

Article

Effect of Temperature and Nanoparticle Concentration on Free Convective Heat Transfer of Nanofluids

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Abstract: A theoretical analysis of the influence of temperature and nanoparticle concentration on free convection heat transfer from a horizontal tube immersed in an unbounded nanofluid was presented. The Nusselt (Nu) number and heat transfer coefficient were parameters of the intensity of the convective heat transfer. For free convection, the Nu number was a function of the Rayleigh (Ra) number and Prandtl (Pr) number. The Rayleigh (Ra) number and Prandtl (Pr) number were functions of the thermophysical properties of nanofluids. The thermophysical properties of nanofluids varied with temperature and nanoparticle concentration. Therefore, an analysis was conducted to evaluate the effects on the performance of nanofluids due to variations of thermal conductivity, viscosity, thermal expansion, density, and specific heat, which are functions of nanoparticle concentration and temperature. Water- and ethylene glycol (EG)-based nanofluids with dispersed alumina (Al₂O₃) nanoparticles at mass concentrations of 0.01%, 0.1%, and 1% were considered. Calculated Nu numbers and heat transfer coefficients were compared with experimental values taken from the published literature.



Citation: Cieśliński, J.T.; Smolen, S.; Sawicka, D. Effect of Temperature and Nanoparticle Concentration on Free Convective Heat Transfer of Nanofluids. *Energies* **2021**, *14*, 3566. <https://doi.org/10.3390/en14123566>

Received: 20 May 2021
Accepted: 14 June 2021
Published: 15 June 2021

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Keywords: nanofluids; thermophysical properties; free convective heat transfer; horizontal cylinder

1. Introduction

A nanofluid is a suspension consisting of a base liquid and metallic or non-metallic nanoparticles with sizes significantly smaller than 100 nm. Despite the small amount of nanoparticles from a few ppm to several percent of volume or mass concentration, the nanofluids exhibit completely different thermophysical properties compared to the base fluids. As a result, distinct heat transfer enhancement can be observed. Of particular interest is single phase convective heat transfer due to potential applications in many cooling systems [1–4].

Contrary to forced convection heat transfer, e.g., [5–7], little attention has been paid to study free convection of nanofluids. Khanafer et al. [8] numerically stated that the application of nanofluid during free convection in a 2D enclosure substantially enhances heat transfer. Putra et al. [9] experimentally studied free convection of water-Al₂O₃ and water-CuO nanofluids inside a horizontal cylinder with heated and cooled end covers. A systematic decrease in heat transfer with the increasing volume concentration of nanoparticles was noted. Wen and Ding [10] experimentally found out that the addition of nanoparticles to base fluid leads to an increase in the thermal conductivity and viscosity of nanofluids. However, a decrease in the Nu number and Ra number was observed, and it was difficult to establish relative importance of the thermal conductivity and viscosity of nanofluids. Polidori et al. [11] studied theoretically free convection over a vertical plate. They pointed out the role of viscosity in free convection heat transfer of nanofluids. Ho et al. [12] investigated experimentally free convection in vertical enclosure. They established substantial

enhancement of heat transfer even for nanofluids with low nanoparticle concentration. Li and Peterson [13] studied experimentally free convection inside a cylindrical gap heated from below. The gradual deterioration of heat transfer coefficient was observed with the increase in the volume fraction of the nanoparticles in the nanofluids. Mahrood et al. [14] conducted experiments with non-Newtonian fluids. Experiments were carried out in vertical cylinders. The dependence of nanoparticle concentration and aspect ratio enhancement or deterioration of heat transfer was observed. Ciesliński and Krygier [15] recorded substantial deterioration of heat transfer during free convection of nanofluids from horizontal porous coated tubes. Garbadeen et al. [16] studied experimentally free convection of water-MWCNT nanofluids in a square enclosure with differentially heated side walls. Substantial enhancement of heat transfer was observed for optimum nanoparticle volume concentration of 0.1%. Rahimi et al. [17] investigated experimentally and numerically free convection heat transfer of water-DMCNT nanofluids in a cuboid enclosure. For nanoparticle concentrations higher than 0.01%, a decrease in the Nu number and average heat transfer coefficient was noted. Minea and Lorenzini [18] found out numerically that during free convection of water-ZnO nanofluids in a rectangular enclosure, the Nu number decreases and the entropy generation increases with the increase in Ra number. Reddy and Chamkha [19] studied numerically the influence of buoyancy and Brownian motion on heat transfer from a horizontal cylinder placed in a porous medium filled with nanofluid. Guestral et al. [20] investigated numerically the free convection of water-Cu and water-TiO₂ nanofluids in a partially heated horizontal cylindrical enclosure. The study showed improvement of heat transfer as the Ra number increased. Moreover, the Nu number increased with the increasing nanoparticle concentration. Sawicka et al. [21] established numerically that the increase in nanoparticle concentration leads to a decrease in Nu number, Ra number, and an increase in the heat transfer coefficient during free convection of nanofluids from a horizontal cylinder.

Existing correlations for the free convection heat transfer of nanofluids [9–11] relate the Nusselt (Nu) number only to Ra number: $Nu = f(Ra)$. As it was demonstrated in [22], the Nu number is not only a function of Ra, but the Pr number as well: $Nu = f(Ra, Pr)$. Therefore, for nanofluids, a more accurate correlation equation would be: $Nu = f(Ra, Pr, \varphi)$. It is well known that thermophysical properties of nanofluids are dependent upon nanoparticle concentration and temperature [23–25]. However, the change of specific heat and density of nanofluids with nanoparticle concentration and temperature is modest [26–29]. The thermal conductivity of nanofluids increases moderately with an increase in temperature and nanoparticle concentration [30–32]. The viscosity of nanofluids, in turn, decreases substantially with an increase in temperature and increases with an increase in nanoparticle concentration [33–35]. Therefore, it is very difficult to evaluate the relative importance of viscosity and thermal conductivity. However, as the Nu number increases with an increase in Prandtl number, it is interesting to question the impact of temperature and nanoparticle concentration on Pr number variation. A key parameter in free convection heat transfer is the thermal expansion coefficient, and it was experimentally established [12] that the thermal expansion coefficient for water-Al₂O₃ nanofluids increases substantially with an increase in temperature, and the change with nanoparticle concentration is modest. Khanafer and Vafai [23] demonstrated that literature correlations have not properly estimated the thermal expansion coefficient of water-Al₂O₃ nanofluids when compared to the experimental data of Ho et al. [12]. Therefore, using the experimental data of Ho et al. [12], they proposed a new correlation as a function of nanoparticle concentration and temperature jointly.

In this paper, according to the best author's knowledge, for the first time, a theoretical analysis was carried out on water-Al₂O₃ and EG-Al₂O₃ nanofluids to determine the influence of temperature and nanoparticle concentration on thermophysical properties of nanofluids, and as a consequence, on Pr number variation, Ra number variation, Nu number variation, and heat transfer coefficient variation. Because the Ra number, Nu number, and consequently, the heat transfer coefficient, are functions of the characteristic



length, it was necessary to define geometry of the thermal system. In the present study, free convection heat transfer from a horizontal tube immersed in an unbounded nanofluid was analyzed. Alumina nanoparticles (Al_2O_3) were considered at the concentration of 0.01%, 0.1%, and 1% by weight within the temperature range 20–40 °C. The range of the considered parameters was selected the same as in experimental study presented in [36]; therefore, a comparison of the calculated values of Nu numbers and heat transfer coefficients with experimental results was conducted.

2. Materials and Methods

2.1. Correlations for Free Convection Heat Transfer from Horizontal Cylinders

For free convection heat transfer of the base fluids, the Nusselt number was calculated from the recognized Churchill and Chu correlation equation [37].

$$\text{Nu} = \left(0.6 + \frac{0.387 \cdot \text{Ra}^{\frac{1}{6}}}{\left[1 + \left(\frac{0.559}{\text{Pr}} \right)^{\frac{9}{16}} \right]^{\frac{8}{27}}} \right)^2 \quad (1)$$

which is valid for all Ra numbers and Pr numbers. The correlation served for prediction of the referenced heat transfer coefficient.

