

# Study of Integer Spin $S = 1$ in the Polar Magnet $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>

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**Abstract:** Polar magnetic materials exhibiting appreciable asymmetric exchange interactions can potentially host new topological states of matter such as vortex-like spin textures; however, realizations have been mostly limited to half-integer spins due to rare numbers of integer spin systems with broken spatial inversion lattice symmetries. Here, we studied the structure and magnetic properties of the  $S = 1$  integer spin polar magnet  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> (Ni<sup>2+</sup>, d<sup>8</sup>, <sup>3</sup>F). We synthesized single crystals and bulk polycrystalline samples of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> by combining low-temperature chemistry techniques and thermal analysis and characterized its crystal structure and physical properties. Single crystal X-ray and powder X-ray diffraction measurements demonstrated that  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> crystallizes in the noncentrosymmetric polar monoclinic structure with space group  $P2_1$ . The combination of the macroscopic electric polarization driven by the coalignment of the (IO<sub>3</sub>)<sup>-</sup> trigonal pyramids along the  $b$  axis and the  $S = 1$  state of the Ni<sup>2+</sup> cation was chosen to investigate integer spin and lattice dynamics in magnetism. The effective magnetic moment of Ni<sup>2+</sup> was extracted from magnetization measurements to be 3.2(1)  $\mu_B$ , confirming the  $S = 1$  integer spin state of Ni<sup>2+</sup> with some orbital contribution.  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> undergoes a magnetic ordering at  $T = 3$  K at a low magnetic field,  $\mu_0 H = 0.1$  T; the phase transition, nevertheless, is suppressed at a higher field,  $\mu_0 H = 3$  T. An anomaly resembling a phase transition is observed at  $T \approx 2.7$  K in the  $C_p/T$  vs.  $T$  plot, which is the approximate temperature of the magnetic phase transition of the material, indicating that the transition is magnetically driven. This work offers a useful route for exploring integer spin noncentrosymmetric materials, broadening the phase space of polar magnet candidates, which can harbor new topological spin physics.

**Keywords:** metal iodates; polar magnet; noncentrosymmetry; asymmetric exchange; integer spin

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## 1. Introduction

The lack of spatial inversion symmetry can stabilize asymmetric exchange interactions in systems with unpaired electrons, giving rise to novel physical phenomena such as multiferroics and topological spin textures [1–6]. However, engineering noncentrosymmetric (NCS) polar crystal structures for magnetic materials remains difficult, owing to a combination of several factors such as dipole–dipole interaction, steric effect, and thermodynamic effects, which often yield centrosymmetric lattices in transition metal complexes. [7–10] Polar asymmetric anions with stereo-active lone-pair electrons such as (SeO<sub>3</sub>)<sup>2-</sup> and (IO<sub>3</sub>)<sup>-</sup> trigonal pyramids provide avenues for accessing NCS polar structures, facilitated by the second-order Jahn–Teller distortion. [6,11–15] The presence of stereo-active lone-pair electrons and strong spin-orbit coupling from the heavy element (Se, I) in these asymmetric units have been shown to enhance Dzyaloshinskii–Moriya (DM) interaction. [3,16]

Increased asymmetric exchange interactions in polar magnets with half-integer spins such as Cu<sub>2</sub>OSeO<sub>3</sub> (Cu<sup>2+</sup>, d<sup>9</sup>, <sup>2</sup>D), Fe(IO<sub>3</sub>)<sub>3</sub> (Fe<sup>3+</sup>, d<sup>5</sup>, <sup>6</sup>S), and VOSe<sub>2</sub>O<sub>5</sub> (V<sup>4+</sup>, d<sup>1</sup>, <sup>2</sup>D) have been demonstrated; [2,16,17] however, studies in integer spin systems featuring the DM interaction have been left unexplored. This is, in part, because there are relatively few integer spin magnets to investigate that have NCS polar lattice symmetries. It has been shown

that half-integer and integer spin systems have different magnetic ground states, that is, the former favors a gapless state while the latter has an excitation gap (Haldane gap) between the singlet ground state and the first excited triplet state. [18–21] An excitation would cost energy in the order of the nearest-neighbor exchange interaction. Here, we study the effects of integer spin in the presence of asymmetric exchange interaction on magnetic properties by looking into the  $S = 1$  polar magnet  $\beta\text{-Ni}(\text{IO}_3)_2$  ( $\text{Ni}^{2+}$ ,  $d^8$ ,  $^3F$ ).

$\beta\text{-Ni}(\text{IO}_3)_2$  crystals are twinned by pseudo-merohedry, challenging its structural modelling as well as interpretation of its structure–property relationships. [22] In addition,  $\text{Ni}(\text{IO}_3)_2$  is polymorphic and can condense in hydrate forms depending on atmospheric and synthetic conditions, adding an extra layer of efforts that need to be invested in selectively synthesizing  $\beta\text{-Ni}(\text{IO}_3)_2$  as well as characterizing the structural and physical properties of this polymorph. The crystal structure of  $\beta\text{-Ni}(\text{IO}_3)_2$  was previously reported; [22] however, no connections between its chemistry, crystal structure, and physical properties have been established. In this study, we developed a method for synthesizing single crystals and bulk-polycrystalline samples of  $\beta\text{-Ni}(\text{IO}_3)_2$  that exhibit NCS polar structure with integer spin  $S = 1$ . We demonstrate that the synthetic chemistry can be used to prepare high-quality bulk polycrystals and single crystalline sample of transition-metal iodates. Furthermore, we probed spin and orbital contribution to the effective magnetic moment of  $\beta\text{-Ni}(\text{IO}_3)_2$  by performing magnetization measurements. We supplement magnetic properties with specific heat characterization to solidify the thermodynamic signature of the phase transition in this material. This work represents a step forward in accessing atomic engineering of integer spin and breaking inversion symmetry in polar magnets.

## 2. Materials and Methods

**Reagents.**  $\text{NiCl}_2$  (Alfa Aesar, Tewksbury, United States, 99%),  $\text{ZnCl}_2$  (Alfa Aesar, Tewksbury, MA, United States, 99.95%),  $\text{HIO}_3$  (Alfa Aesar, Tewksbury, MA, United States, 99.5%),  $\text{Li}_2\text{CO}_3$  (Alfa Aesar, Tewksbury, MA, United States, 99%), and  $\text{HNO}_3$  (BDH, Radnor, OH, United States, 67%) were used as starting materials.

