

# Design and Implementation of a Dual-Band Filtering Wilkinson Power Divider Using Coupled T-Shaped Dual-Band Resonators

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**Abstract:** The paper introduces a novel structure of a dual-band filtering Wilkinson power divider (WPD). Its essential component is a dual-band bandpass filter (BPF), implemented using coupling lines and two T-shaped resonators. The BPF is incorporated into the divider structure to suppress the unwanted harmonics within the circuit. The latter is achieved owing to a wide stopband of the filter. The designed dual-band WPD can suppress third unwanted harmonics in both channels with high levels of attenuation. The designed dual-band WPD operates at 2.6 GHz and 3.3 GHz with a return loss of 22.1 dB and 22.3 dB at the operating frequencies. Furthermore, the insertion loss and isolation are 0.3 dB and 20.2 dB at 2.6 GHz and 0.9 dB and 24.5 dB at 3.3 GHz. The analysis and simulation results are corroborated by the measurements of the fabricated divider prototype. The competitive performance of the proposed circuit is also demonstrated through comparisons with state-of-the-art divider circuits from the literature.

**Keywords:** coupled T-shaped resonator; dual-band power divider; harmonics suppression

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## 1. Introduction

Power dividers belong to the class of important microwave components, widely used in microwave and communication circuits such as amplifiers [1–4] and antenna feeding networks [5–11].

Recently, with the development of multiband microwave communication systems, the demands for multiband devices, including power dividers, has been continuously increasing [12–14]. Numerous dual-band divider circuits have been proposed and studied in the literature. These can be categorized into several groups, distinguished by the specific implementation technique employed to design a circuit. The major methods, recently used to realize dual-band power dividers, include incorporation of two-section transformers [12,15,16], open/short-ended stubs [17–19], defected ground structures [20–22], resonators [23–28], coupled lines [29–32], and lumped elements [33,34].

Another technique to design of dual-band dividers is utilization of two-section transformers combined with open/short-ended stubs [12,14–19]. Although using two-section transformers may enable dual-band operation, harmonic suppression becomes a problem. At the same time, the circuits feature excessive physical size. In [18], a tri-band Gysel power divider is presented based on open stubs, coupled lines, and slow-wave transmission line techniques. In this circuit, the harmonic suppression is obtained; however, the output port isolation is insufficient in some of the operating bands. In [19], a dual-band

filtering divider is presented by applying short-ended stubs at the divider's main branch, forming a T-junction structure. Although this divider implements dual-band operation, neither harmonic suppression nor size reduction have been achieved [19].

In [20–22], a defected ground technique is employed in the design of multi-band dividers. For example, a divider designed in [20] uses a defected ground structure and folded slot lines to realize dual-band operation. Furthermore, the circuit of [20] employs band-pass filter (BPF) cells to obtain harmonic suppression. On the other hand, the data reported in the mentioned paper indicates poor passband insertion loss. It should also be emphasized that defected ground methods contribute to fabrication complexity by adding an extra metallization layer. Additionally, the crystal photonic substrates which are useful for higher frequencies [35–43] have recently employed for power divider designs [44,45].

Currently, dual-band dividers are more frequently implemented with the aid of resonators, which facilitates size reduction and harmonic suppression [23–28]. Notwithstanding, improper utilization of this technique may result in high insertion loss, low isolation, and complex structure. Several types of resonators have been used in divider design such as patch resonators [23], substrate integrated waveguide resonators [24], dual-composite resonators [25], stepped impedance resonators [26], and ring resonators [27]. Another technique is utilization of coupled lines, which can be incorporated into the divider structure to realize dual- or multi-band operation [29–32]. This method can also be employed to achieve broadband performance, but it may also increase the insertion loss in the passband.

Yet, another method to enable multi-band operation along with size reduction and implementation of filtering properties of power dividers is the incorporation of lumped elements [33,34]. However, lumped components may be detrimental to divider performance due to the parasitic effects that occur at higher frequencies.