Contrary to forced convection heat transfer, e.g., [38–41], few correlations exist for free convection heat transfer, and these are mostly devoted to heat transfer in enclosures [42].

Recently, Habibi et al. [43] numerically developed correlation equations for laminar free convection heat transfer of water- Al_2O_3 nanofluids from an isolated, horizontal cylinder as follows:

$$\text{Nu} = \left(0.4667 + 0.1213 \varphi_v^{0.6817} \right) \text{Ra}^{1/4} \quad (2)$$

$$\text{Nu} = \left(0.4667 - 1.0761 \varphi_v^{1.35014} \right) \text{Ra}^{1/4} \quad (3)$$

which is valid for $10 \leq \text{Ra} \leq 10^6$ and $(0\% < \varphi_v < 20\%)$.

Sawicka et al. [36] proposed an experimentally developed correlation equation for free convection heat transfer of water- Al_2O_3 , EG- Al_2O_3 , and water/EG- Al_2O_3 nanofluids from an isolated, horizontal cylinder in the form:

$$\text{Nu} = 0.63 \text{Ra}^{0.23} \cdot \text{Pr}^{0.053} \cdot (1 - \varphi_m)^{2.64} \quad (4)$$

which is valid for $3 \times 10^4 \leq \text{Ra} \leq 1.3 \times 10^6$ and $0.01\% < \varphi_m < 1\%$.

2.2. Analyzed Nanofluids

In this theoretical study, the same base fluids and nanoparticles were considered as used in [36], where distilled, deionized water and EG served as base fluids, and Al_2O_3 were used as nanoparticles. Alumina nanoparticles were examined at the concentration of 0.01%, 0.1%, and 1% by weight. The mean diameter of nanoparticle was equal to $d_p = 47$ nm.

The properties of alumina (Al_2O_3) nanoparticles are shown in Table 1.

Table 1. Properties of Al_2O_3 nanoparticles.

Density [44] ρ_p [kg/m ³]	Specific Heat [44] c_{pp} [J/(kg K)]	Thermal Conductivity [45] k_p [W/(mK)]	Thermal Expansion Coefficient [12] β_p [1/K]
3600	765	35	8.46×10^{-6}

2.3. Correlations for Thermophysical Properties of Nanofluids

A large number of correlations devoted to calculating viscosity of nanofluids is published in the literature, e.g., [46,47]. Corcione [48] proposed following correlation equation for viscosity of the water-Al₂O₃ and EG-Al₂O₃ nanofluids:

$$\mu_{nf} = \mu_{bf} \left(\frac{1}{1 - 34.87 \left(\frac{d_p}{d_f} \right)^{-0.3} \varphi_v^{1.03}} \right) \quad (5)$$

where d_f is the equivalent diameter of a base fluid molecule:

$$d_f = 0.1 \left(\frac{6M}{N\rho_{f0}} \right)^{1/3} \quad (6)$$

in which M is the molecular weight of the base fluid ($M_{H_2O} = 18$ kg/kmol and $M_{EG} = 62.07$ kg/kmol, $N = 6.02214076 \times 10^{26}$ kmol⁻¹ (Avogadro number), and ρ_{f0} is the density of the base fluid calculated at temperature $T_0 = 293$ K.

Viscosity of the pure water reads [49]:

$$\mu_{bf} = 1.435 \cdot 10^{-5} \cdot e^{\frac{1226.8}{T}} \quad (7)$$

and viscosity of the pure EG reads [49]:

$$\mu_{bf} = 1.6 \cdot 10^{-7} \cdot e^{\frac{3440}{T}} \quad (8)$$

Figure 1 shows the influence of nanoparticle concentration on the viscosity of the tested nanofluids against temperature calculated from Equation (5) for water- and EG-based nanofluids.

As seen in Figure 1, viscosity of the tested nanofluids decreases sharply with temperature increase and slightly increases with nanoparticle mass concentration increase. The maximum increase in viscosity of EG-Al₂O₃ nanofluid with 1% nanoparticle concentration compared to pure EG is 1.1%.

Similarly to viscosity, several correlations devoted to calculating thermal conductivity of nanofluids have been published in literature, e.g., [30,50]. For thermal conductivity of water-Al₂O₃ nanofluids, Sawicka et al. [49] proposed the following correlation equation:

$$k_{nf} = k_{bf} (1 + 0.1046 \varphi_m^{0.2388} (100/d_p)^{3.14 \cdot 10^{-3}}) \quad (9)$$

where thermal conductivity of pure water is:

$$k_{bf} = 1.974 \cdot 10^{-3} \cdot T \quad (10)$$

For EG-Al₂O₃ nanofluids, the experimentally developed correlation is of the form:

$$k_{nf} = k_{bf} \left(1 + 0.0193 \left(\frac{k_p}{k_{bf}} \right)^{6.15 \cdot 10^{-3}} \varphi_m^{0.0738} (100/d_p)^{9.76 \cdot 10^{-5}} \right) \quad (11)$$

where thermal conductivity of pure EG is:

$$k_{bf} = 8.49 \cdot 10^{-4} \cdot T \quad (12)$$

The developed correlations are valid for $0.01\% \leq \varphi_m \leq 1\%$ and $293 \text{ K} \leq T \leq 313 \text{ K}$.

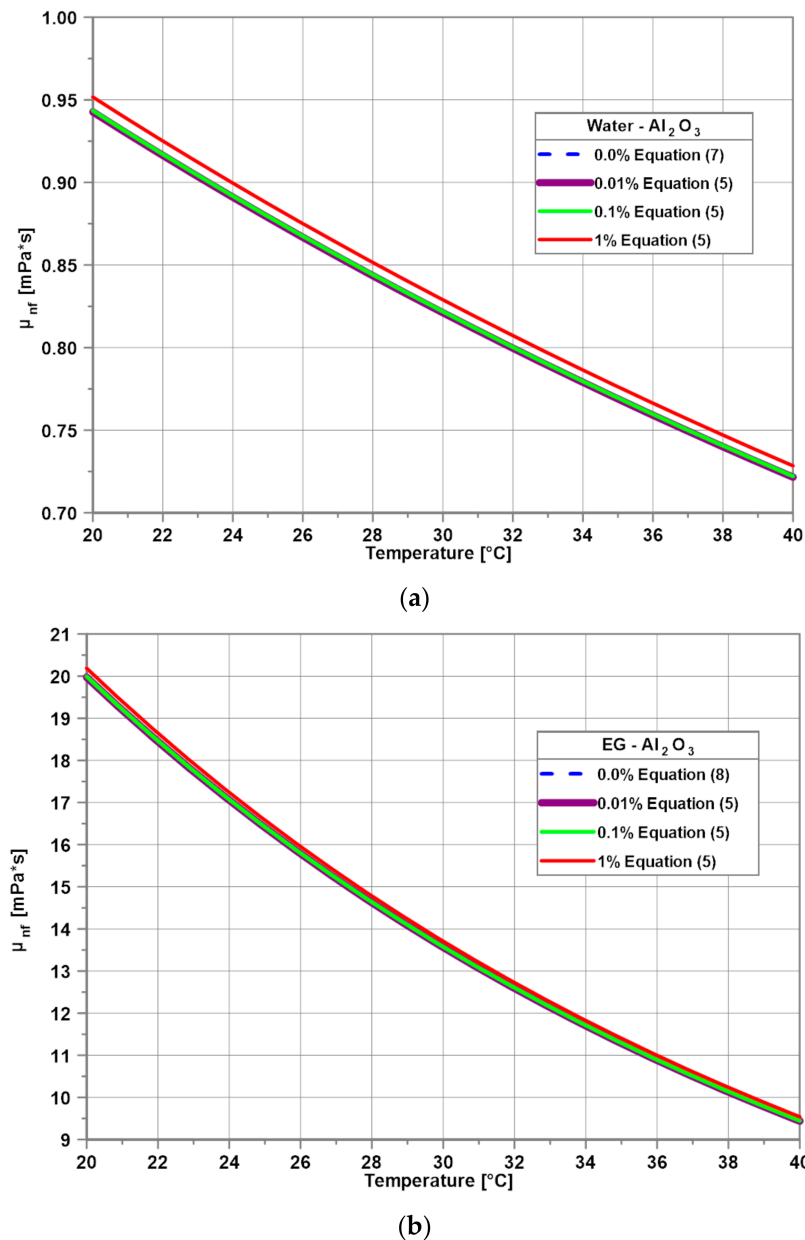


Figure 1. Viscosity of the water-based (a) and EG-based (b) nanofluids.

