constants, a curve-fitting algorithm was used with the simulated values of  $C_m$  derived from the resonant frequency that had been determined by full-wave computation. Equation (10) allows the values of  $C_m$  to be precisely calculated for  $h_m = [0.25 \text{ mm}, 1 \text{ mm}]$  and  $\epsilon_m = [1, 10]$  with a typical 50% tolerance on nominal dimensions of the CSRR, as given in Table I.

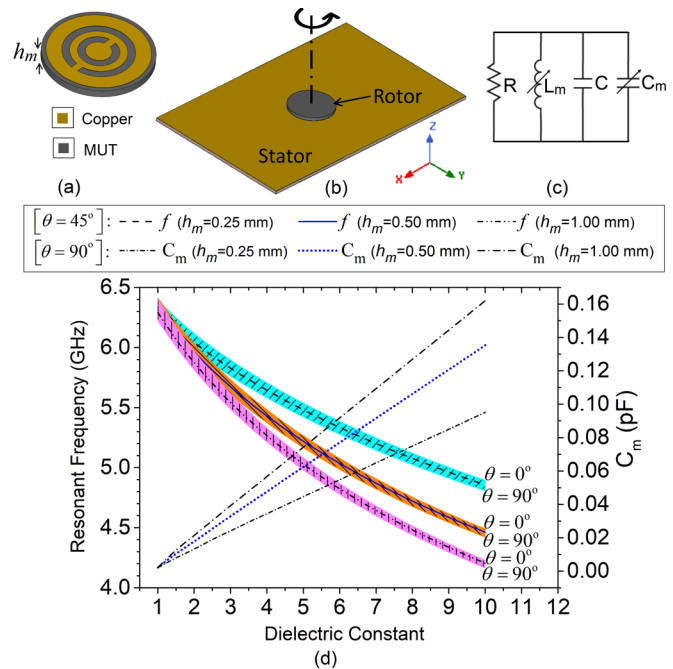


Fig. 6. (a) Band selection imposed by dielectric loading on the CSRR, (b) 3D structural view indicating the location and operation of the rotor, (c) equivalent circuit of the dielectric-loaded CSRR, (d) effect of various types of dielectric loading on resonant frequency and BW.

Fig. 6(d) shows that the dielectric loading—either in terms of the increase in  $h_m$  or  $\epsilon_m$ —leads to a decrease in the resonant frequency. However, a variation in  $\epsilon_m$  has a much greater effect in controlling the resonant frequency and BW than does  $h_m$ , mainly on account of the near-field of the CSRR, which has strong effect only close by; thus, increasing  $h_m$  for fixed  $\epsilon_m$  does not provide as much control as increasing  $\epsilon_m$  for a given

$h_m$ . It can be observed from Fig. 6(d) that various dielectric material loadings, ranging from  $\epsilon_m = 1$  to 10, provide a wide range of operating frequency—e.g., the resonating frequency at  $\theta = 90^\circ$  varies from 6.22 GHz to 4.81 GHz, 4.42 GHz and 4.17 GHz for  $h_m = 0.25$  mm, 0.50 mm, and 1.00 mm, respectively. The BW obtained for various dielectric pucks was also examined in Fig. 6(d), where it corresponds to the thickness of the curves. The upper and lower lines of each curve represent the resonant frequency versus the dielectric constant at the angular positions  $\theta = 0^\circ$  and  $\theta = 90^\circ$ , respectively, while a curve representing  $\theta = 45^\circ$  can also be observed between both the curves. The thickness of each curve decreases (as does BW) as the permittivity of the loading material increases. In quantitative terms, as the dielectric constant of the puck  $\epsilon_m$  changes from 1 to 10, BW varies from 170 MHz to 82.4 MHz, 65.4 MHz and 59.2 MHz for  $h_m = 0.25$  mm,  $h_m = 0.50$  mm, and  $h_m = 1.00$  mm, respectively.