In practical design, the development of a divider architecture and topology has to be accompanied by tuning of geometry parameters. While circuit-theory-based methods typically yield reasonably good initial parameter values, more often than not, these have to be further adjusted to boost the circuit performance as much as possible. In terms of algorithmic approaches [46–54], on the top of conventional (e.g., gradient-based) techniques, artificial intelligence methods [55–65]—which have been widely used to solve a variety of engineering problems [66–75]—can also be employed to model and design power dividers [76,77].

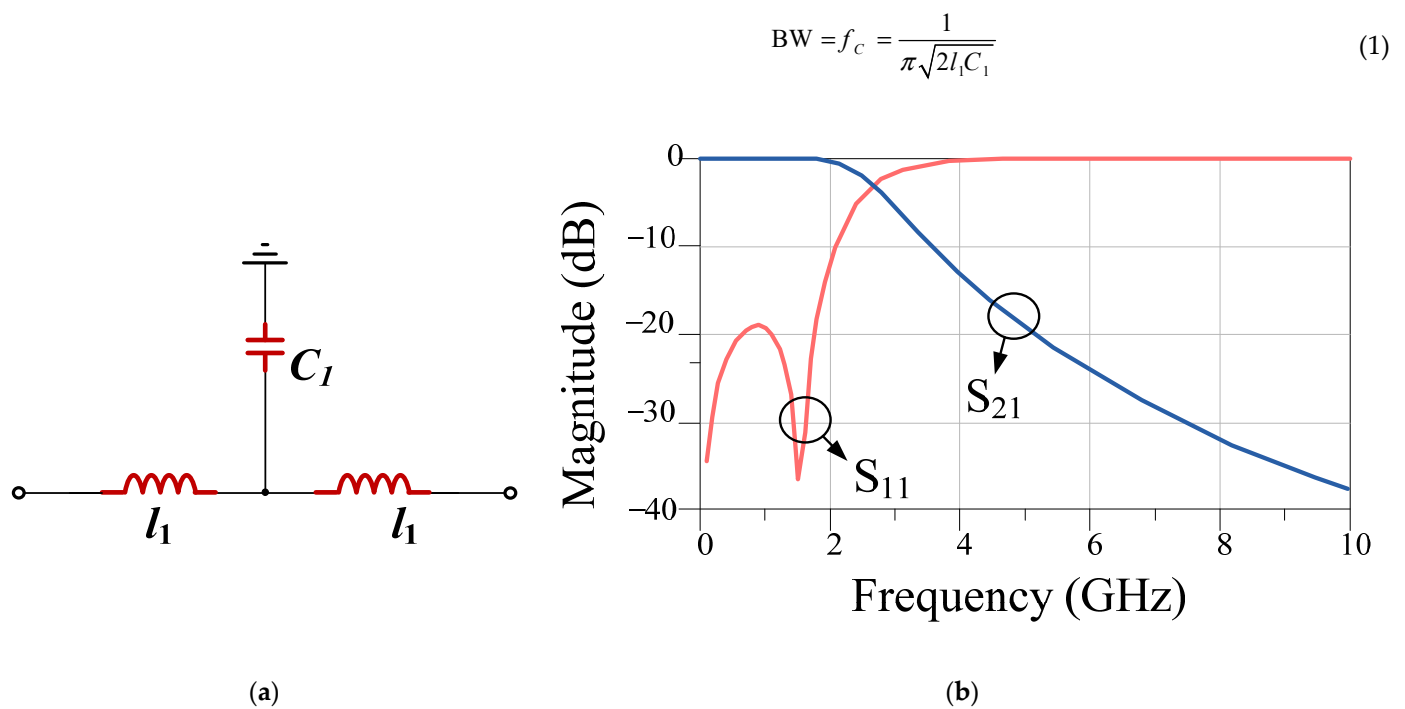
The aim of this research is to demonstrate the usefulness of incorporating T-shaped resonators and coupled lines in the development of dual-band WPDs. The specific divider structure proposed in the paper is designed to operate at 2.6 GHz and 3.3 GHz. An important component of the circuit is a dual-band filter, implemented to ensure suppression of the unwanted harmonics. Simulation and measurement data indicate superior performance of the presented circuit in terms of return and insertion losses, port isolation, as well as harmonic cancellation, which make it competitive over state-of-the-art divider structures reported in the literature.