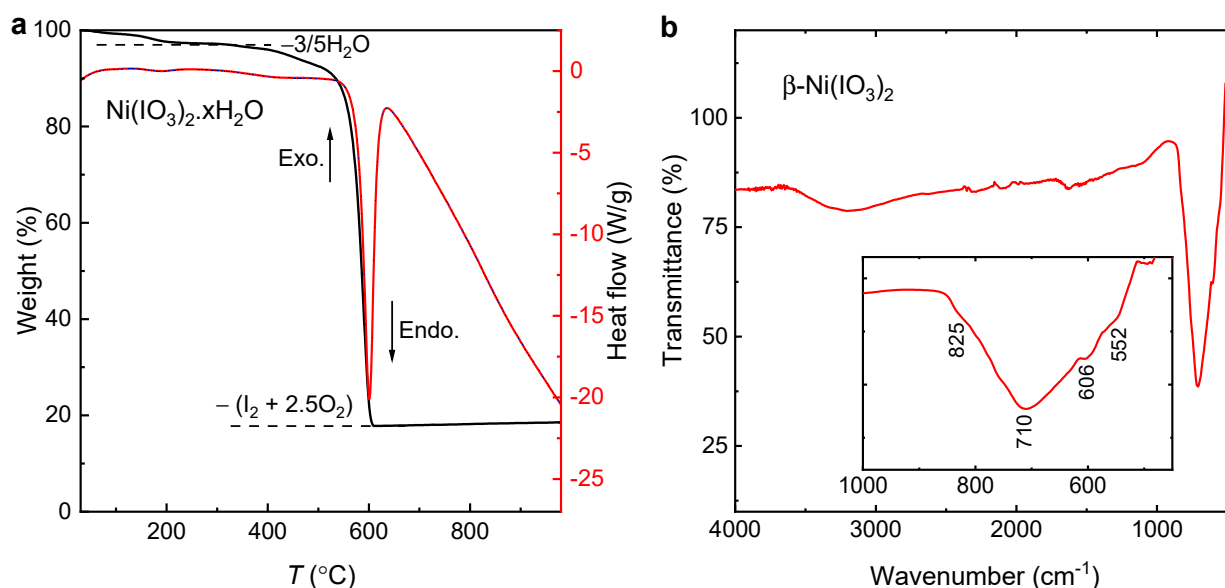
**Synthesis of  $\beta\text{-Ni}(\text{IO}_3)_2$ .** Polycrystalline  $\beta\text{-Ni}(\text{IO}_3)_2$  was obtained by heating a mixture of  $\beta\text{-Ni}(\text{IO}_3)_2$  and  $\text{Ni}(\text{IO}_3)_2 \cdot 2\text{H}_2\text{O}$  at 300 °C for 8 h (Figure 1). For  $\beta\text{-Ni}(\text{IO}_3)_2/\text{Ni}(\text{IO}_3)_2 \cdot 2\text{H}_2\text{O}$  mixture,  $\text{NiCl}_2$  (2.5 mmol) was dissolved in  $\text{HNO}_3$  (1 M, 25 mL), an aqueous solution of  $\text{HIO}_3$  (5 mmol, 10 mL) was added, and the solution was stirred at 80 °C for 1 h. A green solution was obtained and allowed to evaporate completely in a fume hood. A yellow-brown solid, subsequently determined to be  $\beta\text{-Ni}(\text{IO}_3)_2$ , was obtained after 4 days (Yield, 68%).

$\beta\text{-Ni}(\text{IO}_3)_2$  single crystals were grown by hydrothermal reaction.  $\text{Li}_2\text{CO}_3$  (1 mmol),  $\text{NiCl}_2$  (1 mmol), and  $\text{H}_2\text{O}$  (4 mL) were placed in a 23 mL Teflon-lined autoclave. The autoclave was heated at 200 °C for 96 h and cooled slowly to 25 °C at a rate of 5 °C/h.  $\beta\text{-Ni}(\text{IO}_3)_2$  yellowish crystals were isolated by filtration and washed with deionized water.

**Synthesis of  $\text{Zn}(\text{IO}_3)_2$ .**  $\text{ZnCl}_2$  (2.5 mmol) was dissolved in  $\text{HNO}_3$  (1 M, 25 mL). An aqueous solution of  $\text{HIO}_3$  (5 mmol, 10 mL) was added, and the mixture was stirred at 80 °C for 1 h to give a colorless solution.  $\text{Zn}(\text{IO}_3)_2$  white solid precipitated from the solution after 3 days and was collected by filtration and dried in air (yield of  $\text{Zn}(\text{IO}_3)_2$ , 65%; based on Zn).

**Single Crystal X-ray Diffraction.** Single crystal diffraction experiments were performed on  $\beta\text{-Ni}(\text{IO}_3)_2$  using a Bruker D8 Venture diffractometer with  $\text{Mo K}\alpha$  radiation ( $\lambda = 0.71073 \text{ \AA}$ ) and a Photon 100 detector at  $T = 300 \text{ K}$ . Data processing (SAINT) and scaling (SADABS) were performed using the Apex3 software system. The structure was solved by intrinsic phasing (SHELXT) and refined by full matrix least-squares techniques on  $F^2$  (SHELXL) using the SHELXTL software suite. All atoms were refined anisotropically.





**Figure 1.** (a) Thermogravimetric analysis (TGA) and differential scanning calorimetry (DSC) of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>/Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O showing loss of 3/5H<sub>2</sub>O of crystallization at  $T \approx 60$ –200 °C and a decomposition temperature of 523 °C accompanied by the loss of I<sub>2</sub> and 2.5O<sub>2</sub>. (b) FTIR of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> showing four absorption bands corresponding to four fundamental I–O vibrations expected for IO<sub>3</sub> group in C<sub>3v</sub> symmetry  $\Gamma_{\text{vib}} = 2A_1 + 2E$ .

**Powder X-ray diffraction.** Powder X-ray diffraction (PXRD) measurements on polycrystalline  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> and  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>/Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O mixture were performed using the Rigaku Ultima IV diffractometer equipped with Cu K $\alpha$  radiation ( $\lambda = 1.5406$  Å). Data were collected in the  $2\theta$  range of 5°–90° at 0.2°/min scan rate. Rietveld refinement of XRD pattern was performed using TOPAS Academic V6. Vesta software was used for crystal structure visualization [23].

**Synchrotron X-ray Diffraction.** Synchrotron XRD patterns of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>/Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O mixture were collected using the 11-BM beamline at Advanced Photon Source, Argonne National Laboratory. Data were collected at  $T = 295$  K and  $\lambda = 0.45789$  Å.

**Thermal analysis.** A TA SDT Q600 Instrument was used in the thermogravimetry (TG) and differential scanning calorimetry (DSC) measurements. Approximately 10 mg of the solid was isolated from the synthesis, and the  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>/Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O mixture was placed in an alumina crucible and heated at a rate of 20 °C/min from room temperature to 1000 °C under flowing nitrogen (flow rate: 100 mL/min).

**Infrared spectroscopy.** The attenuated total reflection Fourier transform infrared (ATR-FTIR) spectrum for  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> was collected using a Shimadzu IR Affinity-1S in 400 to 4000 cm<sup>-1</sup> frequency range.

**UV-Vis spectroscopy.** Optical reflectance was measured on  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> bulk powder using Agilent Cary UV–Vis (NIR) 7000 Universal Measurement Spectrophotometer from 2500 nm to 350 nm. A mixture of approximately 20 mg of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> and 100 mg of BaSO<sub>4</sub> was pelletized and used for the measurement.

**Magnetization and specific heat.** Magnetization measurements on  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> powder were performed with the vibrating sample magnetometer (VSM) option of a Quantum Design Physical Properties Measurement System (PPMS). Data were collected under the applied magnetic fields of  $\mu_0 H = 0.1$  T and 3 T from  $T = 2$  K–340 K. Magnetic susceptibility was approximated as magnetization divided by the applied magnetic field:  $\chi \approx M/H$ . Heat capacity was measured using the PPMS, employing the semiadiabatic pulse technique from  $T = 2$  K–300 K.

