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## 7 **Discussion: Horizontal stress increase induced by deep vibratory** 8 **compaction**

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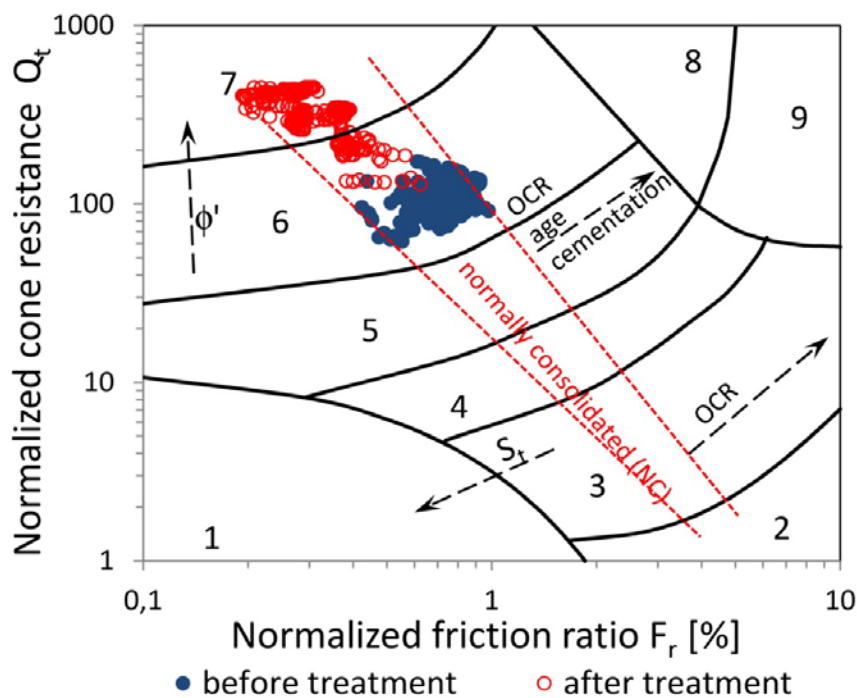
## 31 32 **Contribution by L. Bałachowski, N. Kurek and J. Konkol**

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34 Evaluation of the horizontal stress increase induced by deep compaction is one of the most  
35 difficult topics in geotechnics. The approach of Massarsch et al. (2020) to determine the  
36 overconsolidation ratio (OCR) in compacted soil based on sleeve friction and lateral stress  
37 index seems to be questionable. In Figures 12 and 24 of their paper, the irregular shape of the  
38 OCR with depth and sharp peaks cannot be physically explained. Moreover, the OCR values  
39 based on sleeve friction and lateral stress index are inconsistent. For instance, 14 days after  
40 dynamic compaction, the OCR values determined with the lateral stress index(Figure 9) are  
41 four to seven times higher than those based on sleeve friction (Figure 7). Even greater  
42 inconsistency in the OCR values determined using cone penetration test (CPT) with water  
43 pressure measurement (CPTU) and the Marchetti dilatometer test (DMT) was shown for  
44 vibroflotation (Figures 12 and 14). Very high OCR values, largely exceeding 100 (Figure 14),  
45 estimated with the correlation using the DMT are highly unrealistic. The upper bound of the  
46 OCR-based  $K_0$  should correspond to the passive earth pressure coefficient. Additionally, the  
47 use of sleeve friction is generally considered less reliable than the cone resistance, so the  
48 proposed correlation (Equation 2) should be used with caution. In the contributors' opinion, it  
49 would be better to use the OCR correlations based on combined CPTU and DMT tests, as  
50 proposed by Baldi et al. (1986), Monaco et al. (2014) or Marchetti (2015). Additionally,