Figure 2 shows the influence of nanoparticle concentration on the thermal conductivity of the tested nanofluids against temperature calculated from Equations (9) and (11) for water- and EG-based nanofluids, respectively.

As seen in Figure 2, the thermal conductivity of the tested nanofluids increases moderately with the temperature increase and for given temperature increases with nanoparticle concentration increase. Interesting is that the increase in thermal conductivity is more distinct for water-Al₂O₃ and the increase amounts 2.4% within the whole temperature range.

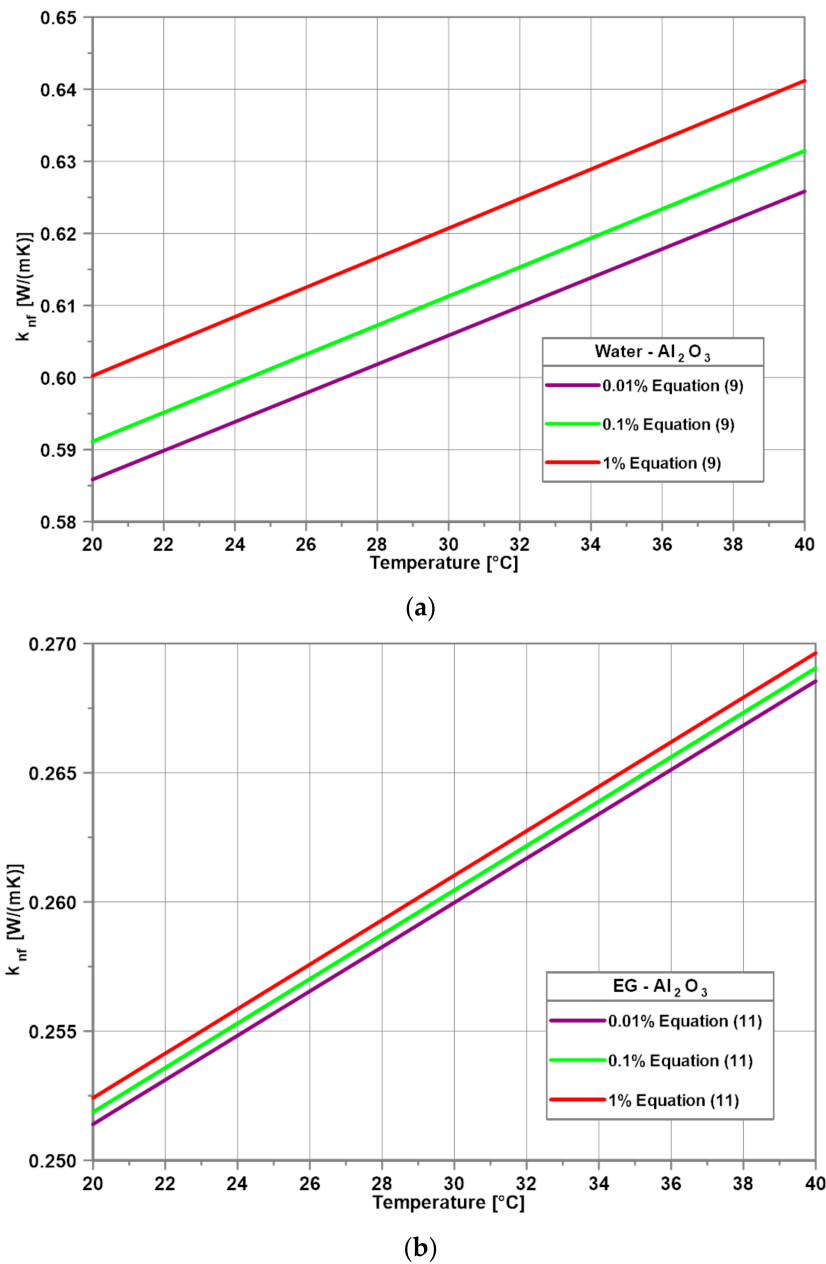


Figure 2. Thermal conductivity of the water-based (a) and EG-based (b) nanofluids.

The commonly accepted equation proposed in [38] was used to estimate the density of the tested nanofluids:

$$\rho_{nf} = \varphi_v \rho_p + (1 - \varphi_v) \rho_{bf} \quad (13)$$

where density of pure water and pure EG is given by the Equations (14) and (15), respectively:

$$\rho_{bf} = 1107.6 - 0.3708 \cdot T \quad (14)$$

$$\rho_{bf} = 1331.2 - 0.732 \cdot T \quad (15)$$

Equations (14) and (15) are based on the data provided by the ASHRAE Handbook [51]. Figure 3 illustrates the influence of the nanoparticle concentration on the density of the tested nanofluids as a function of temperature calculated from Equations (13)–(15).

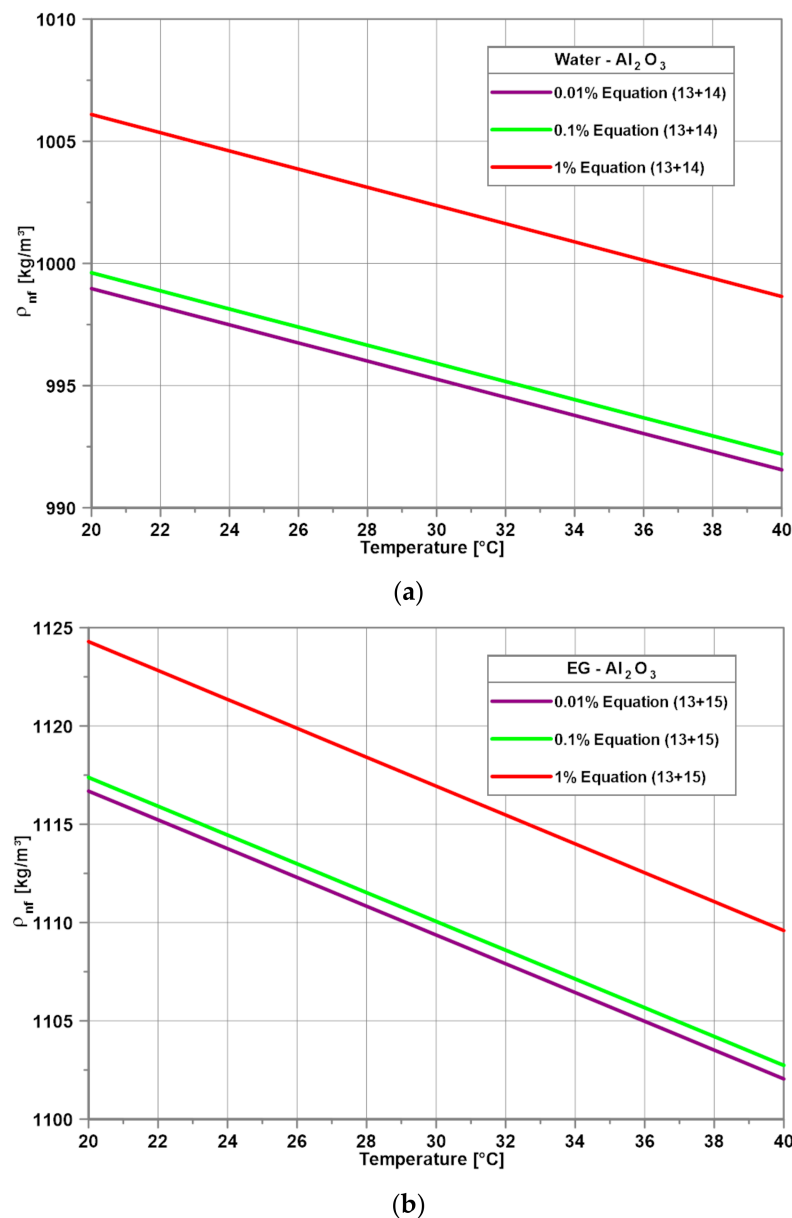


Figure 3. Density of the water-based (a) and EG-based (b) nanofluids.