#### IV. OPERATING BAND SELECTION FOR THE PROXIMITY SENSOR

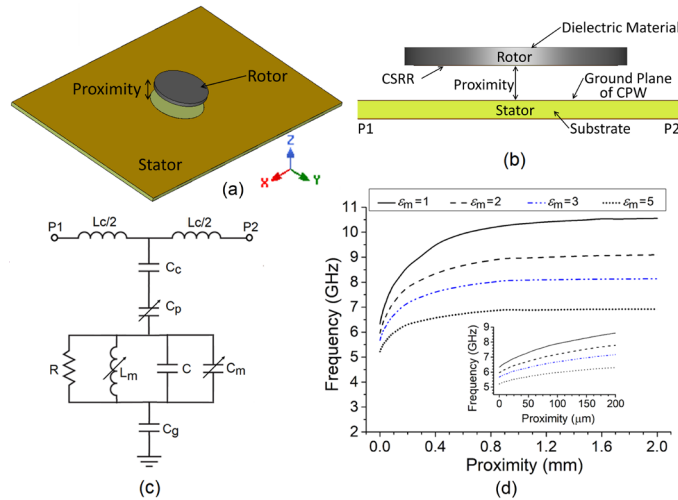


Fig. 7. (a) 3D structure of proximity sensor, (b) schematic for numerical analysis of proximity using the sensor arrangement, (c) equivalent circuit of the tunable proximity sensor, (d) response of the dielectric-loaded proximity sensor for  $h_m = 0.5$  mm.

As the previous section illustrated, it is possible to use the rotation sensor over a wide frequency band by using rotors with the same diameter but different material loadings. As band selection is a useful feature, the proposed proximity sensor is examined in terms of the resonant frequency shift for various pucks placed on the movable CSRR part. A 3D structure of the proximity sensor is shown in Fig 7(a), while a detailed schematic of the stator and movable part is illustrated in Fig. 7(b). The movement of the CSRR, initially placed directly on the ground plane of the CBCPW, is now restricted to the vertical direction, normal to the ground plane of the CBCPW, where  $\theta$  is arbitrarily fixed to  $0^\circ$ . This particular arrangement introduces a capacitance  $C_p$  in series with the coupling capacitance,  $C_c$ , as shown in the equivalent circuit diagram of the proximity sensor in Fig. 7(c). This capacitance changes as the CSRR moves along the normal to the ground

plane of the CPCPW. Though the movement of the rotor away from the ground plane of the CBCPW also alters the value of the gap capacitance  $C_g$ , to maintain continuity and simplicity, the value of  $C_g$  is considered to be constant, and this effect is jointly expressed in terms of  $C_p$ . Since the precision of z-axis calibration and printing requirements of rapid prototyping machines are on the scale of micrometers, the rotor of the proposed sensor is also translated in micrometer steps. A change in resonant frequency is observed, and the calculated data are plotted with respect to the proximity in a range of 2 mm from the ground plane of CBCPW, as shown in Fig. 7(d). For multiband operation, the dielectric constant of material loaded on the CSRR is varied over the range of 1 to 5.

It is interesting to note in Fig. 7(d) that the sensor is highly sensitive in the unloaded case where  $\epsilon_m = 1$ , and attains a resonating frequency of 10.6 GHz for a proximity of 2 mm, which is nearly the same frequency as that obtained by eigenmode analysis of the unloaded rotor in Figs. 4(a) and (b). This is mainly due to the weak coupling of CSRR through the CBCPW, which almost isolates the CSRR from the external circuitry. This arrangement may be very helpful in calculating the unloaded resonant frequency and the unloaded quality factor of planar resonators. It can be observed from Fig. 7(d) that the sensor is highly sensitive close to the CBCPW, and that the response is quite linear up to 200  $\mu\text{m}$  (Fig. 7(d) inset).