51 Figure 17 seems to be erroneous, as the report of sleeve friction elaborated using the data  
52 from Figure 15 is higher than one at larger depths.  
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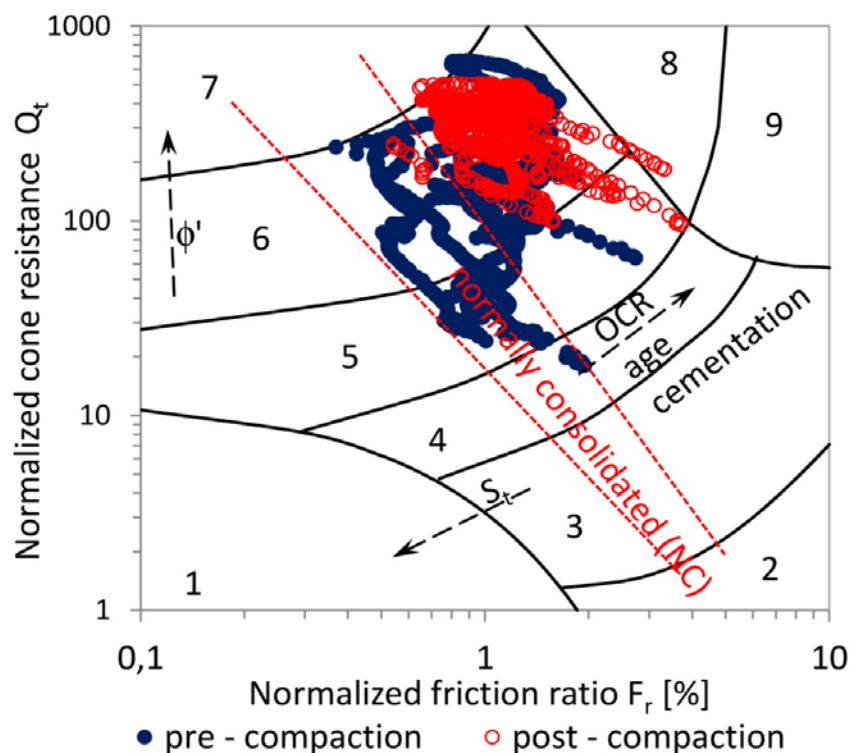
54 To estimate the OCR of compacted sand, the authors used Equation 12 based on calibration  
55 chamber tests with the soil mass prepared by pluviation and then mechanically overloaded  
56 (Lee et al., 2011). Such a procedure is, however, quite different to the mechanisms of deep  
57 soil vibratory compaction with rearrangement of grains, prestressing and, finally, the  
58 formation of a new soil fabric. To meet field conditions, such a type of correlation should be  
59 critically reviewed, including the results of calibration chamber tests where the soil mass was  
60 densified with a vibrator.  
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62 The authors used the classification of Robertson et al. (1986) to present the evolution of soil  
63 behaviour type due to the compaction process. In the contributors' opinion, use of the diagram  
64 presented by Robertson (1990) or its updated version (Robertson, 2009) would be more  
65 appropriate as it allows one to distinguish between normally consolidated and  
66 overconsolidated soils. After vibratory compaction in Gdynia, the soil is classified as  
67 normally consolidated according to the chart of Robertson (1990) (Figure 33), which is  
68 consistent with a mechanism of vibroflotation where only lateral stress increases. After  
69 dynamic compaction in Gdańsk, however, the soil is classified as overconsolidated (Figure  
70 34). Such soil type behaviour reflects, in the contributors' opinion, the mechanism of dynamic  
71 compaction, where the soil is subjected to dynamic contact vertical stress induced by the  
72 pounder impact, as estimated by Jessberger and Beine (1981) and Mayne and Jones (1983).  
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**Figure 33.** Robertson 1990 chart for soil treated by vibroflotation, Gdynia, Poland, Bałachowski and Kurek (2015).  $\phi'$ , angle of internal friction;  $S_t$ , sensitivity



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**Figure 34.** Robertson 1990 chart for soil treated by dynamic compaction, Gdańsk, Poland, Kurek and Bałachowski (2015)

## 87 Authors' reply

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### 1. Introduction

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In the paper under discussion (Massarsch et al., 2020) five case histories were investigated, which all showed that the sleeve resistance,  $f_s$  (CPT), and horizontal stress index,  $K_D$  (DMT), increased independently of the compaction method. The paper demonstrates that permanent changes in horizontal stress do occur as a result of deep vibratory compaction. An important aspect of the proposed approach is that, when assessing preloading, data interpretation should be based on changes of soil parameters rather than on single values after the completed compaction effort. The critique offered by the contributors can be summarised in the following three points.