### 3. Results and Discussion

Polycrystalline anhydrous  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> has a brownish color, which is distinct from the green color of hydrated Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O, while  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> single crystals have a yellow color. The  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>:Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O ratio of the precursor mixture was determined to be 71%:29% by Rietveld refinements of powder XRD data (Figure S1). Pure  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> powder was obtained by heating  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>/Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O mixture at  $T = 300$  °C. The annealing temperature was determined from the thermogravimetry (TG) and differential scanning calorimetry (DSC) experiment (Figure 1a). In TG/DSC analysis, the mass reduction of 2.8% at  $T \approx 60$ – $200$  °C corresponds to the loss of  $\sim 3/5$ H<sub>2</sub>O.  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> is thermodynamically stable at  $T = 220$ – $350$  °C, suggesting that  $T = 300$  °C is an appropriate reaction temperature for the synthesis. The decomposition of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> starts at  $T = 523$  °C, accompanied by a strong endothermic transition in the DSC curve. The mass reduction is attributed to the loss of I<sub>2</sub> and 2.5O<sub>2</sub> (experimental mass loss = 79.4%; calculated mass loss = 79.6%). The polymorphic behavior of Ni(IO<sub>3</sub>)<sub>2</sub> was previously studied by Raman and FTIR spectroscopy. [24] Based on the spectroscopic evidence,  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> can be converted to  $\alpha$ -Ni(IO<sub>3</sub>)<sub>2</sub> or Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O, depending on temperature, time, and atmospheric condition. We observed the conversion of  $\sim 23\%$  of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> to Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O over the course of approximately 6 months. This transition was confirmed by the synchrotron X-ray diffraction experiment (Figure S2).

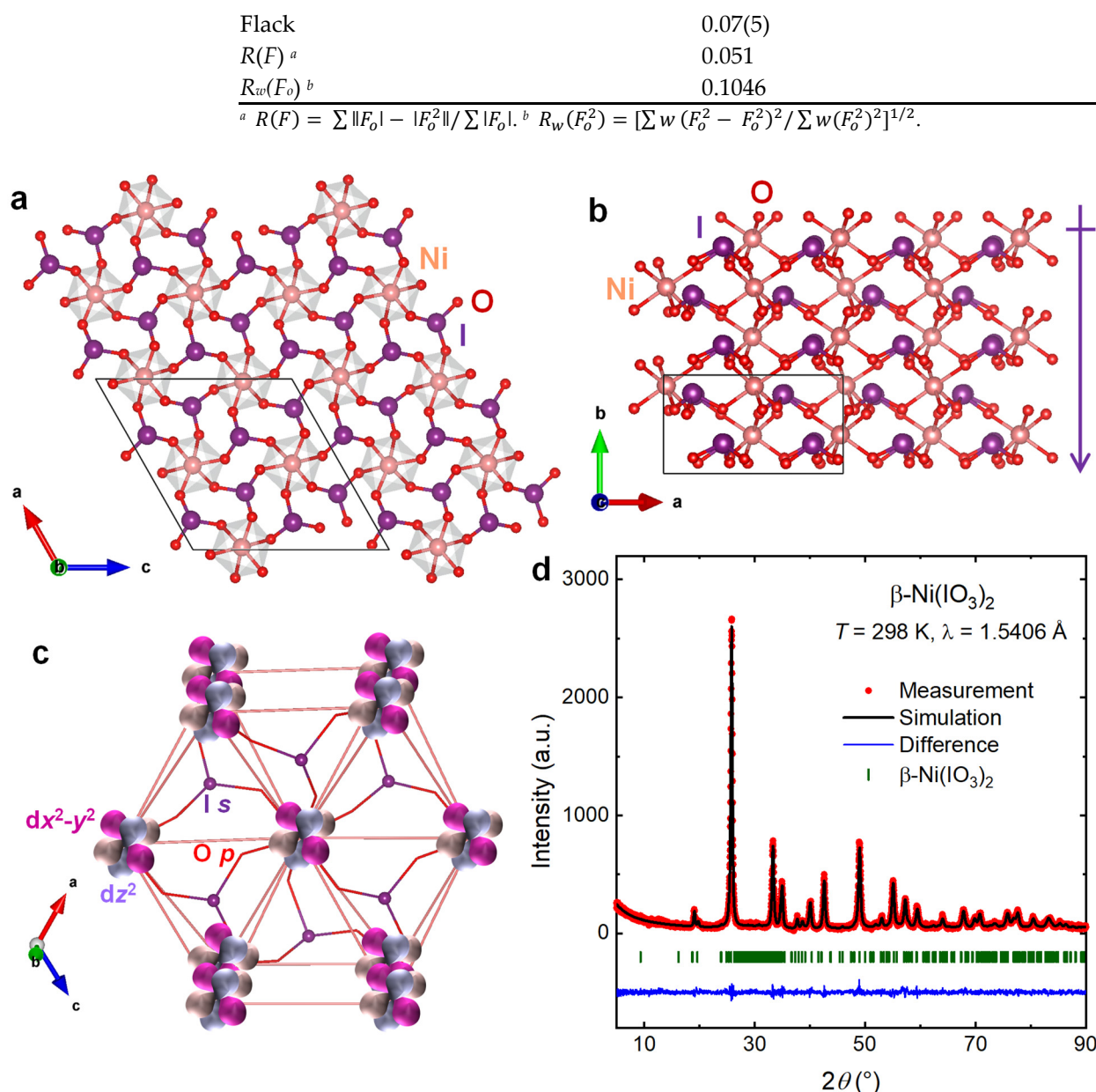
#### 3.1. Crystal Structure

To confirm the reported structure of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> [22] and evaluate its phase purity, we performed single-crystal and powder X-ray diffraction experiments. Details of the crystal structure of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> derived from single crystal X-ray diffraction are summarized in Table 1. The room-temperature powder XRD pattern of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> is in excellent agreement with the structure obtained from single crystal X-ray diffraction (Figure 2).

**Table 1.** Crystal structure information and refinement parameters for  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> obtained by single crystal X-ray diffraction.

Refinement Parameter	Crystallographic Data
Chemical formula	Ni(IO <sub>3</sub> ) <sub>2</sub>
Color	Yellow
Shape	Block
Size (mm × mm × mm)	0.02 × 0.02 × 0.02
Formula weight (g/mol)	408.51
Temperature (K)	300
X-ray radiation	Mo K $\alpha$
Wavelength ( $\lambda$ , Å)	0.71073
Crystal system	Monoclinic
Space group	$P2_1$
Z	4
$a$ (Å)	10.8067(4)
$b$ (Å)	5.1190(2)
$c$ (Å)	10.8151(4)
$\alpha = \gamma$ (°)	90
$\beta$ (°)	119.7950(10)
$V$ (Å <sup>3</sup> )	519.20(3)
$\rho_{\text{calc}}$ (g/cm <sup>3</sup> )	5.226
No. of reflections collected	7093
$\mu$ (mm <sup>-1</sup> )	15.582
$2\theta$ (°)	55
GOF	1.141





**Figure 2.** (a,b) Crystal structure of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> consisting of corner-sharing NiO<sub>6</sub> octahedra and IO<sub>3</sub> trigonal pyramid; the polar symmetry of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> results from the alignment of (IO<sub>3</sub>)<sup>-</sup> local dipole along the *b* axis. (c) Atomic connectivity and orbital overlap in  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>. (d) Rietveld refinements of XRD data of polycrystalline  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>.

$\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> crystallizes in the NCS polar monoclinic structure with space group *P2*<sub>1</sub>. The crystal structure of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> can be described as a 3D network of corner-sharing NiO<sub>6</sub> octahedra and (IO<sub>3</sub>)<sup>-</sup> trigonal pyramids. The unit cell of this material comprises two nonequivalent Ni<sup>2+</sup> positions, and each Ni<sup>2+</sup> cation is bonded to six oxygen in a slightly distorted octahedra, with Ni–O bond lengths ranging from 2.03(3) Å to 2.16(4) Å. Each I<sup>5+</sup> in (IO<sub>3</sub>)<sup>-</sup> unit is bonded to three oxygen atoms in a trigonal pyramidal geometry, induced by the stereo-active lone-pair electrons of the I<sup>5+</sup> cation (*s*<sup>2</sup>). [12,13] The I–O bond lengths range from 1.76(3) Å–1.85(4) Å. The subtle distortion of NiO<sub>6</sub> octahedra is likely induced by the packing effect of the (IO<sub>3</sub>)<sup>-</sup> asymmetric building units [7,12,16].