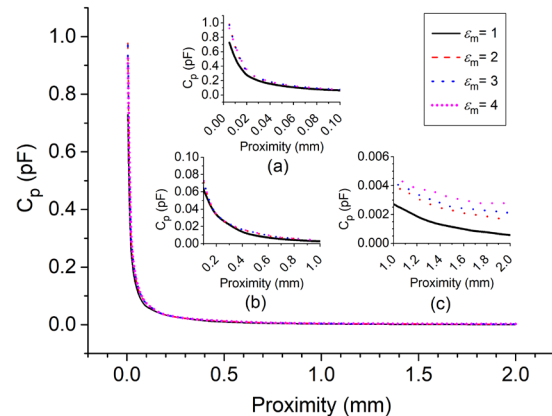


Fig. 8. Plot of capacitance  $C_p$  against proximity for various rotors.

To obtain a theoretical model of the resonant frequency, it is important to evaluate the capacitance,  $C_p$ . The effective change in  $C_p$  due to the change in proximity was thus studied in detail and the results are given in Fig. 8. From the calculated values of  $C_p$  against proximity and various dielectric loadings, it can be seen that the response of  $C_p$  is similar to the response of a parallel plate capacitor with a variation in the distance between the plates. From Fig. 8, it may be observed that the effect of proximity on  $C_p$  dominates over the material loading. To elucidate the dominant behavior of the proximity, the plot is illustrated in three inset pictures (Figs. 8(a)–(c)), which cover most of the proximity range. Though the figure shows that the resolution of the material loading in terms of  $C_p$  is less than 0.001 pF, the effect should still be taken into account over the whole proximity range in order to calculate  $C_p$  precisely.  $C_p$  can be given in picofarads, considering the material loading effect, as



$$C_p = (p\varepsilon_m + q)x^{-1} \quad (11)$$

where  $p=1 \times 10^{-3}$ ,  $q=4 \times 10^{-3}$ ,  $x$  is in mm. Based on the circuit analysis, the resonant frequency of the proximity sensor is

$$f_p = \left[ 2\pi \sqrt{(L - k\sqrt{LL_c}) \left( C + C_m + (C_c^{-1} + C_g^{-1} + C_p^{-1})^{-1} \right)} \right]^{-1} \quad (12)$$

## V. SENSITIVITY

The sensitivity of the proposed sensor was analyzed and quantified for various rotors with a thickness of  $h_m = 0.5$  mm. The sensitivity was calculated in the linear range as the derivative of sensor response with respect to the physical quantity being measured. From Fig. 6(c), the angular rotation sensitivity is 4.23 MHz/degree, 3.80 MHz/degree, 3.37 MHz/degree, and 2.73 MHz/degree, using rotors with dielectric constants of 1, 2, 3, and 5, respectively. Fig. 7(c) shows that the proximity sensitivity is 11.57 MHz/ $\mu\text{m}$ , 9.29 MHz/ $\mu\text{m}$ , 7.57 MHz/ $\mu\text{m}$ , and 5.53 MHz/ $\mu\text{m}$  using rotors with dielectric constants of 1, 2, 3, and 5, respectively.

## VI. MEASUREMENT

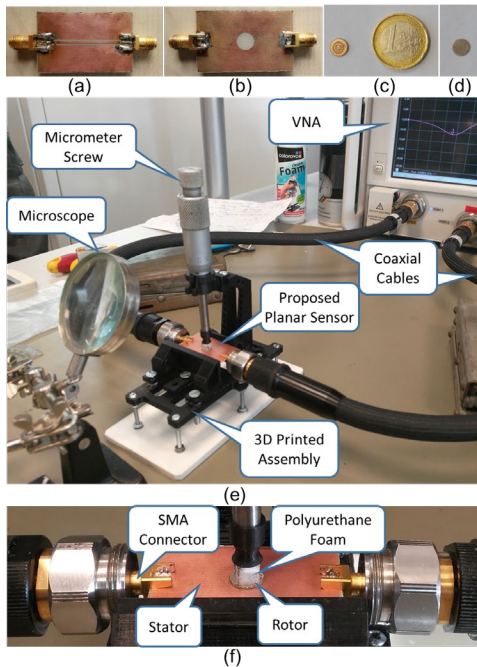


Fig. 9. (a) Top layer and (b) bottom layer of the fabricated CBCPW based stator; (c) top view and (d) bottom view of the fabricated rotor; (e) the measurement setup, and (f) enlarged view of the assembled sensor.