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- (a) Changes in sleeve resistance (CPT) or horizontal stress index (DMT) do not reflect changes in horizontal effective stress.
- (b) The strong variation of the OCR shows that the authors' proposed horizontal stress concept is incorrect.
- (c) An increase in horizontal effective stress cannot be related to a preloading ('overconsolidation') effect.

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In the authors' opinion, these three points are based on conjecture rather than factual evidence and do not address the fundamental and widely accepted concepts presented in the paper.

109 Rather, they focus on the fact that the interpretation of field data, in some cases, produces a  
110 large scatter.

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## 112 **2. Questionable quality of geotechnical data**

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114 Two of the contributors were co-authors of two of the case histories (Gdańsk and Gdynia)  
115 cited in the original paper. The case history presented by Kurek and Bałachowski (2015)  
116 (CPTU/DMT control of heavy tamping compaction of sands) describes the application of  
117 dynamic compaction (heavy tamping) to treat loose to medium dense sand layers and states  
118 that ‘the cone penetration test CPTU and the dilatometer test DMT were used as main tools of  
119 compaction control’ (Kurek and Bałachowski, 2015, 2015: p. 2). The case history presented  
120 by Bałachowski and Kurek (2015) (Vibroflotation control of sandy soils using DMT and  
121 CPTU) describes the application of vibroflotation. However, although the titles of both case  
122 histories mention CPTU, the papers omit pore water pressure measurements. Also, the depths  
123 to groundwater tables are missing. While CPTU and DMT investigations were carried out at  
124 three locations prior to compaction and after compaction, respectively, only the results of one  
125 CPT and one DMT before and after treatment are reported. The absence of these  
126 measurements may be the cause of the scatter of the OCR values derived from the Gdańsk  
127 and Gdynia case histories.

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129 In addition, in the paper by Bałachowski and Kurek (2015) only reports test data for one CPT  
130 without pore pressure measurement and one DMT. Vibroflotation causes strong lateral  
131 vibrations and the ensuing increase of horizontal stress is evident from the strong increase in  
132  $K_D$  measurements. It would be unreasonable to accept that  $f_s$  would decrease while  $K_D$  would  
133 increase. Therefore, the authors’ interpretation is that the  $f_s$  data are erroneous and that  $f_s$   
134 actually increased, similar to  $K_D$ .

135

136 When interpreting geotechnical data from the case histories, the authors did not comment on  
137 the accuracy of the reported data. Despite our concern regarding the quality of the two case  
138 histories mentioned, due to the large amount of other data from other cited cases, the authors’  
139 general conclusion was that horizontal stresses increased in all the case histories, independent  
140 of the compaction method. In the following, the points raised by the contributors will be  
141 addressed in the order made. The text from the discussion is quoted, followed by the authors’  
142 response.

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## 144 **3. Response to specific comments**

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- 146 ■ The approach of Massarsch et al. (2020) to determine the OCR in compacted soil  
147 based on sleeve friction and lateral stress index seems to be questionable.

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149 The generalised statement ‘seems to be questionable’ is rejected because no factual  
150 information is given as a base to the statement. The paper addresses changes in horizontal  
151 stress due to vibratory compaction. In the authors’ opinion, and substantiated by a large  
152 number of case histories, both sleeve resistance  $f_s$  and horizontal stress index  $K_D$  are sensitive  
153 to changes in horizontal stress and changes measured between before and after compaction do  
154 reflect the preloading effect.

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- 156 ■ In Figures 12 and 24 ... the irregular shape of the OCR with depth and sharp peaks  
157 cannot be physically explained. Moreover, the OCR values based on sleeve friction  
158 and lateral stress index are inconsistent.

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The objective of the paper was not to determine the OCR, but to address horizontal stress increase as measured by CPTs and DMTs. The reason for the variation of OCR in Figures 12 and 24 is due to the fact that, after compaction by vibroflotation,  $f_s$  is reported to have decreased significantly while  $K_D$  increased by a factor of 10 – 15. The authors' conclusion is that the accuracy of both the CPT and DMT measurements of the particular case history (Kurek and Bałachowski, 2015) is questionable, which therefore caused a considerable scatter in the evaluation using the cited records.