## 2. Basic Dual-Band Filter Design

The design procedure of the basic dual-band filter is described in this section. Therein, a prototype of a three-pole Butterworth low pass filter (LPF) is selected as the fundamental circuit for the dual-band filter.

### 2.1. The Three-Pole Butterworth Low-Pass Filter (LPF)

The prototype of a three-pole Butterworth LPF schematic and its simulated  $S$ -parameters are depicted in Figure 1. It can be observed that the three-pole Butterworth LPF transition band is not sufficiently sharp; additionally, dual-band operation cannot be realized with this structure. The cutoff frequency and bandwidth (BW) of the LPF can be determined as



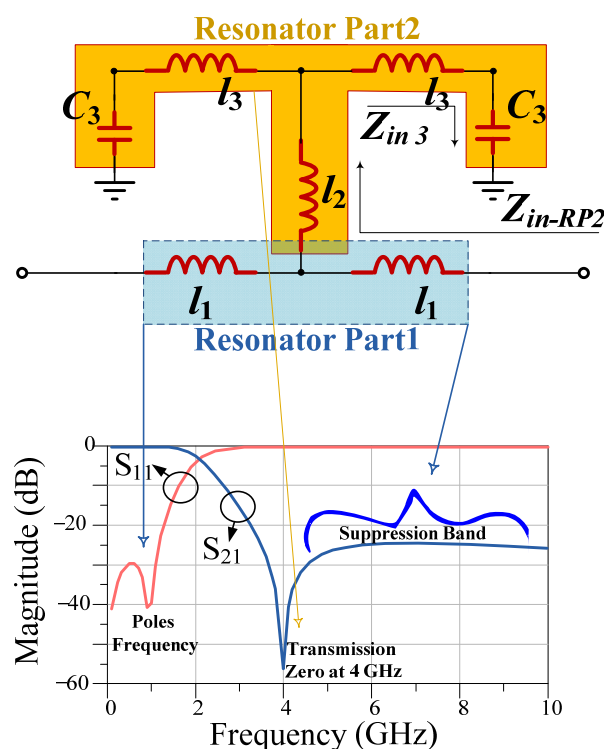
**Figure 1.** The prototype of a 3-pole Butterworth low pass filter. (a) Schematic and (b) simulated S-parameters. The Butterworth filter is known for the maximally flat bandpass characteristics. The cutoff frequency of the filter is 2.7 GHz, and the frequency corresponding to the 20 dB attenuation level is 5.2 GHz. The filter is selected as the basic cell for the designed dual-band filter, which will finally be incorporated into the proposed power divider.

To improve the performance of the three-pole Butterworth LPF, a new resonator is incorporated into the filter structure, which will be discussed in the next section.

## 2.2. Basic LPF Prototype

The prototype of the basic LPF and its simulated S-parameters are depicted in Figure 2. As seen, the transition band and the suppression band are improved over the structure of Section 2.1. The resonator marked as Part2, as indicated in Figure 2, realizes the transmission zero at 4 GHz. The frequency of the transmission zero can be modified by adjusting the resonator element values. To calculate the frequency of the transmission zero, the input impedance  $Z_{in-RP2}$  of the filter must be extracted. It can be written as

$$Z_{in-RP2} = jl_2\omega + Z_{in3} / 2 \quad (2)$$



**Figure 2.** The schematic and simulated S-parameters of the basic low pass filter prototype. The resonator Part1 includes two inductors  $l_1$ , marked with blue square, whereas the blue arrows show the resonator Part1's effects on the frequency response. The resonator Part 2 includes the  $l_2$  inductor and two parallel  $l_3C_3$  resonator branches, marked with yellow square, whereas the yellow arrow shows the resonator Part2's effects on the frequency response.