The stator was fabricated on a 0.5-mm-thick RF-35 substrate using standard photolithography techniques. The picture of the top and bottom layers of the fabricated CBCPW based stator is provided in Figs. 9(a) and (b). The rotor was fabricated on TLY-5 ( $\varepsilon_s = 2.2$ ,  $\tan \delta = 0.0009$ ) and Taconic RF-35 substrates. The top and bottom views of the fabricated rotor is given in Figs. 9(c) and (d), respectively. A support fixture made of Acrylonitrile Butadiene Styrene (ABS) was realized by additive manufacturing to hold the stator and rotor components in perfect alignment, which is essential to precisely measure angular rotation and proximity. A test

fixture was assembled from ABS using a micrometer screw gauge with two degrees of freedom in the vertical direction and rotational movement around the axis. The resolution of the micrometer screw used in the experiment is 0.01 mm, the range of measurement is 0 to 25 mm, and the accuracy of the micrometer is  $\pm 10 \mu\text{m}$ . A microscopic lens was used for manual alignment and taking readings of angular rotation and proximity data. Two subminiature version A (SMA) connectors were mounted on the two ports of the sensor and connected to the vector network analyzer using coaxial cables. The setup for measuring angular rotation and proximity is shown in Fig. 9(d), whereas a detailed enlarged view of the assembled sensor is presented in Fig. 9(e). For uniformity, this section is divided into two subsections dealing with the measurement of angular rotation and the measurement of proximity.

### A. Measurement of Angular Rotation

In measuring angular rotation, vertical translation of the rotor is prevented and the center of the rotor is aligned, while firm contact is made with the geometric center of the stator. Only rotational movement around the axis of the rotor is allowed. The angle of rotation of the stator was varied from  $0^\circ$  to  $90^\circ$  in 11 steps. The transmission coefficients were recorded and the resonant frequency corresponding to the angular displacement was measured. The results are plotted in Fig. 10, which also includes data simulated using full-wave FEM code to imitate the real measurement situation—i.e., the stator with SMA connectors and the rotor connected to the axis of the micrometer screw gauge using 5-mm-thick polymethacrylimide (PMI) structural foam. This PMI foam, also referred to as Rohacell, has air-like dielectric properties (dielectric constant 1.07 and loss tangent 0.002 at 5 GHz) and provides the required mechanical strength for rotation and fair isolation between the rotor and the metallic support from the micrometer screw gauge. To verify the theoretical approach described in Section III, the data obtained using (9) are also plotted in Fig. 10.

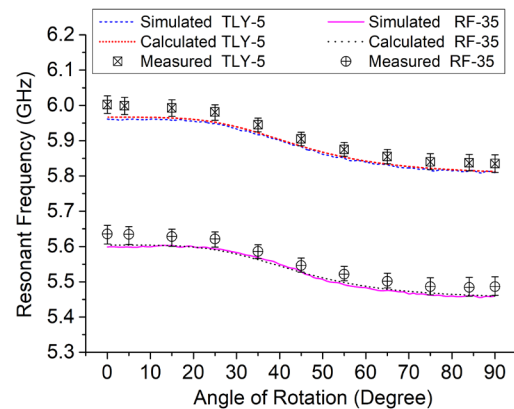


Fig. 10. Measurement of angle of rotation using the microwave sensor.