- For instance, 14 days after dynamic compaction, the OCR values determined with the lateral stress index (Figure 9) are four to seven times higher than those based on sleeve friction (Figure 7).

Compaction was carried out in granular soil with a low fines content. CPT data (cone resistance  $q_c$  and sleeve resistance  $f_s$ ) show a marked increase 1 day after compaction and only a small increase during the following period. However, the reported DMT ( $K_D$ ) measurements show only a slight increase after 1 day, but a strong increase during the following 13 days.

- Even greater inconsistency in the OCR values determined using CPTU and DMT was shown for vibroflotation (Figures 12 and 14).

As already stated, the sleeve resistance measurements after compaction in the cited case history are questionable (Bałachowski and Kurek, 2015). The contributors stated that 'granular material supply was used from the surface' but did not provide information regarding the added soil volume (Bałachowski and Kurek, 2015: p. 1). It is unreasonable that the friction ratio  $R_f$  would decrease by more than 50%.

- The upper bound of the OCR-based  $K_0$  should correspond to the passive earth pressure coefficient.

Rather than using the OCR, the authors applied the preloading stress margin (the margin between preloading stress and vertical effective stress). This was because the margin is, in effect, the relatively small difference between two larger numbers, which results in uncertainty of the OCR. Moreover, the reported OCR values also reflect the uncertainty (inaccuracy) of the cited geotechnical information.

- Additionally, the use of sleeve friction is generally considered less reliable than the cone resistance, so the proposed correlation (Equation 2) should be used with caution.

The authors agree that sleeve resistance is more prone to variations than cone resistance. However, in the authors' opinion, changes in  $f_s$  reflect changes in horizontal stress better than  $q_c$ . While the accuracy of the absolute value of  $f_s$  can be low, the ratio of sleeve resistance (the ratio of sleeve resistance determined after compaction to that before compaction) is significantly more reliable.

- In the contributors' opinion, it would be better to use the OCR correlations based on combined CPTU and DMT tests, as proposed by Baldi et al. (1986), Monaco et al. (2014) or Marchetti (2015).



209 The use of a combination of CPT and DMT results is potentially useful for determining the  
210 stress history of soil deposits. However, in the case of soil compaction, the authors prefer to  
211 use changes in horizontal stress based on  $f_s$  and  $K_D$  separately. In the case of soil compaction,  
212 the conservative approach is to assume that, prior to treatment, the soil deposit was normally  
213 consolidated.

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- 215 ■ Additionally, Figure 17 seems to be erroneous, as the report of sleeve friction  
216 elaborated using the data from Figure 15 is higher than one at larger depths.

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218 Figure 17 is correct. As stated in the paper under discussion

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220 *... the sleeve resistance down to 5 m depth was unrealistically low and was neglected.*  
221 *Therefore, the pre-compaction sleeve resistance was not used to determine the increase in*  
222 *horizontal stress, as it would give unacceptably high improvement values.*

223

- 224 ■ To estimate the OCR of compacted sand the authors used Equation 12 based on  
225 calibration chamber tests with the soil mass prepared by pluviation and then  
226 mechanically overloaded (Lee et al., 2011). Such a procedure is, however, quite  
227 different to the mechanisms of deep soil vibratory compaction with rearrangement of  
228 grains, prestressing and, finally, the formation of a new soil fabric.

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230 The sample preparation method was described in detail by Choi et al. (2010). Pluviation is a  
231 dynamic deposition process that is particularly intense when trying to achieve a density index  
232 (relative density) exceeding about 60%. After pluviation, the sample was subjected to one  
233 static preloading cycle. If the sample had been subjected to several loading and unloading  
234 cycles, as suggested by the contributors, the preloading effect would have been even more  
235 pronounced. Therefore, the authors' cited data (Lee et al., 2011) actually underestimate the  
236 effect of the preloading.