By substituting the impedance  $Z_{in3}$  of  $l_3C_3$  resonator branch, the filter input impedance can be expressed as

$$Z_{in-RP2} = j \frac{\omega^2 (2l_2C_3 + l_3C_3) - 1}{2C_3\omega} \quad (3)$$

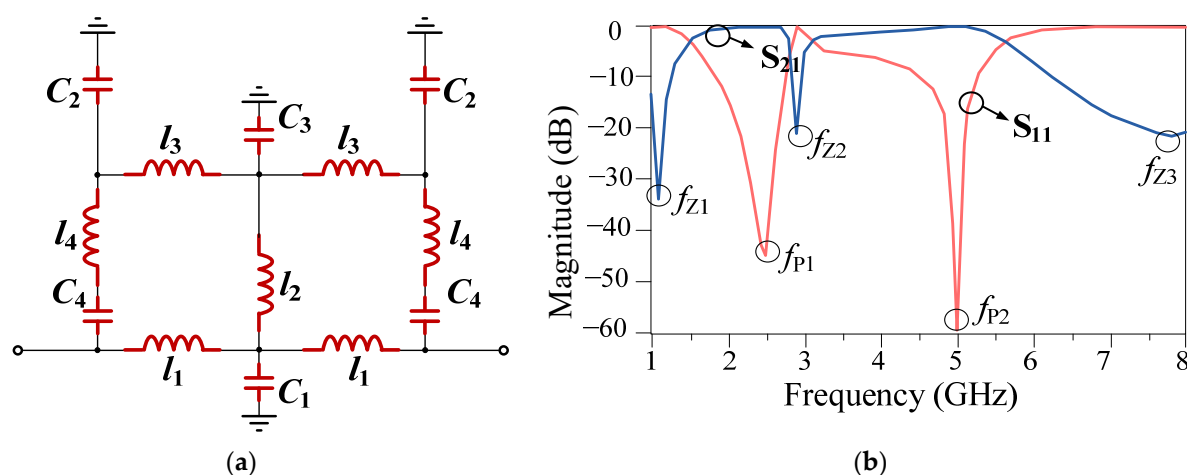
The resonance condition will be satisfied, when the imaginary part of  $Z_{in}$  becomes zero. Consequently, the resonant frequency of the basic LPF can be found as

$$f_{TZ} = \frac{1}{2\pi\sqrt{2l_2C_3 + l_3C_3}} \quad (4)$$

The resonator marked as Part1, also indicated in Figure 2, controls the pole frequencies, and the suppression band attenuation level in the low pass filter.

### 2.3. Basic Dual-Band Filter

The prototype of the proposed basic dual-band filter and its simulated S-parameters are depicted in Figure 3. The filter realizes dual-band operation by adding extra poles, created by incorporating extra capacitances into the basic low-pass filter circuit. The relevance of these modifications has been demonstrated in Figure 3b by showing the two aforementioned poles visible in the simulated reflection response of the device. The values of lumped elements, used in the discussed resonators and filters, explained in Section 2, have been gathered in Table 1.



**Figure 3.** The prototype of the proposed basic dual-band filter: (a) schematic and (b) simulated S-parameters. In the figure,  $f_{z1}$ ,  $f_{z2}$ , and  $f_{z3}$  correspond to transmission zero frequencies, whereas  $f_{P1}$  and  $f_{P2}$  correspond to the pole frequencies. The two poles created in the desired frequency range realize dual operating bands for the filter.