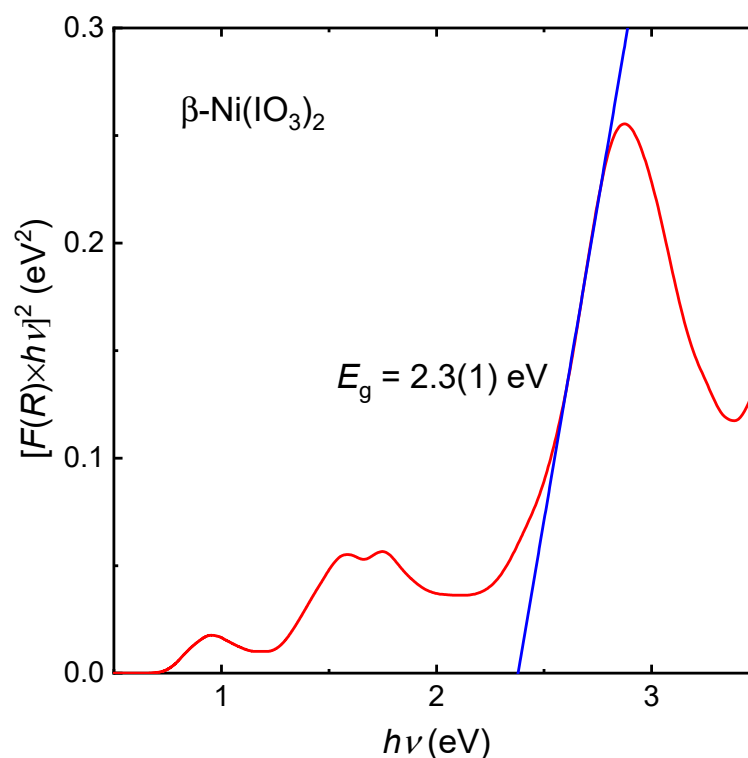
The polar symmetry of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> results largely from the alignment and addition of the (IO<sub>3</sub>)<sup>-</sup> local dipole along the *b* axis (Figure 2a). [12,13] FTIR spectra of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> show four absorption bands corresponding to four fundamental I–O vibrations expected for the (IO<sub>3</sub>)<sup>-</sup> group in *C*<sub>3v</sub> symmetry  $\Gamma_{\text{vib}} = 2A_1 + 2E$  (Figure 1b). The combined effect of the broken inversion symmetry, macroscopic polarization, stereo-active lone-pair electrons, and

triangular sub-lattice of the  $\text{Ni}^{2+}$  cations can facilitate competing magnetic exchange interactions in  $\beta\text{-Ni}(\text{IO}_3)_2$  [25–27].

$\text{Ni}(\text{IO}_3)_2 \cdot 2\text{H}_2\text{O}$  crystallizes in the centrosymmetric orthorhombic lattice with  $Pbca$  space group, and the crystal structure comprises a 2D network of corner-sharing trans- $\text{NiO}_4(\text{H}_2\text{O})_2$  octahedra and  $(\text{IO}_3)^-$  trigonal pyramids. [28] Unlike in  $\beta\text{-Ni}(\text{IO}_3)_2$ , the  $(\text{IO}_3)^-$  trigonal pyramids in  $\text{Ni}(\text{IO}_3)_2 \cdot 2\text{H}_2\text{O}$  are arranged in opposite directions along the  $b$  axis, giving rise to the centrosymmetric structure with zero polarization.

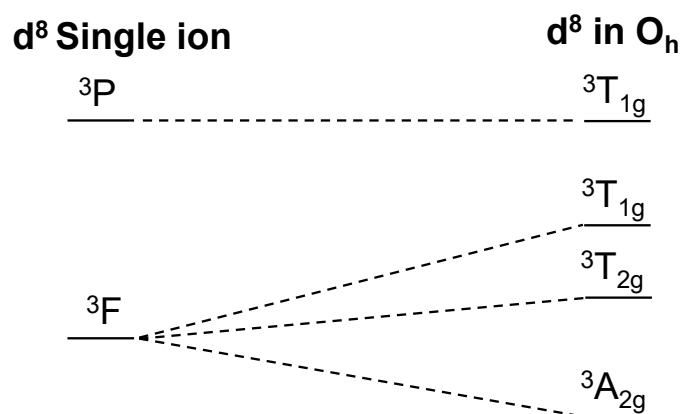
### 3.2. UV–Vis Spectra

To study the electronic transitions and estimate the optical bandgap of this material, we performed UV–Vis reflectance measurement on  $\beta\text{-Ni}(\text{IO}_3)_2$  powder. Figure 3 shows features of three characteristic bands associated with  $d \rightarrow d$  electronic transitions of a  $d^8$  metal cation in octahedral geometry. Energy states for a  $d^8$  ion in  $O_h$  symmetry is presented in Figure 4. The bands at 0.85, 1.6, and 1.8 eV are ascribed to  ${}^3T_{2g} \leftarrow {}^3A_{2g}$ ,  ${}^3T_{1g}(\text{F}) \leftarrow {}^3A_{2g}$  and  ${}^3T_{1g}(\text{P}) \leftarrow {}^3A_{2g}$  electronic transitions, respectively. The optical bandgap was estimated from the linear region of the Tauc plot of  $[F(R) \times h\nu]^2$  versus  $h\nu$  to be 2.3(1) eV (Figure 3). [29] This is consistent with the brown-yellow color (2.1–2.3 eV) of the compound.



**Figure 3.** Tauc plot for  $\beta\text{-Ni}(\text{IO}_3)_2$  showing characteristics of the electronic transitions and estimated optical bandgap of 2.3(1) eV.





**Figure 4.** Energy states for a  $d^8$  ion in  $O_h$  symmetry based on the ligand field theory.

### 3.3. Magnetization

To evaluate the magnetic properties of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>, we performed temperature-dependent magnetization measurement from  $T = 2$  K–300 K at different magnetic fields  $\mu_0H = 0.1$  T and 3 T (Figure 5). High density data of dc magnetization were collected using the VSM option of PPMS to enable accurate estimation of magnetic transition temperature and phase change.  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> exhibits field-dependent magnetic behavior. At low magnetic field  $\mu_0H = 0.1$  T,  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> undergoes a phase transition at  $T = 3$  K, while at high magnetic field  $\mu_0H = 3$  T, no magnetic phase transition was observed. Magnetic susceptibility curve above the magnetic phase transition was fit to the Curie–Weiss equation (Equation (1)):

$$\chi(T) = \frac{C}{T - \theta_{CW}} + \chi_0, \quad (1)$$

where  $C$  is the Curie constant,  $\theta_{CW}$  is the Curie–Weiss temperature, and  $\chi_0$  is the temperature-independent contribution to the susceptibility, which includes the small diamagnetic signals of the electron core and the sample holder [30].