As seen in Figure 3, the density of the analyzed nanofluids decreases with the temperature increase and increases with the nanoparticle concentration increase because the density of the nanoparticle material (Table 1) is higher than the density of pure water or pure EG.

In order to calculate the specific heat of the tested nanofluids, the correlation equation proposed in [44] was used:

$$c_{pnf} = \frac{(1 - \varphi_v)\rho_{bf}c_{pbf} + \varphi_v\rho_p c_{pp}}{\rho_{bf}} \quad (16)$$

where the specific heat of pure water and pure EG is given by the Equations (17) and (18), respectively:

$$c_{pbf} = 5603 - 9.2129 \cdot T + 0.0149 \cdot T^2 \quad (17)$$

$$c_{pbf} = 1062.3 + 4.507 \cdot T \quad (18)$$

Equations (17) and (18) are based on the data provided by the ASHRAE Handbook [51]. Figure 4 illustrates the influence of nanoparticle concentration on the specific heat of the tested nanofluids as a function of temperature calculated from Equations (16)–(18).

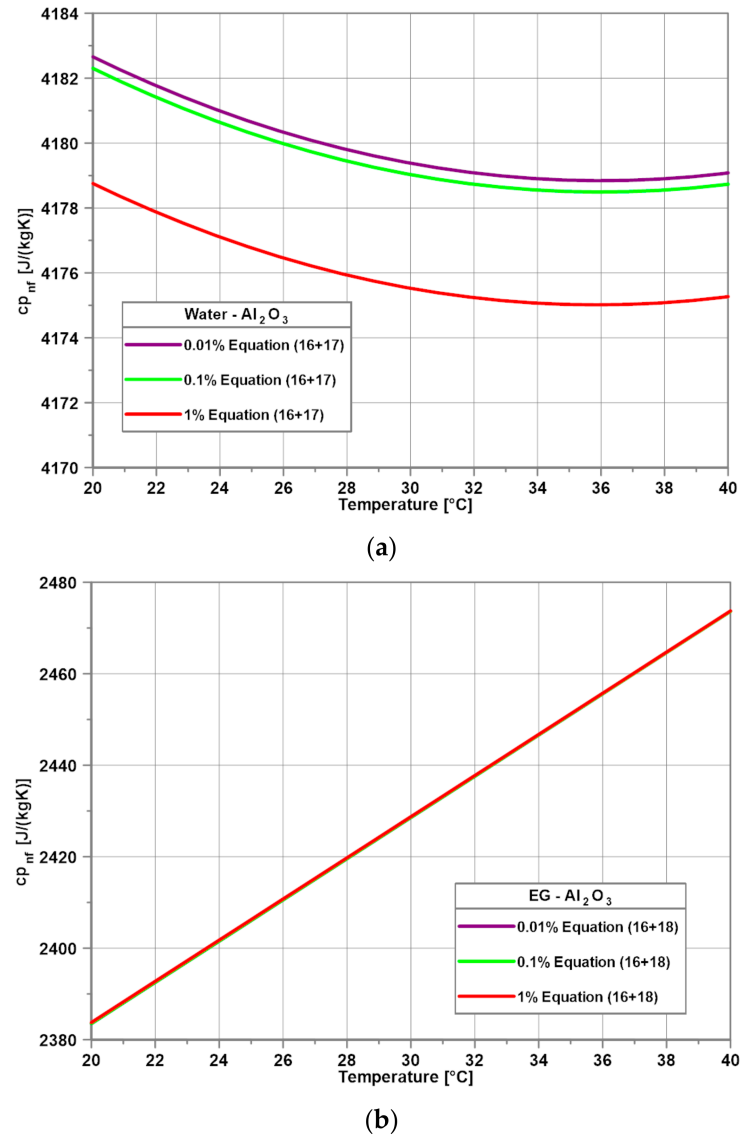


Figure 4. Specific heat of the water-based (a) and EG-based (b) nanofluids.

As seen in Figure 4, the specific heat of water-based nanofluids decreases with the temperature increase and for given temperature decreases with the nanoparticle concentration increase because the specific heat of the nanoparticle material (Table 1) was lower than the specific heat of pure water. It is worthy to note the nonmonotonic course of the specific heat for water-based nanofluids against temperature (Figure 4a) that results from data for pure water. Contrary to water-based nanofluids, the specific heat of EG-based nanofluids increased with temperature increase and was independent on the nanoparticle mass concentration tested.

Thermal expansion coefficient of water-Al₂O₃ nanofluids was determined from the correlation proposed in [23]:

$$\beta_{nf} = \left(-0.479\varphi_v + 9.3158 \cdot 10^{-3}t - \frac{4.7211}{t^2} \right) \cdot 10^{-3} \quad (19)$$

which is valid for $0 \leq \varphi_v \leq 0.04$ and $10 \text{ }^\circ\text{C} \leq t \leq 40 \text{ }^\circ\text{C}$.

For pure water thermal expansion coefficient was calculated from Equation (19) assuming $\varphi_v = 0$, namely:

$$\beta_{bf} = \left(9.3158 \cdot 10^{-3} t - \frac{4.7211}{t^2} \right) \cdot 10^{-3} \quad (20)$$

Thermal expansion coefficient of EG-Al₂O₃ nanofluids was determined from the correlation proposed in [52,53]:

$$\beta_{nf} = (1 - \varphi_v) \beta_f + \varphi_{vp} \quad (21)$$

where the thermal expansion coefficient of pure EG is $\beta_{bf} = 0.00065$ 1/K [54]. Figure 5 illustrates the influence of the nanoparticle concentration on the thermal expansion coefficient of the tested nanofluids as a function of temperature calculated from Equations (19) and (21) for water-Al₂O₃ and EG-Al₂O₃ nanofluids, respectively.

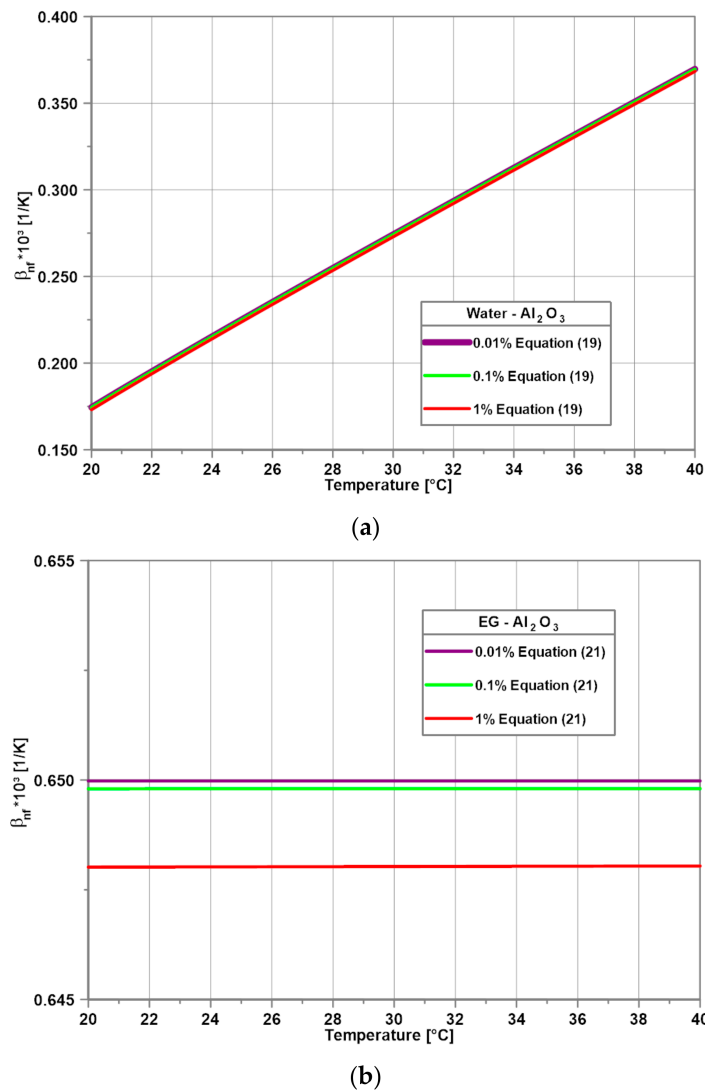


Figure 5. Thermal expansion coefficient of water-based (a) and EG-based (b) nanofluids.