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238 During vibratory compaction, a soil deposit is subjected to cyclic loading and unloading with  
239 a large number of loading cycles. As stated by Rowe (1954), compaction could be interpreted  
240 as the repeated application and removal of a static surcharge. Rowe suggested that virtually all  
241 peak soil stresses induced by surcharge loading would be retained after surcharge removal.  
242 Based on the concept of cyclic loading during vibratory compaction, Duncan and Seed (1986)  
243 and Symons and Clayton (1992) developed semi-empirical procedures for estimating  
244 horizontal stresses due to vibratory compaction. Rearrangement, in the sense of relative  
245 motion between soil particles, occurs in a similar manner for compaction and preloading.  
246 These considerations also apply to deep compaction of granular soils, a fact that needs to be  
247 recognised, as stated by Massarsch and Fellenius (2002).

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- 249 ■ ... use of the diagram presented by Robertson (1990) or its updated version  
250 (Robertson, 2009) would be more appropriate as it allows one to distinguish between  
251 normally consolidated and overconsolidated soils. After vibratory compaction in  
252 Gdynia, the soil is classified as normally consolidated according to the chart of  
253 Robertson (1990) (Figure 33), which is consistent with a mechanism of vibroflotation  
254 where only lateral stress increases. After dynamic compaction in Gdańsk, however,  
255 the soil is classified as overconsolidated (Figure 34).

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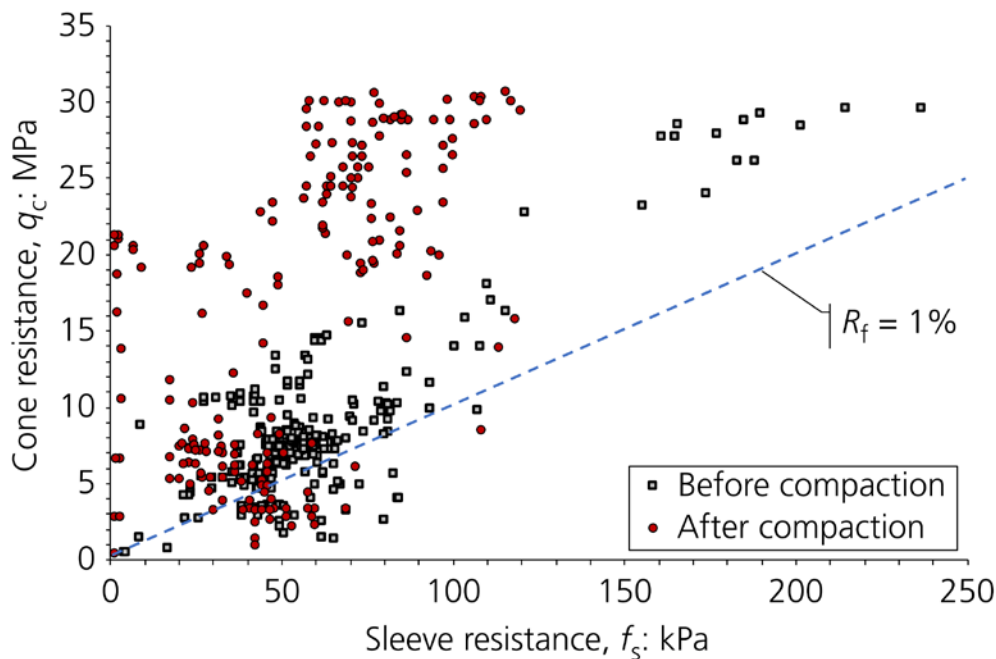
257 The reliability of soil behaviour type (SBT) charts depends on the accuracy of sleeve  
258 resistance measurements. However, soil compaction significantly changes horizontal stresses



259 and thus sleeve resistance, which is demonstrated by the case histories presented in the paper  
260 under discussion. Normalised SBT charts apply absolute values of cone resistance and sleeve  
261 resistance, which disguises the effect of the rearrangement of the soil fabric, easily leading to  
262 erroneous conclusions (e.g. the soil type would have changed as a result of compaction).

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264 Vibroflotation Gdynia: according to the normalised SBT chart provided by the contributors  
265 (Figure 33), the soil category changed, but the soil deposit remained normally consolidated.  
266 However, this conclusion is, in the authors' opinion, due to inaccurate sleeve resistance  
267 measurements. This effect is illustrated in Figure 35, where the same data are plotted in a non-  
268 normalised diagram, as suggested by Massarsch and Fellenius (2002).