**Table 1.** Values of lumped elements used in resonators and filters of Section 2.

Element (Circuit)	Value (NH)- (PF)	Element	Value (NH)- (PF)
$l_1$ (LPF1)	4.0	$l_2$ (DBF)	1.8
$C_1$ (LPF1)	2.0	$l_3$ (DBF)	0.6
$l_1$ (LPF2)	3.6	$l_4$ (DBF)	0.6
$l_2$ (LPF2)	0.6	$C_1$ (DBF)	0.6
$l_3$ (LPF2)	0.2	$C_2$ (DBF)	2.8
$C_3$ (LPF2)	1.2	$C_3$ (DBF)	1.2
$l_1$ (DBF)	1.0	$C_4$ (DBF)	1.0

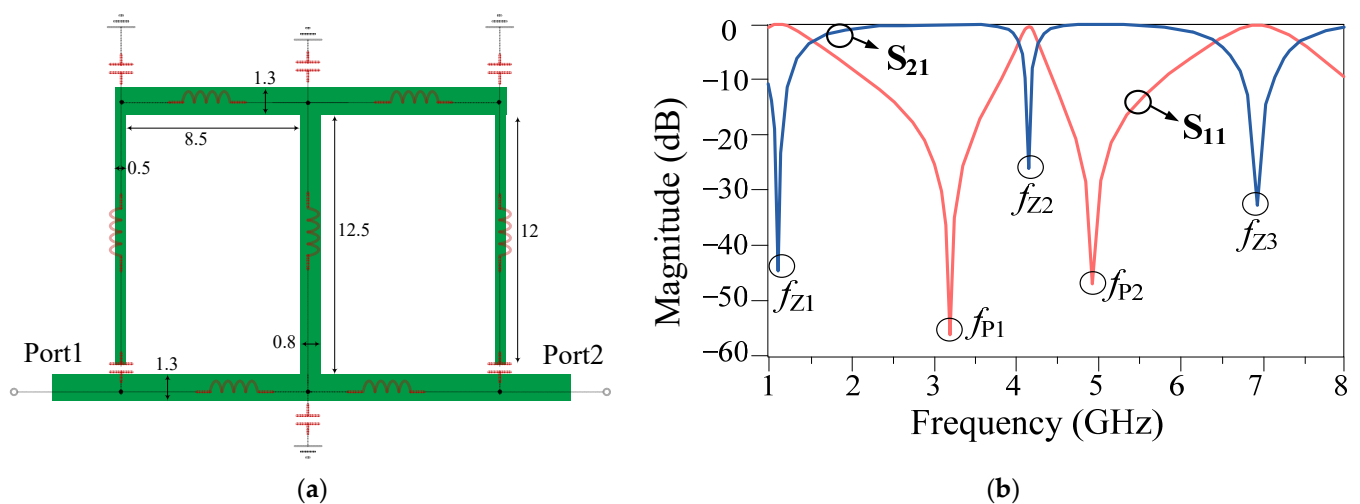
The meaning of abbreviations utilized in the table: LPF1—the 3-pole Butterworth low pass filter, shown in Figure 1, LPF2—the basic low pass filter, shown in Figure 2, DBF—the proposed basic dual-band filter, shown in Figure 3.

### 3. Dual-Band Filter: Layout Design

Realization of a satisfactory suppression band in the dual-band power divider requires the design of a dual-band filter. Section 2 discussed a basic dual-band filter architecture. In this section, the transmission line realization of the filter, which will be referred to as a dual-band T-shaped resonator, is described.