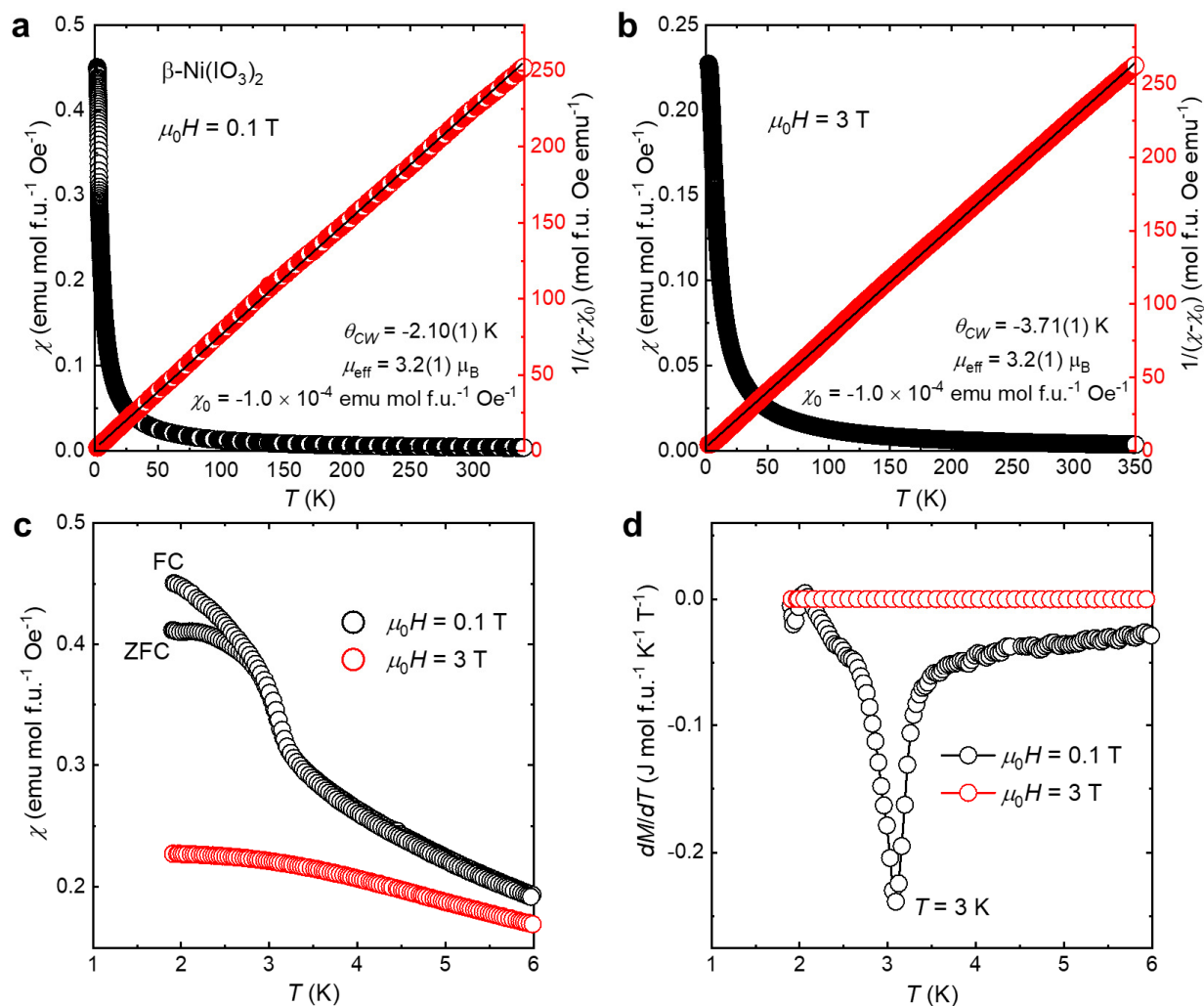
The effective magnetic moment  $\mu_{\text{eff}}$  per Ni<sup>2+</sup> cation was estimated using the relation (Equation (2))

$$\mu_{\text{eff}} = \sqrt{\left(\frac{3k_B}{N_A}\right) C}, \quad (2)$$

where  $N_A$  is the Avogadro number, and  $k_B$  is the Boltzmann constant. The obtained effective magnetic moment of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> at both magnetic fields is 3.2(1)  $\mu_B$ , which is slightly higher than the ideal spin-only magnetic moment  $g(S(S+1))^{1/2} = 2.83 \mu_B$  expected for a free spin  $S = 1$ . This result is consistent with the  $S = 1$  integer spin state with some orbital magnetic moment. Unlike the pseudo 1D Haldane SrNi<sub>2</sub>V<sub>2</sub>O<sub>8</sub>, [21] the  $\chi(T)$  plots of this material do not show a typical signature of low dimensional magnetic systems (a broad hump over a wide temperature range); these curves nevertheless exhibit a rather flat feature at 100 K <  $T$  < 350 K. This suggests that the magnetic exchange interactions of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> are not 1D but in higher dimensions of spin communication network. This observation is supported by the proposed 3D orbital overlap of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> (Figure 2c), which pertains to its electronic dimensionality and thus its magnetic interactions. Neutron diffraction experiments would provide additional insights into these magnetic exchange couplings.

An inverse susceptibility vs. temperature plot highlights the Curie–Weiss character of the magnetic susceptibility of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> (Figure 5a,b). The Curie–Weiss temperature  $\theta_{CW}$  of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> was extracted from the intercept of the linear fit to be  $-2.1$  K and  $-3.7$  K at  $\mu_0H = 0.1$  T and 3 T, respectively. The negative values of the Curie–Weiss temperature signify antiferromagnetic (AFM) exchange interaction, [31] and the small values can indicate either weak AFM coupling or competing exchange interactions. The zero-field-cooled (ZFC) and field-cooled (FC) magnetic susceptibilities as a function of temperature

measured at applied magnetic fields  $\mu_0 H = 0.1$  T and 3 T are presented in Figure 5c. ZFC and FC susceptibilities show a bifurcation below the transition temperature and a downturn at  $\sim 2.5$  K, demonstrating the possibility of competing AFM-FM interactions at low magnetic field [31,32].