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273 **Figure 35.** Linear chart of cone resistance against sleeve resistance. Evaluation of soil treated  
274 by vibroflotation, Gdynia Poland (Bałachowski and Kurek, 2015). For ease of evaluation, the  
275 friction ratio  $R_f = 1\%$  is indicated

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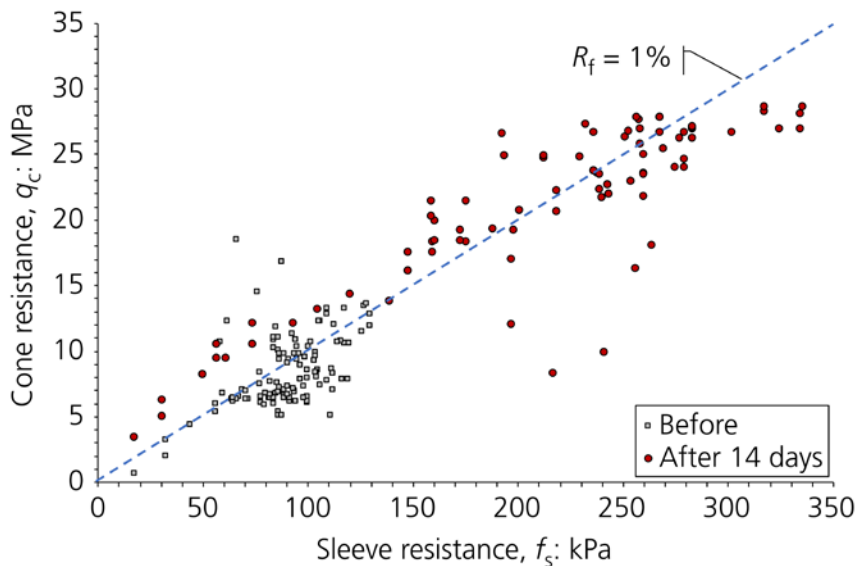
277 The authors agree with the contributors that horizontal stresses increase as a result of  
278 vibroflotation. Therefore, it is difficult to follow their assertion, that  $f_s$  – which is sensitive to  
279 horizontal stress changes (as is  $K_D$ ) – would decrease by more than 50%. From Figure 35, it  
280 would appear that  $f_s$  would decrease in the denser soil layers. This conjecture is contrary to  
281 extensive experience published in the literature. For instance, Howie et al. (2000) analysed the  
282 effect of vibro-replacement in a sandy soil, similar to the method described by the  
283 contributors. Different types of in situ tests were used to evaluate the compaction effect.  
284 Testing comprised seismic CPTs, full displacement pressuremeter tests and resistivity CPTs.  
285 The CPT data showed that, after treatment, both the cone resistance and the sleeve resistance  
286 increased markedly. Howie et al. (2000) concluded

287

288 *After ground treatment, changes were observed in tip resistance, pore pressure response,*  
289 *shear wave velocity, the characteristics of pressuremeter curves and bulk resistivity. Some of*  
290 *these changes can be caused by changes in lateral stress as well as by density increases.*

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 292 Dynamic compaction, Gdańsk: the results from the Gdańsk case history where dynamic  
 293 compaction was used are replotted in a linear chart of cone resistance against sleeve resistance  
 294 in Figure 36. Figure 36 clearly shows the effect of the soil treatment. The soil type (friction  
 295 ratio) remained approximately unchanged. However,  $q_c$  and  $f_s$  increased by approximately by  
 296 the same degree. It is obvious from the concepts outlined in the original paper that the treated  
 297 soil deposit had become preloaded. The contributors are referred to publications that discuss  
 298 the limitation of using SBT charts in connection with vibratory compaction (e.g. Asalemi,  
 299 2006; Howie et al., 2000; Nguyen et al., 2014). Nguyen et al. (2014: p. 1120) studied the  
 300 effect of vibratory compaction (vibroflotation with the addition of granular material from the  
 301 ground surface) on the interpretation of SBT charts, when used for liquefaction evaluation.  
 302 They showed that, after treatment, the in situ horizontal effective stresses were significantly  
 303 increased. They concluded the following.