#### 3.1. Dual-Band T-Shaped Resonator Design

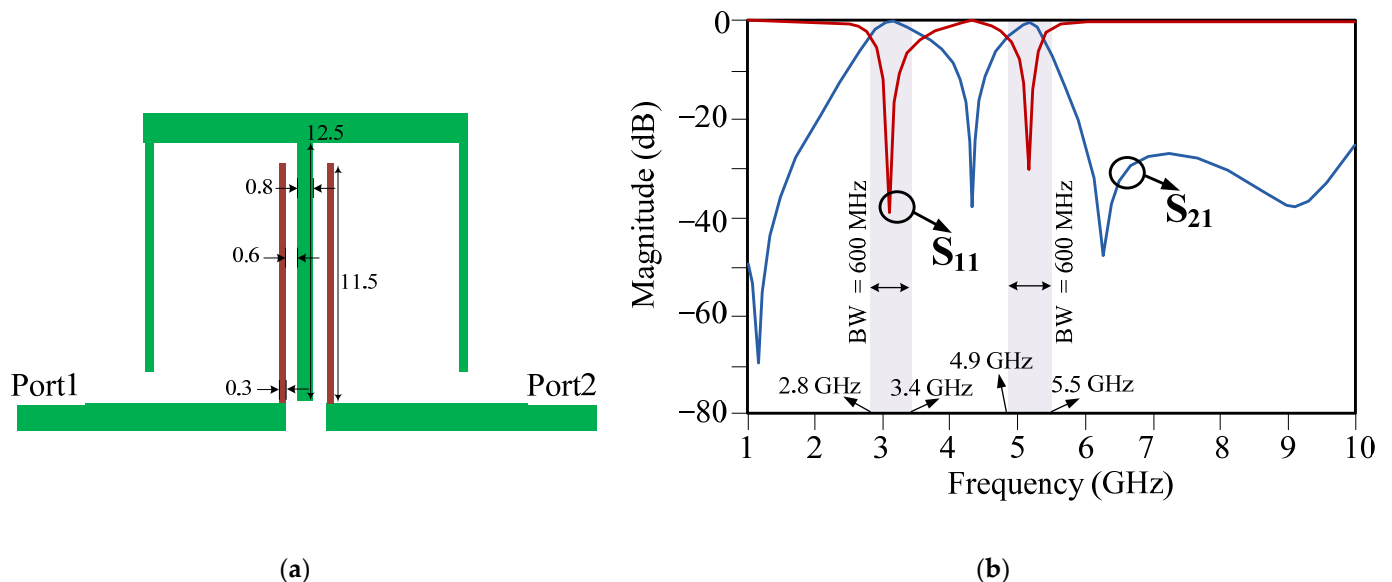
The T-shaped resonator is selected as the basic structure of the proposed power divider, because of its desirable performance and compact size. The layout and the simulated S-parameters of the dual-band T-shaped resonator have been shown in Figure 4. The resonator frequency response contains three transmission zeroes and two poles. The pole location can be adjusted to modify the dual-band operation as needed.



**Figure 4.** The proposed dual-band T-shaped resonator: (a) layout realization and (b) simulated S-parameters. In the figure,  $f_{z1}$ ,  $f_{z2}$ , and  $f_{z3}$  correspond to transmission zero frequencies, whereas  $f_{p1}$  and  $f_{p2}$  correspond to the poles' frequencies. The two poles created in the desired operating range realize dual-band operation of the filter. All dimensions are in mm.

### 3.2. Final Dual-Band Filter Design

The layout and the simulated S-parameters of the proposed final dual-band filter have been shown in Figure 5. The final circuit is formed by adding the coupled lines to the dual-band T-shaped resonator. In the proposed filter, the bandwidth of the bandpass channels can be modified by adding the coupled lines to achieve the desired frequency response.