As seen in Figure 5a, the thermal expansion coefficient for water-based nanofluids increases almost linearly with temperature and is independent on the tested mass nanoparticle concentration. For EG-based nanofluids, the thermal expansion coefficient did not depend on the temperature and slightly decreased for the maximum nanoparticle concentration tested.

3. Results

3.1. Variaton of Prandtl Number

Figure 6 shows a comparison of the Pr numbers of the tested water- Al_2O_3 (Figure 6a) and EG- Al_2O_3 (Figure 6b) nanofluids as a function of temperature. For the tested nanofluids, the Pr number decreased with an increase in temperature, predominantly due to the decrease in viscosity (Figure 1). For water- Al_2O_3 nanofluids—independently of mass nanoparticle concentration—the Pr number decreased by about 29% with the temperature increase from 20 to 40 °C. For EG- Al_2O_3 nanofluids—independently of mass nanoparticle concentration—the Pr number decreased by about 55% with the temperature increase from 20 to 40 °C. The decrease in the Pr number with temperature was more distinct for EG- Al_2O_3 nanofluids than in the case of water- Al_2O_3 nanofluids, because of the more significant decrease in viscosity with temperature—Figure 1.

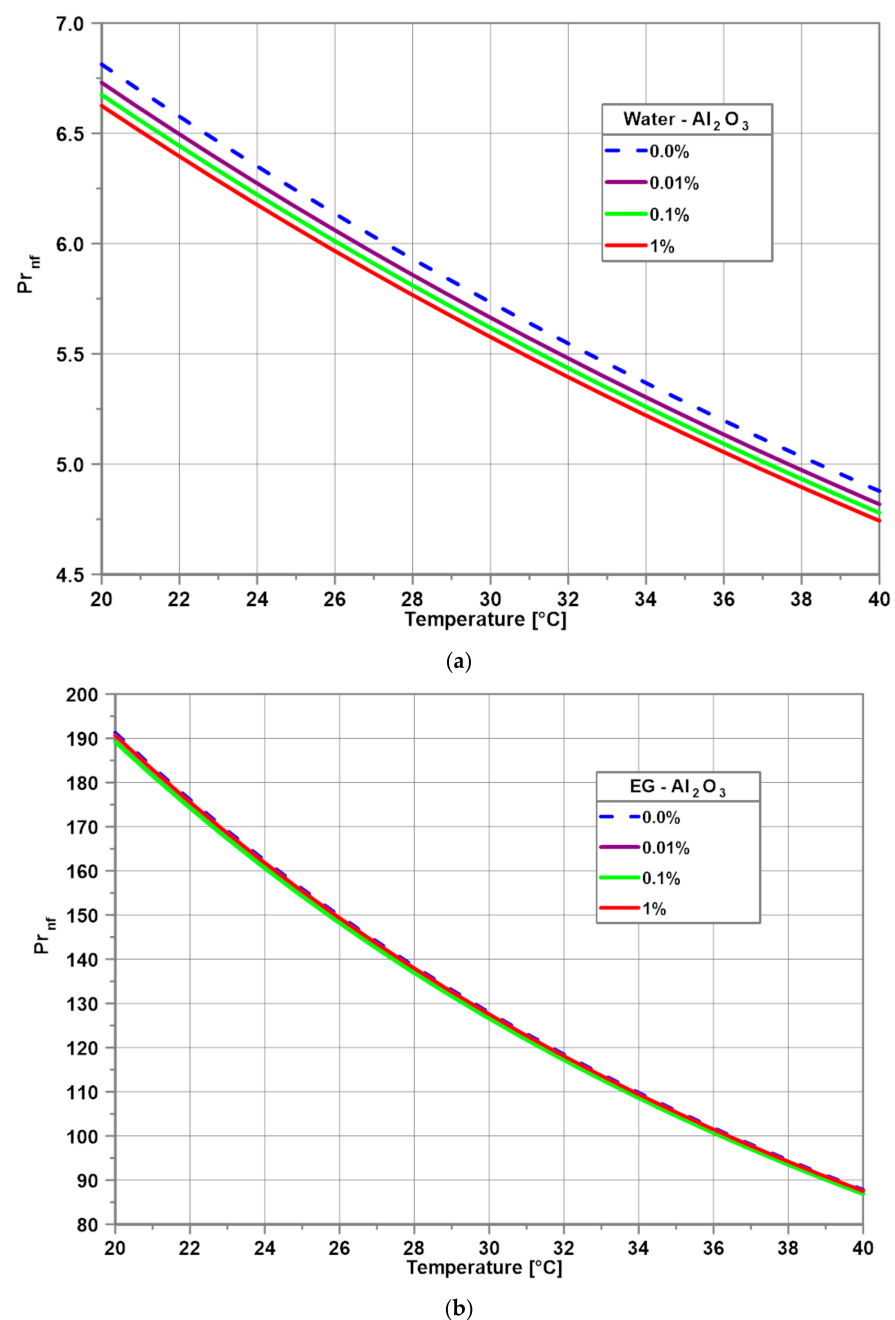
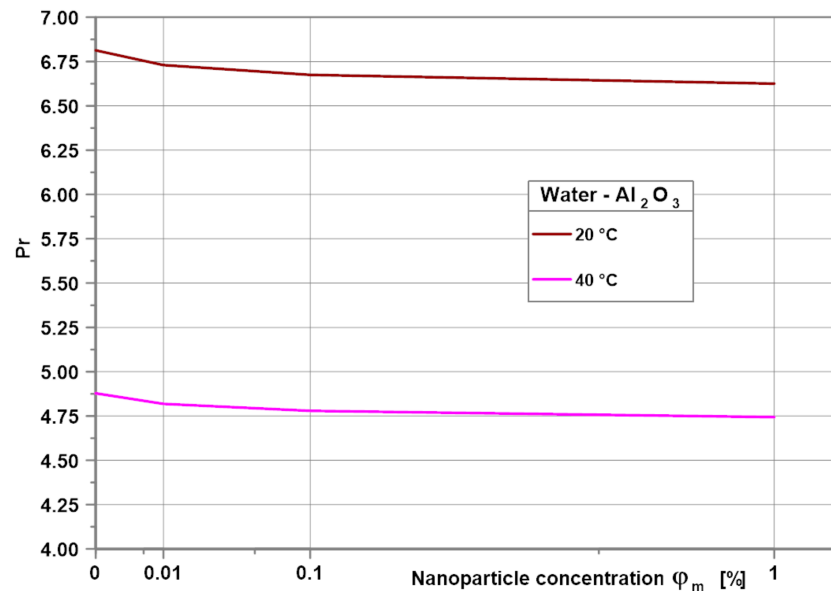
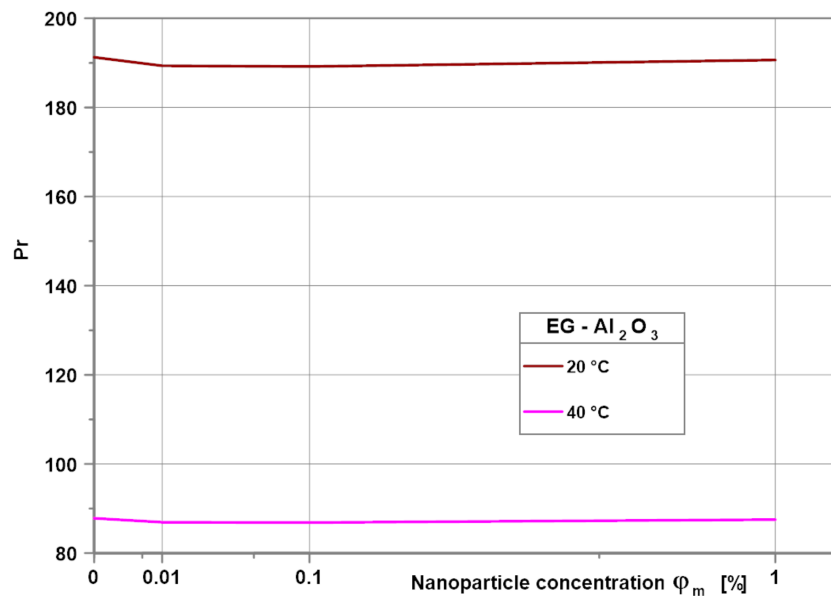


Figure 6. Prandtl number water-based (a) and EG-based (b) nanofluids.