304  
 305 *The NCEER 1997 CPT-based liquefaction analysis uses the CPT Soil Behavior Type Index,*  
 306  *$I_c$ , to infer grain characteristics, such as fines content and plasticity of fines. However, after*  
 307 *vibratory ground improvement, the in situ horizontal effective stresses are typically increased*  
 308 *(i.e. higher  $K_0$ ) and are no longer linked to vertical effective stress in the same manner as the*  
 309 *case histories. This change in  $K_0$  has an influence on the CPT results and can result in a*  
 310 *reduction of the measured  $I_c$  value, and a corresponding decrease of apparent fines content.*  
 311 *However, it is impossible for the vibratory compaction process to produce a decrease in fines*  
 312 *content. The authors have performed extensive CPT, SPT, and soil sampling during recent*  
 313 *vibro-replacement (stone column) projects in southern California. The  $I_c$  values and fine*  
 314 *contents of the soil were compared before and after ground improvement. The authors*  
 315 *propose a correction method in order to compensate for the shift in  $I_c$  and to maintain the*  
 316 *same fines content in the pre- and the post-treatment CPT based liquefaction analyses.*  
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 320 **Figure 36.** Linear chart of cone resistance against sleeve resistance. Evaluation of soil treated  
 321 by dynamic compaction, Gdańsk, Poland (Kurek and Bałachowski, 2015). For ease of  
 322 evaluation the friction ratio  $R_f = 1\%$  is indicated  
 323



324       ▪ Such soil type behaviour reflects, in the contributors' opinion, the mechanism of  
325 dynamic compaction, where the soil is subjected to dynamic contact vertical stress  
326 induced by the poulder impact, as estimated by Jessberger and Beine (1981) and  
327 Mayne and Jones (1983). The statement is based on conjecture rather than scientific  
328 evidence. As demonstrated in the original paper, showing stress changes as a result of  
329 different soil compaction methods, all types of vibratory compaction cause a  
330 permanent increase in horizontal stress. For a more detailed description of the  
331 vibratory compaction process and thereby induced stress changes, reference is made  
332 to, for instance, Duncan and Seed (1986), who state The compaction of soil represents  
333 a process of load application and removal which can result in significant increases in  
334 residual lateral earth pressure. Several theories and analytical methods have been  
335 proposed to explain and/or analyse the residual lateral earth pressures induced by soil  
336 compaction. Common to all of these is the idea that compaction represents a form of  
337 overconsolidation wherein stresses resulting from a temporary or transient loading  
338 condition are retained to some extent following removal of this peak load.

## 339 REFERENCES

340  
341 Asalemi AA (2006) Application of Seismic Cone for Characterization of Ground Improved  
342 by Vibro-Replacement. Doctoral thesis, University of British Columbia, Vancouver, BC,  
343 Canada.

344  
345 Bałachowski L and Kurek N (2015) Vibroflotation control of sandy soils using DMT and  
346 CPTU. In Proceedings of the 3rd International Conference on the Flat Dilatometer (DMT 15),  
347 Rome, Italy (Marchetti S (ed.)). International Society for Soil Mechanics and Geotechnical  
348 Engineering, London, UK.

349  
350 Baldi G, Bellotti R, Ghionna V et al. (1986) Flat dilatometer tests in calibration chambers. In  
351 Proceedings of In Situ '86 ASCE Specialty Conference on Use of In Situ Tests in  
352 Geotechnical Engineering (Clemence SP (ed.)). ASCE, Reston, VA, USA. Special  
353 Publication 6, pp. 431 – 446.

354  
355 Choi SK, Lee MJ, Choo HW, Tumay MT and Lee WJ (2010) Preparation of a large size  
356 granular specimen using a rainer system with a porous plate. Geotechnical Testing Journal  
357 33(1) : 1 – 10. Duncan JM and Seed RB (1986) Compaction-induced earth pressures under K  
358 0-conditions. Journal of Geotechnical Engineering ASCE 112(1) : 1 – 22.

359  
360 Howie JA, Daniel JA, Asalemi AA and Campanella RG (2000) -Combinations of in situ tests  
361 for control of ground modification in silts and sands. In Geo-Denver 2000, Denver, CO, USA.  
362 American Society of Civil Engineers, Reston, VA, USA.