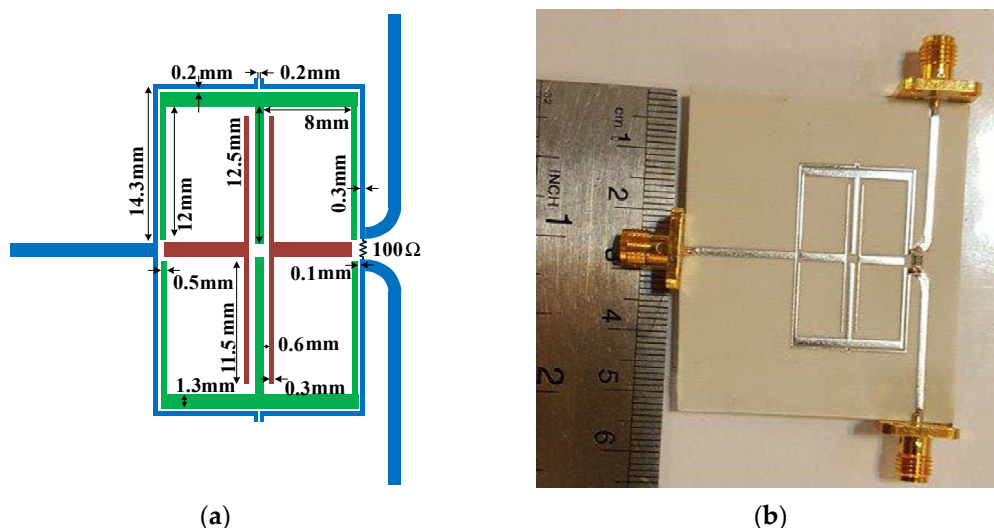
**Figure 5.** Proposed final dual-band filter: (a) circuit layout and (b) simulated S-parameters. The added coupled lines are indicated with different color in the figure. The coupled lines are used in the filter to modify the bandwidths of the bandpass channels. All dimensions are in mm.

By adding the coupled lines into the proposed dual-band T-shaped resonator, the poles' frequencies, which were located at  $f_{p1} = 3.2$  GHz and  $f_{p2} = 4.9$  GHz are changed to the desired frequencies of  $f_{p1\_New} = 3.1$  GHz and  $f_{p2\_New} = 5.2$  GHz in the proposed final dual-band filter. Additionally, adding the coupled lines into the proposed dual-band T-shaped resonator have led to about 0.1 dB improvement of the insertion loss parameter for the both channels in the proposed final filter. In the proposed final dual-band filter, the two

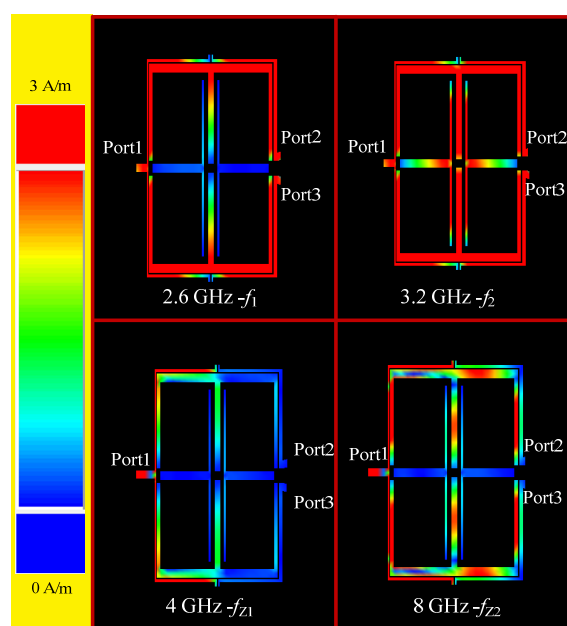
poles, created at 3.1 GHz and 5.2 GHz, provide two desired operating channels for the filter. Subsequently, the obtained dual-band filter can be incorporated in the power divider structure to obtain dual operating bands. The 3 dB obtained bandwidth of the first passband channel is from 2.8 GHz and 3.4 GHz, whereas the bandwidth of the second passband channel is from 4.9 GHz and 5.5 GHz. Thus, the bandwidth at both passband channels is 600 MHz. The insertion loss  $|S_{21}|$  and the return loss  $|S_{11}|$  at first operating frequency (3.1 GHz) are 0.1 dB and 39 dB, respectively, whereas  $|S_{21}|$  and  $|S_{11}|$  at second operating frequency (5.2 GHz) are 0.3 dB and 25 dB, respectively.