Figure 7 illustrates the influence of nanoparticle mass concentration on the Pr number of the tested nanofluids at two temperatures, namely 20 and 40 °C. As seen in Figure 7a, the Pr number for water- Al_2O_3 decreased slightly with nanoparticle concentration increase. The decrease in the Prandtl number did not depend on temperature and for the nanoparticle mass concentration of 1% equalled 2.7%. For EG- Al_2O_3 nanofluids, the influence of nanoparticle mass concentration on the Pr number was negligible.



(a)



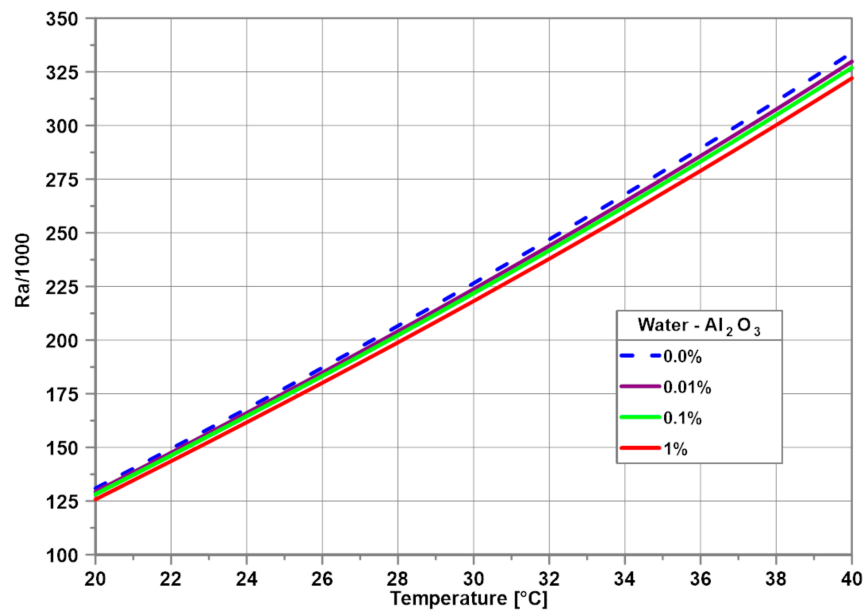
(b)

Figure 7. Variation of Pr number with nanoparticle mass concentration for water-based (a) and EG-based (b) nanofluids.

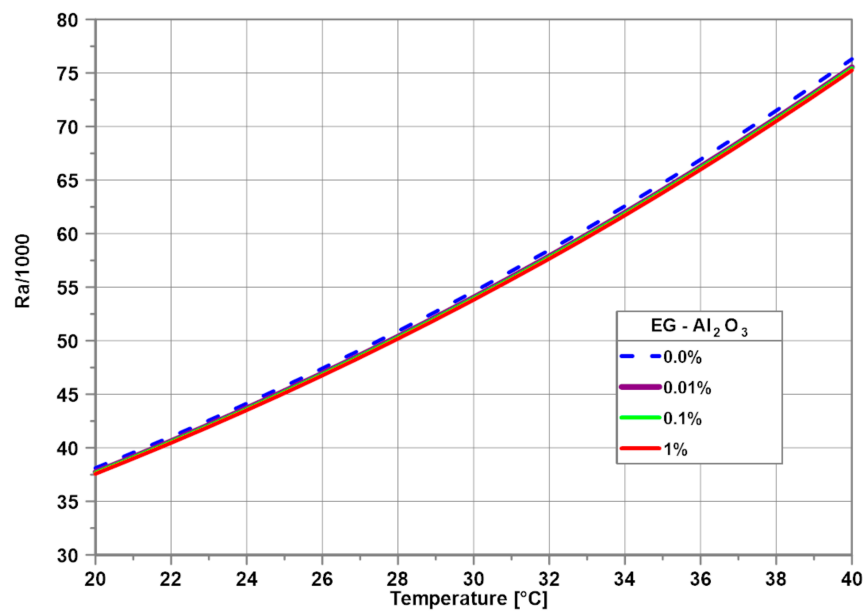
3.2. Variaton of Rayleigh Number

Figure 8 illustrates the change of Ra number versus temperature for the tested nanofluids. In this case the temperature difference and the diameter of the horizontal cylinder are held constant at the values taken from the experiment presented in [36]— $\Delta T = 10$ K, $D = 10$ mm. The Ra number was a function of all discussed thermophysical properties;

however, the most significant parameters were viscosity and thermal expansion coefficient in the case of water based nanofluids (Figure 5a). The Ra number definitively increased with temperature increase, which also resulted in the increase in the Nu number. For water- Al_2O_3 nanofluids and the mass nanoparticle concentration of 0.01%, the Ra number increased by about 162% with the temperature increase from 20 to 40 °C. For EG- Al_2O_3 nanofluids the Ra number increased—independently of mass nanoparticle concentration—by about 106% with the temperature increase from 20 to 40 °C. The increase in the Ra number with temperature was more distinct for water- Al_2O_3 nanofluids than in the case of EG- Al_2O_3 nanofluids, because of the more significant increase in the thermal expansion coefficient with temperature (Figure 5).



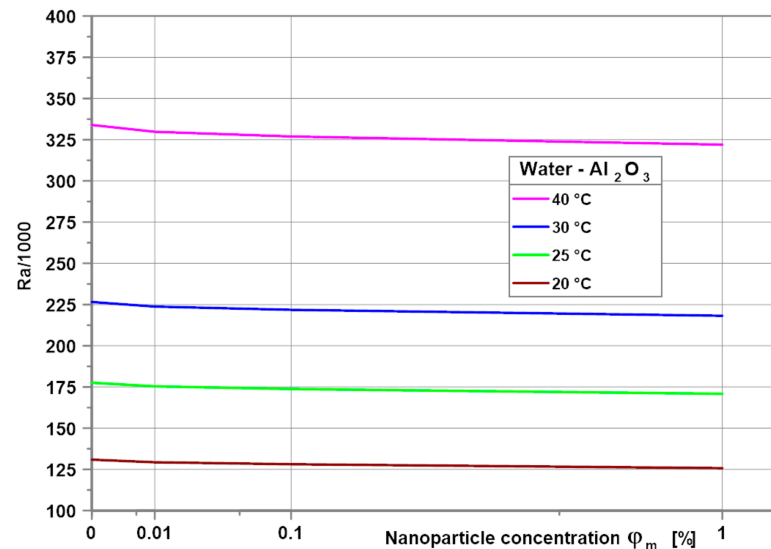
(a)



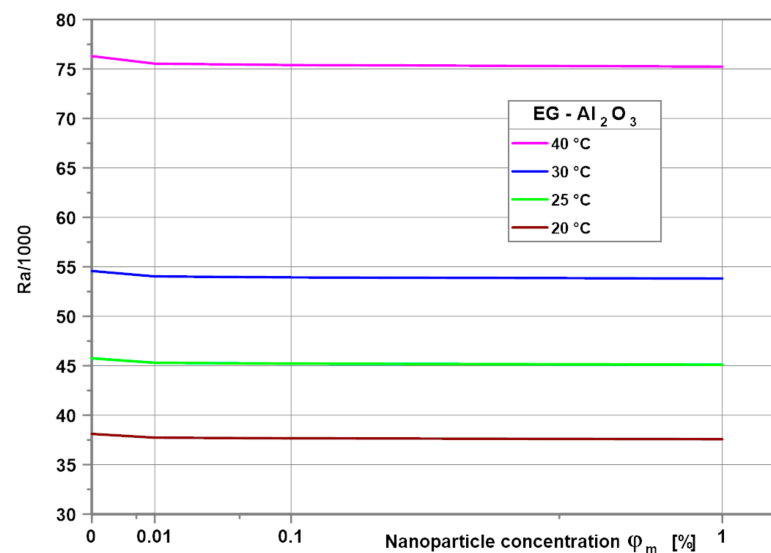
(b)

Figure 8. Variation of Rayleigh number with temperature for water-based (a) and EG-based (b) nanofluids.