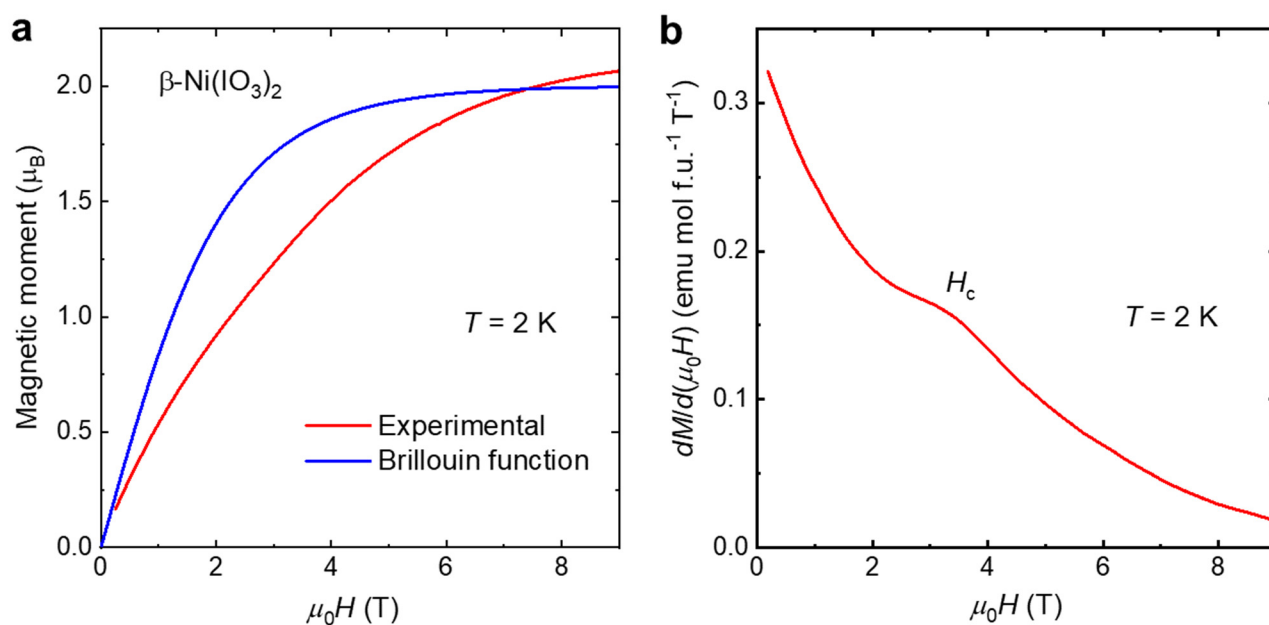
**Figure 5.** (a,b) (Black) magnetic susceptibility of  $\beta\text{-Ni}(\text{IO}_3)_2$  measured from  $T = 2$  K–300 K at (a)  $\mu_0 H = 0.1$  T and (b)  $\mu_0 H = 3$  T. (red) Curie–Weiss fitting of  $1/(\chi - \chi_0)$  against temperature for the paramagnetic phase. (c) Zero-field-cooled (ZFC) and field-cooled (FC) magnetic susceptibilities of  $\beta\text{-Ni}(\text{IO}_3)_2$  as a function of temperature at different magnetic field. (d) First derivative of magnetization with respect to the temperature,  $dM/dT$  vs.  $T$  for  $\beta\text{-Ni}(\text{IO}_3)_2$ .

The field-dependent magnetic properties of  $\beta\text{-Ni}(\text{IO}_3)_2$  can be further illustrated in the plot of first-derivative of magnetization as a function of temperature  $dM/dT$  vs.  $T$  at different fields (Figure 5d). An apparent peak is observed at  $T = 3$  K and  $\mu_0 H = 0.1$  T, indicating magnetic phase transition from a paramagnetic state to a magnetically ordered state. At  $\mu_0 H = 3$  T, no phase magnetic phase transition is observed.

To gain more insight into the nature of the magnetic phase transition, we measured the evolution of magnetization as a function of magnetic field at  $T = 2$  K (Figure 6). The nonlinear character of the  $M(H)$  curve cannot be simply described. In Figure 6a, Brillouin function (blue) describes magnetization of non-interacting paramagnetic spins, and the  $M(H)$  data of  $\beta\text{-Ni}(\text{IO}_3)_2$  are shown in  $\mu_B$  for comparison. The  $M(H)$  curve should saturate at around  $2(g^*J)$ , but instead, it crosses the 2.0 limit and reaches a higher saturation moment at a higher field, indicating orbital contribution to the magnetic moment. This is consistent with the results extracted from the Curie–Weiss analysis illustrated above. In addition, the deviation from the Brillouin function curvature likely suggests some AFM



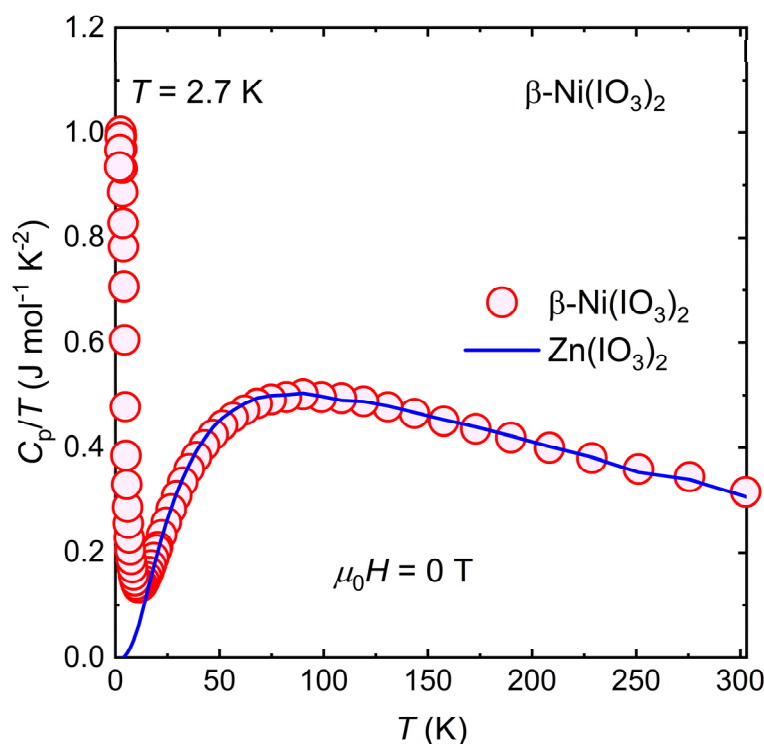
interactions present in the system. A critical field of  $\sim 3$  T is observed in the  $dM/dH$  curve as a function of magnetic field (Figure 6b).  $dM/dH$  declines and approaches zero at high magnetic fields, suggesting either saturation of magnetization or formation of a singlet state. Nevertheless, additional studies are needed to provide better understanding of the magnetic ground state of the material.



**Figure 6.** (a) (red)  $M(H)$  data of  $\beta\text{-Ni}(\text{IO}_3)_2$  in  $\mu_B$  at  $T = 2$  K, (blue) Brillouin function for  $J = 1$  and  $T = 2$  K. (b)  $dM/dH$  curve for  $\beta\text{-Ni}(\text{IO}_3)_2$ , showing critical field  $H_c$  at  $\sim 3$  T.

### 3.4. Heat Capacity

To investigate the thermodynamic properties of the ground state of this  $S = 1$  integer spin polar magnet, we performed a zero-field specific heat capacity measurement over a temperature range of  $2 \text{ K} \leq T \leq 300 \text{ K}$  (Figure 7).



**Figure 7.** Molar heat capacity over temperature ( $C_p/T$ ) vs. temperature ( $T$ ) for  $\beta\text{-Ni}(\text{IO}_3)_2$ .

An anomaly is observed at  $T \approx 2.7$  K in the  $C_p/T$  vs.  $T$  plot, which is approximately the temperature of the magnetic phase transition in  $\beta\text{-Ni}(\text{IO}_3)_2$ . The entropy recovered  $\Delta S$  from this transition can be estimated from Equation (3):

$$\Delta S = \int_0^T \frac{C_v}{T} dT, \quad (3)$$

where  $C_v$  is the heat capacity at constant volume, which is approximated as  $C_p$ —heat capacity at constant pressure—for solid at low temperatures, and  $T$  is the temperature. Phonon contribution to specific heat entropy can be accurately estimated using appropriate nonmagnetic isostructural material. The heat capacity of nonmagnetic isostructural  $\text{Zn}(\text{IO}_3)_2$  was used to subtract the phonon contribution. The entropy recovered from the specific heat data at  $2 \text{ K} \leq T \leq 300 \text{ K}$  was estimated to be  $3.3(1) \text{ J mol f.u.}^{-1} \text{ K}^{-1}$ , which is  $\sim 36\%$  of the expected value of  $R \ln(3)$  for  $S = 1$  (Figure S3). The entropy change accompanying the magnetic phase transition in  $\beta\text{-Ni}(\text{IO}_3)_2$  was underestimated because the transition was not complete down to  $T = 2$  K. Further specific heat measurements at  $T < 2$  K in the presence of applied magnetic fields will enable a more complete elucidation of the thermodynamic properties of the magnetic ground state of  $\beta\text{-Ni}(\text{IO}_3)_2$ .