### B. Measurement of Proximity

In measuring proximity, angular rotation around the rotor's axis is prevented and the center of the rotor is aligned with the geometric center of the stator. Vertical movement along the axis of the rotor is allowed. The vertical displacement of the stator was varied from 0 mm to 2 mm in 24 steps. The

transmission coefficients were recorded and the resonant frequencies corresponding to the proximity were measured. The proximity results are plotted in Fig. 11 with simulated data imitating real conditions, as explained previously. To verify the theoretical approach described in Section IV, the data obtained from (12) are also plotted in Fig. 11.

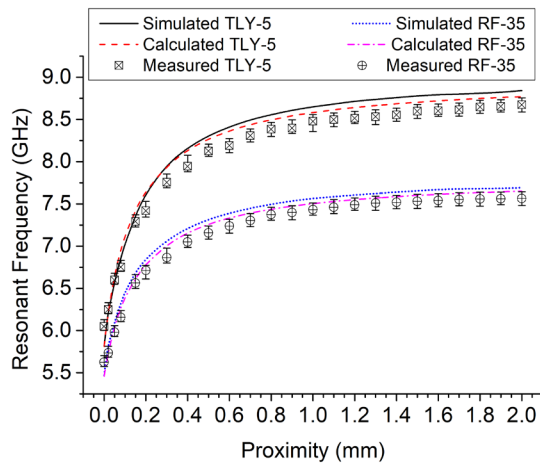


Fig. 11. Measurement of proximity using the microwave sensor.

## VII. DISCUSSION

In Figs. 10 and 11, the good match between the calculated and simulated data, obtained numerically by emulating real conditions, validates the newly developed formulae (9) and (12) for measuring respectively the angular displacement and proximity with the sensor. The angular displacement and proximity measurements were repeated several times, and the mean values are plotted with error bars in Figs. 10 and 11. In Fig. 10, the intrinsic air gap of a few micrometers between the rotor and the stator may explain the value being higher than the corresponding simulated or calculated data; however, the values are in good agreement. From Fig. 11, it can be observed that the measured data closely follow the simulated and calculated data. The standard deviation in the angular rotation and proximity measurements were 0.02 MHz and 0.08 MHz, respectively. From Figs. 10 and 11, the performance of the sensor was found to be linear from  $30^\circ$  to  $60^\circ$  when measuring angular rotation and up to  $200 \mu\text{m}$  when measuring proximity. The angular rotation measurement sensitivity was calculated from the slope of the curve in the linear region to be 3.18 MHz/degree and 2.97 MHz/degree using the rotors with TLY-5 and RF-35 dielectric pucks, respectively. The sensitivity of proximity measurement in the linear range of operation was found to be 7.85 MHz/ $\mu\text{m}$  and 5.87 MHz/ $\mu\text{m}$  using the TLY-5 and RF-35 dielectric pucks, respectively. The angular rotation measurement shows that the BW of the proposed sensor is 167 MHz and 149 MHz using the TLY-5 and RF-35 rotors, respectively. Fig. 10 shows that the bands corresponding to TLY-5 and RF-35 rotors were well isolated at 367 MHz, which demonstrates the band selectivity of the sensor. Unlike the almost constant band isolation in angular rotation, the band isolation measured for proximity sensing was found to vary nonlinearly from 379 MHz to 1.11 GHz over the proximity range. From Fig. 11, the maximum

frequency sweep is 2.625 GHz and 1.94 GHz, using TLY-5 and RF-35 rotors, respectively.

### A. Enhancing the Dynamic Range of Rotation

The primary purpose of the proposed sensor is to provide a unified scheme for the measurement of rotation and proximity; however, the present configuration offers angular rotation in a limited range of  $0^\circ$ - $90^\circ$ . It is mainly due to the presence of two symmetry planes in the angular span of  $180^\circ$ ; the first symmetry plane is along the y-axis at  $\theta = 0^\circ$ , and the second symmetry plane is along the x-axis at  $\theta = 90^\circ$ , as shown in Fig. 1(a). The dynamic range of the angular rotation can be increased in a number of ways, a few of them are suggested here.