Figure 9 shows the change in the Ra number against mass nanoparticle concentration for selected temperatures. It was observed that an increase in the nanoparticle concentration resulted in a gradual decrease in the Ra number for all tested temperatures. An increase in the nanoparticle concentration increased the viscosity (Figure 1) and thermal conductivity of nanofluids (Figure 2). However, the rate of increase in viscosity was higher than the increase in the thermal conductivity. Therefore, the final result was a decrease in Ra number due to an increase in nanoparticle concentration. The maximum decrease in the Ra number for water- Al_2O_3 and EG- Al_2O_3 nanofluids, at the temperature of 40 °C, equalled 3.6% and 1.4%, respectively.



(a)



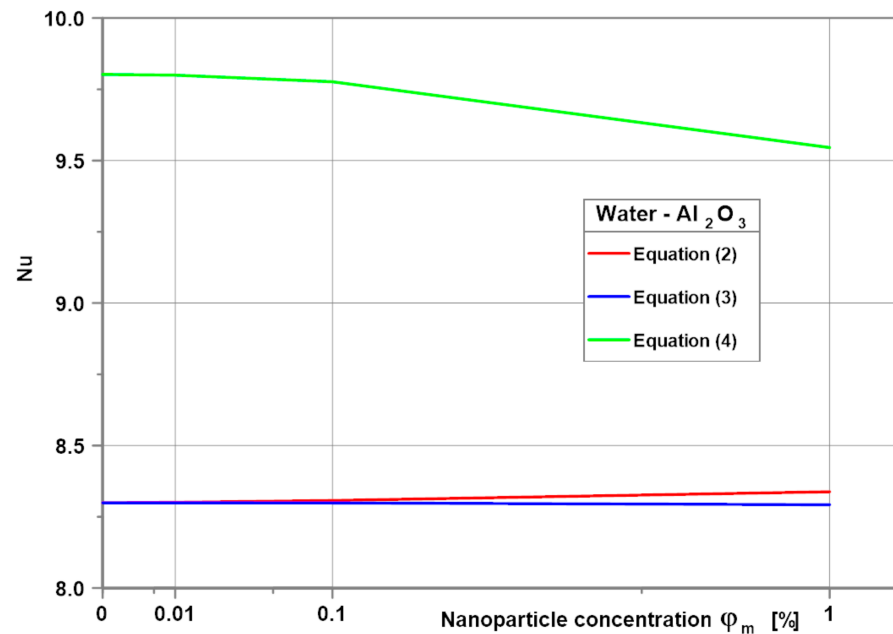
(b)

Figure 9. Variation of Ra number with temperature and nanoparticle concentration for water-based (a) and EG-based (b) nanofluids.

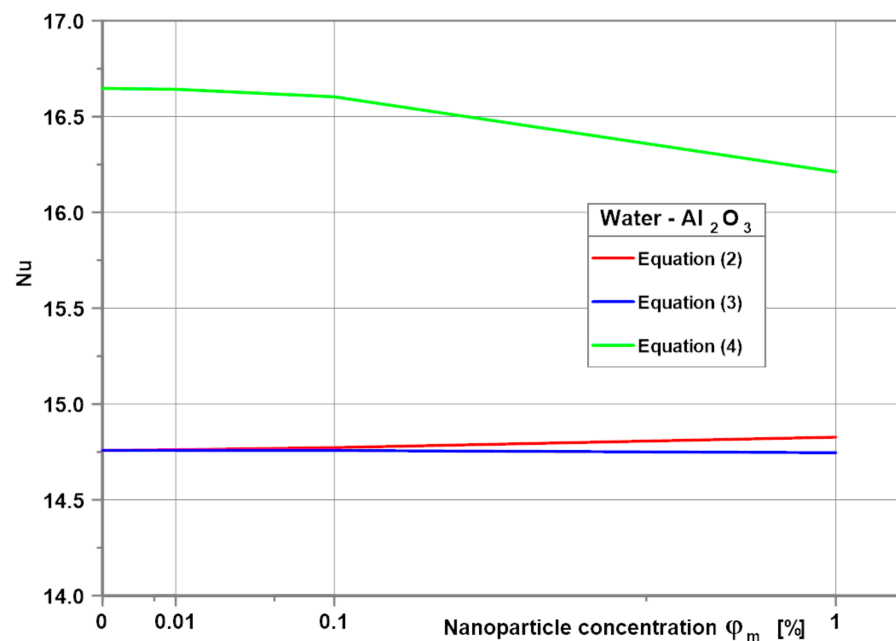
Figure 10 shows the variation of Nu number against nanoparticle mass concentration for water- Al_2O_3 nanofluids and two selected values of the Ra number, namely 10^5 and 10^6 . Predictions from the Habibi et al. correlations (Equations (2) and (3)) were compared to the predictions from the correlation developed by the present authors (Equation (4)). Calculations were conducted for a constant Pr number of $\text{Pr} = 6.2$, as it was done by Habibi



et al. [43]. As seen in Figure 10, the influence of nanoparticles on the Nu number for the tested mass concentration range $0.01\% \leq \varphi_m \leq 1\%$ was negligible for both tested Ra numbers.



(a)

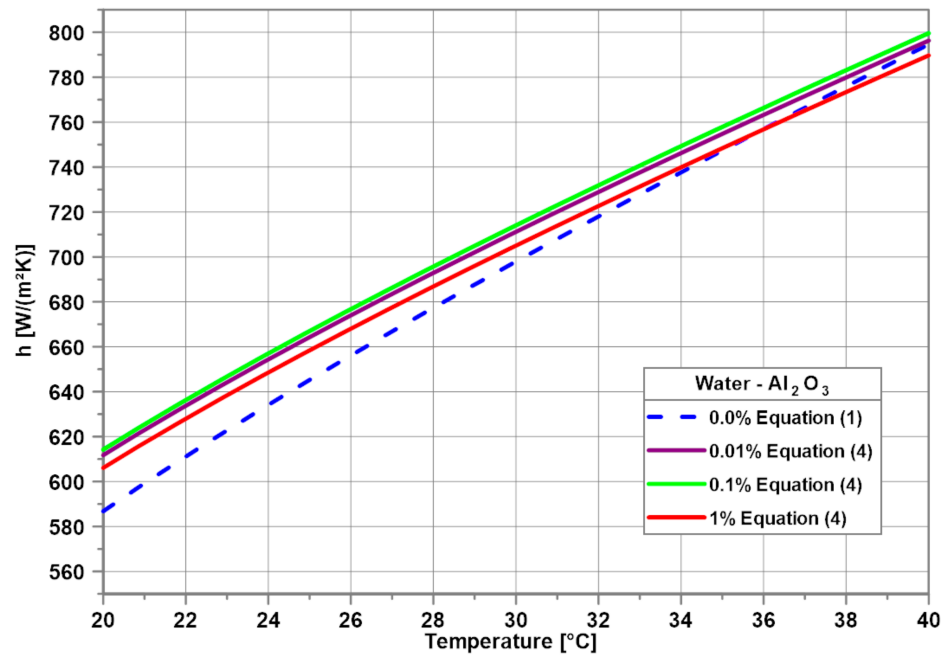


(b)