#### 4. Conclusions

Studies in polar magnetic materials possessing asymmetric exchange interactions, which are relevant to possible emergence of topological spin physics, have been in a rather confined space of half-integer spins attributed to the scarcity of integer spin systems with broken spatial inversion symmetry.  $\beta\text{-Ni}(\text{IO}_3)_2$  was selected for the focus of this work due to its combined integer spin  $S = 1$  and NCS polar lattice components. The synthetic approach for both single crystal and polycrystalline form of  $\beta\text{-Ni}(\text{IO}_3)_2$  developed in this study provides facile chemistry for preparing new polar magnetic compounds. The magnetic behavior of  $\beta\text{-Ni}(\text{IO}_3)_2$  is field-dependent, i.e., the material undergoes a phase transition at  $T = 3$  K at low magnetic field, but the transition is suppressed at higher fields. The phase transition is magnetically driven, as evident by an anomaly observed at

approximately the same temperature in the specific heat data. Taken together, the results provide us with an avenue for expanding the phase space of polar magnets to integer spins. Additional ac magnetization, specific heat measurements, and neutron diffraction could help further demonstrate the magnetic ground state at zero field and magnetic states at finite fields, as well as determine whether integer spins in a polar crystal lattice have any impact on tuning asymmetric exchange interactions and thus potential vortex-like spin textures.

**Supplementary Materials:** The following are available online, Figure S1: Rietveld fit of powder XRD pattern of the bulk polycrystalline  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> precursor- $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>/Ni(IO<sub>3</sub>)<sub>2</sub>·2H<sub>2</sub>O mixture. Figure S2: Rietveld fit of synchrotron XRD pattern of the bulk polycrystalline  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> after 6 months in air. Figure S3: (a) Molar heat capacity over temperature ( $C_p/T$ ) vs. temperature for  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>, (b) Magnetic entropy change from 2 K to 300 K,  $\Delta S_{\text{mag}}$  ( $2 \text{ K} \leq T \leq 300 \text{ K}$ ) = 3.3(1) J mol<sup>-1</sup> K<sup>-1</sup>~36% of expected value for  $S = 1$  spins (Rln3). Table S1: Crystal structure information and refinement parameters for  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> obtained by Rietveld refinement of powder X-ray diffraction patterns. Table S2: Atomic positions for  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> obtained from the single crystal XRD. Table S3: Bond lengths and bond angles of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>. Table S4: Calculated bond valence sum ( $V_i$ ) of  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub>.

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**Conflicts of Interest:** The authors declare no conflict of interest.

**Sample Availability:** Samples of the compounds  $\beta$ -Ni(IO<sub>3</sub>)<sub>2</sub> and Zn(IO<sub>3</sub>)<sub>2</sub> are available from the authors.

## References

1. Spaldin, N.A.; Ramesh, R. Advances in magnetoelectric multiferroics. *Nat. Mater.* **2019**, *18*, 203–212, doi:10.1038/s41563-018-0275-2.
2. Seki, S.; Yu, X.Z.; Ishiwata, S.; Tokura, Y. Observation of skyrmions in a multiferroic material. *Science* **2012**, *336*, 198, doi:10.1126/science.1214143.
3. Kanazawa, N.; Seki, S.; Tokura, Y. Noncentrosymmetric magnets hosting magnetic skyrmions. *Adv. Mater.* **2017**, *29*, 1603227, doi:10.1002/adma.201603227.
4. Ruff, E.; Widmann, S.; Lunkenheimer, P.; Tsurkan, V.; Bordacs, S.; Kezsmarki, I.; Loidl, A. Multiferroicity and skyrmions carrying electric polarization in GaV<sub>4</sub>S<sub>8</sub>. *Sci. Adv.* **2015**, *1*, e1500916, doi:10.1126/sciadv.1500916.
5. Araki, Y.; Sato, T.; Fujima, Y.; Abe, N.; Tokunaga, M.; Kimura, S.; Morikawa, D.; Ukleev, V.; Yamasaki, Y.; Tabata, C.; et al. Metamagnetic transitions and magnetoelectric responses in the chiral polar helimagnet Ni<sub>2</sub>InSbO<sub>6</sub>. *Phys. Rev. B* **2020**, *102*, 054409, doi:10.1103/PhysRevB.102.054409.