363  
364 Jessberger HL and Beine RA (1981) Heavy tamping: theoretical and practical aspects.  
365 Proceedings of the 16th International conference on Soil Mechanics and Geotechnical  
366 Engineering. IOS Press, Amsterdam, the Netherlands, vol. 3, pp. 695 – 699.

367  
368 Kurek N and Bałachowski L (2015) CPTU/DMT control of heavy tamping compaction of  
369 sands. In Proceedings of the 3<sup>rd</sup> International Conference on the Flat Dilatometer (DMT 15),  
370 Rome, Italy (Marchetti S (ed.)). International Society for Soil Mechanics and Geotechnical  
371 Engineering, London, UK.

372  
373



- 374 Lee M, Choi S, Kim M and Lee W (2011) Effect of stress history on CPT and DMT results in  
375 sand. *Engineering Geology* 117(3–4) : 259 – 265.  
376
- 377 Marchetti S (2015) Some 2015 updates to the TC16 DMT report 2001. In *Proceedings of the*  
378 *3rd International Conference on the Flat Dilatometer (DMT 15)*, Rome, Italy (Marchetti S  
379 (ed.)). International Society for Soil Mechanics and Geotechnical Engineering, London, UK.  
380
- 381 Massarsch KR and Fellenius BH (2002) Vibratory compaction of coarse-grained soils.  
382 *Canadian Geotechnical Journal* 39(3) : 695 – 709.  
383
- 384 Massarsch KR, Wersäll C and Fellenius BH (2020) Horizontal stress increase induced by  
385 deep vibratory compaction. *Proceedings of the Institution of Civil Engineers – Geotechnical*  
386 *Engineering* 173(3) : 228 – 253, <https://doi.org/10.1680/jgeen.19.00040>.  
387
- 388 Mayne PW and Jones JS (1983) Impact stresses during dynamic compaction. *Journal of*  
389 *Geotechnical Engineering ASCE* 109(6) : 1342 – 1346.  
390
- 391 Monaco P, Amoroso S, Marchetti S et al. (2014) Overconsolidation and stiffness of Venice  
392 lagoon sands and silts from SDMT and CPTU. *Journal of Geotechnical and*  
393 *Geoenvironmental Engineering ASCE* 140(1) : 215 – 227,  
394 [https://doi.org/10.1061/\(ASCE\)GT.1943-5606.0000965](https://doi.org/10.1061/(ASCE)GT.1943-5606.0000965) .  
395
- 396 Nguyen TV, Shao L, Gingery J and Robertson P (2014) Proposed modification to CPT-based  
397 liquefaction method for post-vibratory ground improvement. In *Proceedings of the ASCE*  
398 *Geo-Congress 2014 Technical Papers: Geo-Characterization and Modeling for Sustainability*  
399 (Abu-Farsakh M, Yu X and Hoyos LR). ASCE, Reston, VA, USA, pp. 1120 – 1132.  
400
- 401 Robertson PK (1990) Soil classification using the cone penetration test. *Canadian*  
402 *Geotechnical Journal* 27(1) : 151 – 158, <https://doi.org/10.1139/t90-014> .  
403
- 404 Robertson PK (2009) Interpretation of cone penetration tests – a unified approach. *Canadian*  
405 *Geotechnical Journal* 46(11) : 1337 – 1355, <https://doi.org/10.1139/T09-065>.  
406
- 407 Robertson PK, Campanella RG, Gillespie D and Greig J (1986) Use of piezometer cone data.  
408 In *In-Situ '86 Use of In-situ testing in Geotechnical Engineering*, GSP 6, ASCE, Reston, VA,  
409 USA, Specialty Publication, SM 92, pp. 1263 – 1280.  
410
- 411 Rowe PW (1954) Stress – strain theory for cohesionless soil with applications to earth  
412 pressures at rest and moving walls. *Géotechnique* 4(2) : 70 – 88,  
413 <https://doi.org/10.1680/geot.1954.4.2.70> .  
414
- 415 Symons IF and Clayton CRI (1992) Earth pressures on backfilled retaining walls. *Ground*  
416 *Engineering* 26(3) : 26 – 34.