The idea of independent rotation of both the rings of CSRR offers an extended range of angular rotation from  $90^\circ$  to  $180^\circ$ . The extension of dynamic range is due to the reduction of the number of symmetry planes from 2 to 1 in the angular span of  $180^\circ$ ; the only symmetry plane is along the x-axis. Out of the two cases, one particular case is discussed when the outer ring is fixed, and the inner ring is rotated. The schematic and the results are shown in Figs. 12(a) and (b), respectively. From Figs. 2(c) and 12(b), it can be noticed that the dynamic and linear ranges of operation are increased from  $90^\circ$  to  $180^\circ$  and from  $30^\circ$ - $60^\circ$  to  $30^\circ$ - $150^\circ$ , respectively. Another way to enhance the output dynamic range of the proposed sensor for detecting the rotation is to exploit the asymmetric properties of the scattering (S) parameters. The magnitude profile (resonant frequency, quality factor) of the sensor is an even function of rotation angle; however, this does not apply to the phase response. Considering the phase response of the two-port S parameters, the dynamic range of the sensor can be increased from  $90^\circ$  to  $180^\circ$ . The dynamic range can also be extended by wisely choosing the type of stator and rotor. A typical example of enhancing the dynamic and linear ranges of operation are presented in [16].

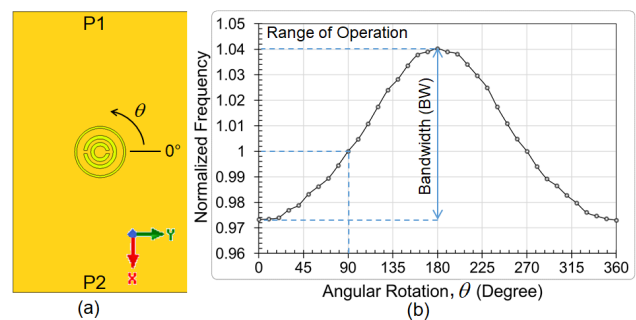


Fig. 12. Rotation of inner ring to extend the dynamic and linear ranges of operation, and (b) variation of normalized resonant frequency with rotation.

### B. Converting Output Parameters to Voltage/Current

For making the cost-effective, practical angular rotation and proximity sensor, it is essential to change the measurement technology of the proposed sensor from the resonant frequency to either voltage or current. The electronic equipment required to process the microwave signal (in the frequency domain) into voltage waveform (in the time domain) is discussed in [12], [14]-[15]. A general representation of extracting the envelope of the modulated



signal due to rotation and proximity measurement in terms of voltage is shown in Fig. 13. The function generator sinusoidal output close to the resonant frequency of the proposed sensor propagates through the planar microwave sensor, which is directed to the rectifier/envelope detector using a circulator. The circulator is used to isolate the sensor from the rectifier to avoid signal interference due to impedance mismatch. For making such a sensing system compatible with the planar technology, a magnetless isolator, as described in [32], can be effectively used. The output voltage waveform in the time domain can be visualized in the oscilloscope.

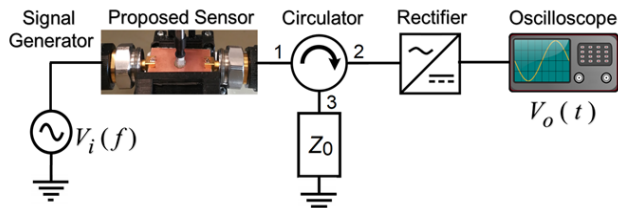


Fig. 13. A general schematic to extract the envelope of the modulated signal due to rotation and proximity measurement

In the presence of resistive loss, it may be possible that voltage signal in a parallel circuit varies from one node to the other node, while the magnitude of current remains the same throughout the series circuit. To represent the rectified voltage in terms of the current, additional circuitry, e.g., an op-amp with negative feedback may be required.