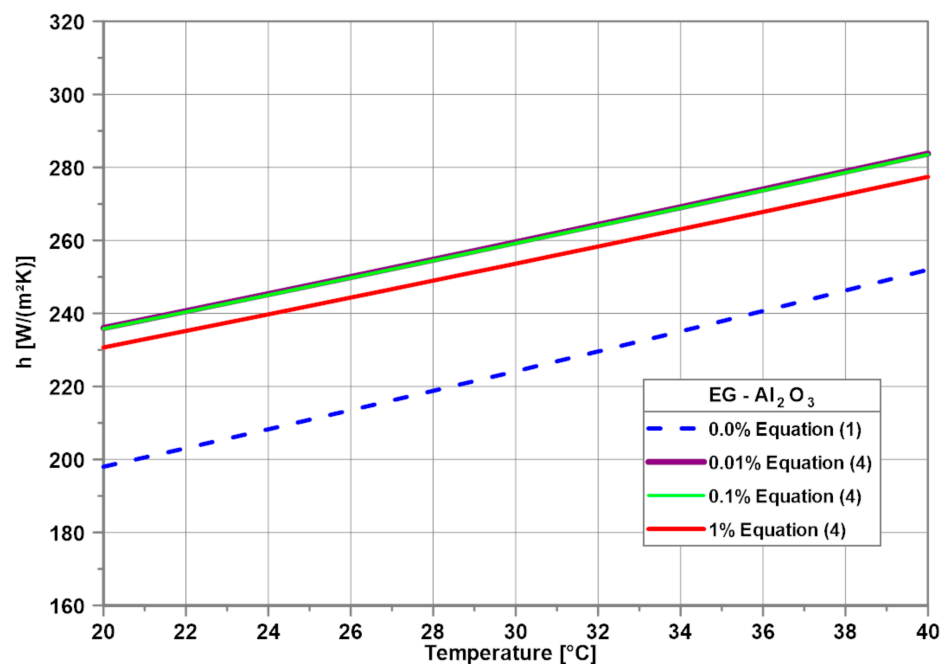
Figure 10. Variation of Nusselt number with nanoparticle mass concentration for water- Al_2O_3 nanofluids for $\text{Ra} = 10^5$ (a) and $\text{Ra} = 10^6$ (b).

Using Equation (4) and the experimental data presented in [36] ($D = 10 \text{ mm}$, $\Delta T = 10 \text{ K}$), the convective heat transfer coefficient was calculated for the water- Al_2O_3 and EG- Al_2O_3 nanofluids. The base fluid heat transfer coefficient was obtained from the Churchill and Chu correlation (Equation (1)). Figure 11 shows the variation of the heat transfer coefficient for the tested nanofluids as a function of temperature. For water- Al_2O_3 nanofluids and temperature below $35 \text{ }^\circ\text{C}$, the heat transfer coefficient was found to be higher than that

of the base fluid (pure water). However, for temperatures higher than 35 °C and the maximum tested mass concentration (1%), the advantage of nanofluids over the base fluid was diminished (Figure 11a). For EG- Al_2O_3 nanofluids and the whole temperature range, the heat transfer coefficient was found to be higher than that of the base fluid (pure EG). The highest heat transfer coefficient was observed for the minimum tested mass concentration, namely 0.01%. The increase in the heat transfer coefficient in comparison to the predicted values from the Churchill and Chu correlation (Equation (1)) equalled 19% for the lowest temperature tested (20 °C), and decreased to 12.4% for the highest temperature tested (40 °C) (Figure 11b).



(a)



(b)

Figure 11. Impact of temperature and nanoparticle mass concentration on heat transfer coefficient for water-based (a) and EG-based (b) nanofluids.

4. Discussion and Conclusions

The addition of Al₂O₃ nanoparticles to water and EG increases viscosity, thermal conductivity, and density. For example, the viscosity of the water-Al₂O₃ nanofluid of 1% mass concentration increased by 1% in comparison to the base fluid of water at the room temperature of 20 °C. Under the same conditions, the thermal conductivity of the same nanofluid increased by 3.4%, the density by 0.7%, the specific heat decreased by 0.1%, and the thermal expansion coefficient was the same. Such inconsiderable changes of the thermophysical properties resulted from the very small nanoparticle concentrations tested, namely $0.01\% \leq \varphi_m \leq 1\%$ by weight. For room temperature, this mass nanoparticle concentration range corresponded to the volume nanoparticle concentration range $0.0028\% \leq \varphi_v \leq 0.28\%$.

Viscosity of the tested nanofluids increased with nanoparticle concentration. As a key factor in understanding the viscosity of nanofluids, the Brownian motion was indicated [55].

Thermal conductivity of nanofluids increased with nanoparticle concentration. As potential mechanisms of thermal conductivity enhancement, Brownian motion, thermophoresis, nanolayer, and clustering were mentioned [25].

Density of the tested nanofluids increased with nanoparticle concentration because the density of Al₂O₃ was above three times higher than pure water or EG.

The specific heat of the tested water-based nanofluids decreased with the nanoparticle concentration increase because the specific heat of Al₂O₃ was lower than the specific heat of pure water. The specific heat of the tested EG-based nanofluids is independent on Al₂O₃ nanoparticle concentration. Equation (16) was based on the assumption of thermal equilibrium between solid nanoparticles and the liquid phase. According to [44], these two phases are not in thermal equilibrium. Probably in the case of EG-based nanofluids, a more accurate correlation for specific heat is needed.

The influence of nanoparticle concentration on the thermal expansion coefficient was negligible because the thermal expansion coefficient of Al₂O₃ was at least two orders of magnitude lower than pure water or EG.

The Pr number of nanofluids decreased as the nanoparticle mass concentration increased (e.g., for the water-Al₂O₃ nanofluid of 1% concentration the decrease is 2.8%), and decreased with an increase in temperature.

The Ra number slightly decreased with an increase in nanoparticle mass concentration and distinctly increased with temperature. As an example, for the water-Al₂O₃ nanofluid at 20 °C, the Ra number decreased from 1.30×10^5 for 0.01% to 1.26×10^5 for 1% nanoparticle concentration, and at 40 °C, the Ra number decreased from 3.32×10^5 for 0.01% to 3.23×10^5 for 1% nanoparticle concentration.

The convective heat transfer coefficient of nanofluids increased with an increase in temperature and concentration and was significantly higher than that of the base fluids. As an example, for a 1% EG-Al₂O₃ nanofluid, the convective heat transfer coefficient could increase by 16.5% compared to the base fluid at room temperature.

Author Contributions: Conceptualization, J.T.C.; methodology, J.T.C. and S.S.; software, S.S.; validation, J.T.C. and S.S.; formal analysis, J.T.C.; investigation, D.S.; data curation, S.S.; writing—original draft preparation, J.T.C.; writing—review and editing, J.T.C. and S.S.; funding acquisition, S.S. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Not applicable.

Acknowledgments: The authors thank Albrecht Eicke (City University of Applied Sciences Bremen) for kind cooperation during figure preparation.

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

a	Thermal diffusivity	(m ² /s)
c_p	Specific heat	(J/(kg K))
D	Diameter	(m)
g	Gravitational acceleration	(m/s ²)
h	Heat transfer coefficient	(W/(m ² K))
k	Thermal conductivity	(W/(m K))
$Nu = \frac{hD}{k}$	Nusselt number	(-)
$Pr = \frac{\nu}{a} = \frac{\mu c_p}{k}$	Prandtl number	(-)
$Ra = \frac{g\beta(T_w - T_f)D_o^3}{\nu\alpha}$	Rayleigh number	(-)
T	Temperature	(K)
ΔT	Temperature difference	(K)

Greek symbols

β	Thermal expansion coefficient	(1/K)
μ	Dynamic viscosity	(Pa s)
ν	Kinematic viscosity	(m ² /s)
φ	Nanoparticle concentration	(-)
ρ	Density	(kg/m ³)

Subscripts

bf	Base fluid
m	Mass
nf	Nanofluid
o	Outside
p	Particle
v	Volume

Abbreviations

DWCNT	Double-walled carbon nanotubes
MWCNT	Multi-walled carbon nanotubes

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