6. Oyeka, E.E.; Winiarski, M.J.; Sorolla II, M.; Taddei, K.M.; Scheie, A.; Tran, T.T. Spin and orbital effects on asymmetric exchange interaction in polar magnets:  $M(\text{IO}_3)_2$  ( $M = \text{Cu}$  and  $\text{Mn}$ ). *Inorg. Chem.* **2021**, *60*, 16544–16557, doi:10.1021/acs.inorgchem.1c02432.
7. Qian, Z.; Wu, H.; Yu, H.; Hu, Z.; Wang, J.; Wu, Y. Synthesis, structure, and characterization of  $d^0$  transition-metal iodate:  $\text{BaTi}(\text{IO}_3)_6 \cdot 0.5\text{H}_2\text{O}$ . *Inorg. Chem.* **2020**, *59*, 15430–15437, doi:10.1021/acs.inorgchem.0c02426.
8. Luo, M.; Liang, F.; Hao, X.; Lin, D.; Li, B.; Lin, Z.; Ye, N. Rational design of the nonlinear optical response in a tin iodate fluoride  $\text{Sn}(\text{IO}_3)_2\text{F}_2$ . *Chem. Mater.* **2020**, *32*, 2615–2620, doi:10.1021/acs.chemmater.0c00196.
9. Nguyen, S.D.; Halasyamani, P.S. Synthesis, structure, and characterization of new  $\text{Li}^+d^0$ -lone-pair-oxides: Noncentrosymmetric polar  $\text{Li}_6(\text{Mo}_2\text{O}_5)_3(\text{SeO}_3)_6$  and Centrosymmetric  $\text{Li}_2(\text{MO}_3)(\text{TeO}_3)$  ( $M = \text{Mo}^{6+}$  or  $\text{W}^{6+}$ ). *Inorg. Chem.* **2012**, *51*, 9529–9538, doi:10.1021/ic301334c.
10. Donakowski, M.D.; Gautier, R.; Yeon, J.; Moore, D.T.; Nino, J.C.; Halasyamani, P.S.; Poeppelmeier, K.R. The role of polar,  $\Lambda$ -shaped building units in noncentrosymmetric inorganic structures. *J. Am. Chem. Soc.* **2012**, *134*, 7679–7689, doi:10.1021/ja210984k.
11. Kim, S.-H.; Yeon, J.; Halasyamani, P.S. Noncentrosymmetric polar oxide material,  $\text{Pb}_3\text{SeO}_5$ : Synthesis, characterization, electronic structure calculations, and structure-property relationships. *Chem. Mater.* **2009**, *21*, 5335–5342, doi:10.1021/cm902639p.
12. Nguyen, S.D.; Yeon, J.; Kim, S.-H.; Halasyamani, P.S.  $\text{BiO}(\text{IO}_3)$ : A new polar iodate that exhibits an aurivillius-type  $(\text{Bi}_2\text{O}_2)^{2+}$  layer and a large SHG response. *J. Am. Chem. Soc.* **2011**, *133*, 12422–12425, doi:10.1021/ja205456b.
13. Chang, H.-Y.; Kim, S.-H.; Halasyamani, P.S.; Ok, K.M. Alignment of lone pairs in a new polar material: Synthesis, characterization, and functional properties of  $\text{Li}_2\text{Ti}(\text{IO}_3)_6$ . *J. Am. Chem. Soc.* **2009**, *131*, 2426–2427, doi:10.1021/ja808469a.
14. Ok, K.M. Toward the rational design of novel noncentrosymmetric materials: Factors influencing the framework structures. *Acc. Chem. Res.* **2016**, *49*, 2774–2785, doi:10.1021/acs.accounts.6b00452.
15. Chen, J.; Hu, C.-L.; Zhang, X.-H.; Li, B.-X.; Yang, B.-P.; Mao, J.-G.  $\text{CsVO}_2\text{F}(\text{IO}_3)$ : An excellent SHG material featuring an unprecedented 3D  $[\text{VO}_2\text{F}(\text{IO}_3)]^-$  anionic framework. *Angew. Chem. Int. Ed.* **2020**, *59*, 5381–5384, doi:10.1002/anie.202000587.
16. Oyeka, E.E.; Winiarski, M.J.; Błachowski, A.; Taddei, K.M.; Scheie, A.; Tran, T.T. Potential skyrmion host  $\text{Fe}(\text{IO}_3)_3$ : Connecting stereoactive lone-pair electron effects to the Dzyaloshinskii-Moriya interaction. *Chem. Mater.* **2021**, *33*, 4661–4671, doi:10.1021/acs.chemmater.1c01163.
17. Kurumaji, T.; Nakajima, T.; Ukleev, V.; Feoktystov, A.; Arima, T.H.; Kakurai, K.; Tokura, Y. Neel-type skyrmion lattice in the tetragonal polar magnet  $\text{VOSe}_2\text{O}_5$ . *Phys. Rev. Lett.* **2017**, *119*, 237201, doi:10.1103/PhysRevLett.119.237201.
18. Buyers, W.J.L.; Morra, R.M.; Armstrong, R.L.; Hogan, M.J.; Gerlach, P.; Hirakawa, K. Experimental evidence for the Haldane gap in a spin-1 nearly isotropic, antiferromagnetic chain. *Phys. Rev. Lett.* **1986**, *56*, 371–374, doi:10.1103/PhysRevLett.56.371.
19. Cubitt, T.S.; Perez-Garcia, D.; Wolf, M.M. Undecidability of the spectral gap. *Nature* **2015**, *528*, 207–211, doi:10.1038/nature16059.
20. Kelly, Z.A.; Tran, T.T.; McQueen, T.M. Nonpolar-to-polar trimerization transitions in the  $S = 1$  Kagomé magnet  $\text{Na}_2\text{Ti}_3\text{Cl}_8$ . *Inorg. Chem.* **2019**, *58*, 11941–11948, doi:10.1021/acs.inorgchem.9b01110.
21. Bera, A.K.; Lake, B.; Islam, A.T.M.N.; Klemke, B.; Faulhaber, E.; Law, J.M. Field-induced magnetic ordering and single-ion anisotropy in the quasi-one-dimensional Haldane chain compound  $\text{SrNi}_2\text{V}_2\text{O}_8$ : A single-crystal investigation. *Phys. Rev. B* **2013**, *87*, 224423, doi:10.1103/PhysRevB.87.224423.
22. Phanon, D.; Bentría, B.; Jeanneau, E.; Benbental, D.; Mosset, A.; Gautier-Luneau, I. Crystal structure of  $M(\text{IO}_3)_2$  metal iodates, twinned by pseudo-merohedry, with MII: MgII, MnII, CoII, NiII and ZnII. *Z. Kristallogr. Cryst. Mater.* **2006**, *221*, 635–642, doi:10.1524/zkri.2006.221.9.635.
23. Momma, K.; Izumi, F. VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Crystallogr.* **2011**, *44*, 1272–1276, doi:10.1107/S0021889811038970.
24. Pracht, G.; Lange, N.; Lutz, H.D. High-temperature Raman spectroscopic studies on nickel iodates. *Thermochim. Acta* **1997**, *293*, 13–24, doi:10.1016/S0040-6031(97)00013-0.
25. Ideue, T.; Kurumaji, T.; Ishiwata, S.; Tokura, Y. Giant thermal Hall effect in multiferroics. *Nat. Mater.* **2017**, *16*, 797–802, doi:10.1038/nmat4905.
26. Peng, L.; Takagi, R.; Koshibae, W.; Shibata, K.; Nakajima, K.; Arima, T.-h.; Nagaosa, N.; Seki, S.; Yu, X.; Tokura, Y. Controlled transformation of skyrmions and antiskyrmions in a non-centrosymmetric magnet. *Nat. Nanotechnol.* **2020**, *15*, 181–186, doi:10.1038/s41565-019-0616-6.
27. Halder, M.; Chacon, A.; Bauer, A.; Simeth, W.; Mühlbauer, S.; Berger, H.; Heinen, L.; Garst, M.; Rosch, A.; Pfeleiderer, C. Thermodynamic evidence of a second skyrmion lattice phase and tilted conical phase in  $\text{Cu}_2\text{OSeO}_3$ . *Phys. Rev. B* **2018**, *98*, 144429, doi:10.1103/PhysRevB.98.144429.
28. Abrahams, S.C.; Bernstein, J.L.; Elemans, J.B.A.A.; Verschoor, G.C. Paramagnetic  $\text{Ni}(\text{IO}_3)_2 \cdot 2\text{H}_2\text{O}$ . Crystal structure of the transition-metal iodates. I. *J. Chem. Phys.* **1973**, *59*, 2007–2018, doi:10.1063/1.1680287.
29. Makuła, P.; Pacia, M.; Macyk, W. How to correctly determine the band gap energy of modified semiconductor photocatalysts based on UV-Vis spectra. *J. Phys. Chem. Lett.* **2018**, *9*, 6814–6817, doi:10.1021/acs.jpcclett.8b02892.
30. Winiarski, M.J.; Tran, T.T.; Chamorro, J.R.; McQueen, T.M.  $(\text{CsX})\text{Cu}_5\text{O}_2(\text{PO}_4)_2$  ( $X = \text{Cl}, \text{Br}, \text{I}$ ): A family of  $\text{Cu}^{2+} S = 1/2$  compounds with capped-Kagome networks composed of  $\text{OCu}_4$  units. *Inorg. Chem.* **2019**, *58*, 4328–4336, doi:10.1021/acs.inorgchem.8b03464.
31. Fritsch, V.; Moreno, N.O.; Thompson, J.D.; Sarrao, J.L.; Bovev, S. Antiferromagnetic order and evolution of magnetic entropy in  $\text{RE}_4\text{Zn}_5\text{Ge}_6$  ( $\text{RE} = \text{Y}, \text{Gd-Lu}$ ). *J. Magn. Magn. Mater.* **2005**, *299*, 87–93, doi:10.1016/j.jmmm.2005.03.087.
32. Fita, I.; Wisniewski, A.; Puzniak, R.; Iwanowski, P.; Markovich, V.; Kolesnik, S.; Dabrowski, B. Competing exchange bias and field-induced ferromagnetism in La-doped  $\text{BaFeO}_3$ . *Phys. Rev. B* **2017**, *95*, 134428, doi:10.1103/PhysRevB.95.134428.