### C. Measurement of Unknown Rotation or Proximity

The simultaneous measurement of unknown rotation and proximity from the measured resonant frequency is not possible with the proposed scheme. It is mainly due to two unknowns depending on a single measurable quantity; therefore, uniqueness is not guaranteed. However, the technique can be extended to measure the detection of rotation or proximity, one at a time, in a very effective way. It is a two-step process. In the first step, the type of movement, either rotation or proximity, is identified. The identification of the type of movement rotation or proximity is possible due to the uniqueness of the resonance profile. From Figs. 2(c), and 7(d), it can be easily identified that rotation provides a periodic change in the resonant frequency with a period of 180°, whereas the proximity provides monotonic linear behavior. After processing the signal, as explained in Fig. 13, the angular velocity can be calculated from the period of the envelope signal, recorded by the oscilloscope. One full rotation provides quite a limited BW (maximum 400 MHz) in the resonant frequency, whereas the proximity has broader BW and higher sensitivity than rotation. Once the type of movement is identified, equations (9) or (12) can be used to get the precise value of rotation and the proximity.

### D. State of Art of Rotation and Proximity Sensor

For making a fair comparison of the proposed sensor with the sensors available in the literature, the state of the art of the rotation and proximity sensor is presented in Table II. The qualitative comparison among various sensors is made on the basis of the technology, adaptability, and sensing type,

whereas the quantitative comparison is performed on dynamic range, sensitivity, sampling, and accuracy. The sensitivity for measuring rotation angle (in degrees) is presented in terms of dB/° and MHz/°, while the sensitivity for measuring proximity is provided in MHz/μm. Since the sampling rate is a major limiting factor for the infrared and ultrasonic sensors, it is given in ms, and the accuracy of proximity is provided in ± mm. From Table II, it can be noted that the proposed sensor bears an impressive specification among the rotation and proximity sensors.

TABLE II. STATE OF THE ART OF ANGULAR DISPLACEMENT SENSORS AND PROXIMITY SENSOR

Ref.	Technology/ Stator: Rotor	Dynamic Range	Adaptability	Proximity Sensing	Sensitivity/ Sampling/ Accuracy	
					Rotation	Proximity
[21]	Microwave/ CPW: SRR	0°-90°	X	X	0.26 dB/°	---
[25]	Microwave/ Microstrip: U-type	0° to 180°	X	X	1.81 MHz/°	---
[26]	Microwave/ CPW: Horn-type	0° to 8°	X	X	1.75 dB/°	---
[27]	Microwave/ Microstrip: CSRR-RF35	0° to 90°	✓ (Freq. Band)	X	1.65 MHz/°	---
[16]	Infrared/ Pulsed mode	(Fixed) 10 cm	X	✓	---	150 ms ---
[18]	Ultrasonic Sensor	3-100 cm	X	✓	---	1 ms ±1 mm
[19]	Fiber Optic Sensor	1 mm	X	✓	---	± 3x10 <sup>-5</sup> mm
This work	Microwave/ CBCPW: CSRR-TLY5 CSRR-RF35	0° to 90° and 0 to 2 mm	✓ (Freq. Band Selection)	✓	3.18 MHz/° 2.97 MHz/°	7.85 MHz/μm 5.87 MHz/μm

## VIII. CONCLUSION

This paper presented the design, fabrication, and testing of a planar microwave sensor for measuring angular displacement and proximity. It was observed that the sensor can effectively measure both of these physical quantities, which are crucial in the automation industry. The operating frequency range can be selected using several rotors, keeping diameter unchanged while altering the material loading. The prototype is easy to fabricate and assemble, is lightweight, and sufficiently sensitive to measure the angle of rotation in degrees and proximity in micrometers. The formulae proposed in this work were quite accurate for calculating the angular rotation and proximity. The sensor has potential applications in the robotic, industrial, and automotive fields for the calibration and control of errors.

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