#### 4. The Proposed Power Divider Results

The layout and the picture of the fabricated prototype of the proposed dual-band WPD have been shown in Figure 6. As explained in Sections 2 and 3, a dual-band filter is first designed and analyzed. Subsequently, the main branch lines of the power divider are replaced with the proposed filter to achieve the designed dual-band WPD. The lumped 100  $\Omega$  resistor is added between port 2 and port 3 to ensure sufficient port isolation. The current distributions of the presented divider at the two main operating frequencies and the two transmission zero frequencies are shown in Figure 7. As seen, the high-magnitude current is observed within the divider at the two main frequencies, while it is reduced at the transmission zero frequencies.

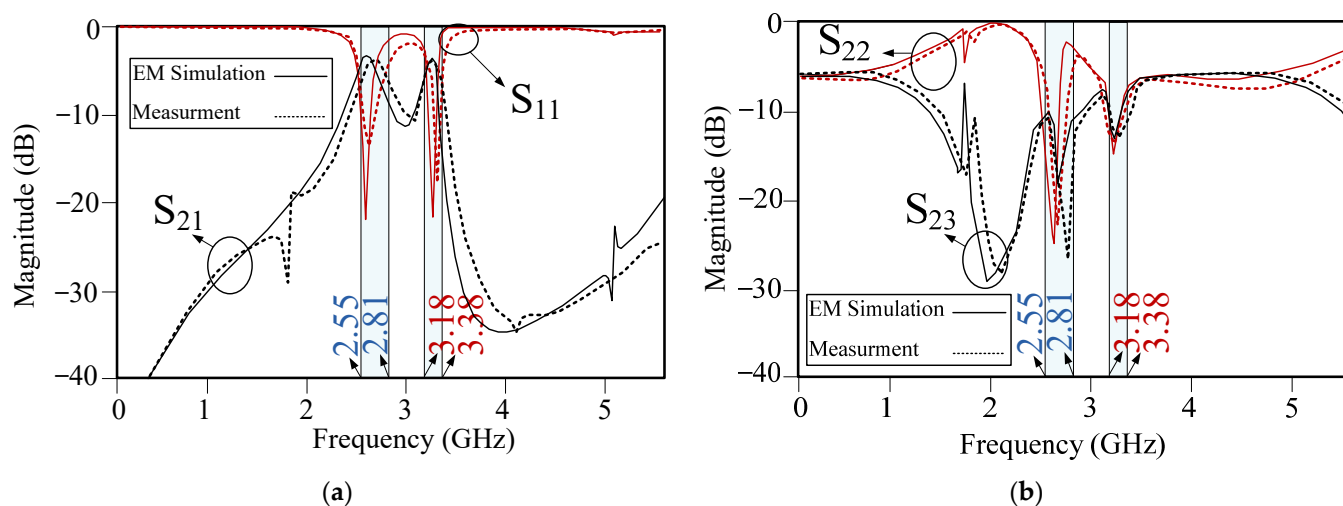


**Figure 6.** Proposed dual-band power divider: (a) circuit layout and (b) a photograph of the fabricated divider prototype.



**Figure 7.** Current distributions within the proposed dual-band WPD at the two main frequencies and the two transmission zero frequencies.

The  $S$ -parameters of the designed dual-band WPD have been shown in Figure 8. The measured values of  $S$ -parameters at the first operating frequency of 2.6 GHz are  $|S_{21}| = 4.2$  dB,  $|S_{11}| = 13.5$  dB,  $|S_{22}| = 14.1$  dB, and  $|S_{23}| = 12.2$  dB, whereas the measured  $S$ -parameter values at the second operating frequency of 3.3 GHz are  $|S_{21}| = 4.1$  dB,  $|S_{11}| = 16$  dB,  $|S_{22}| = 11.5$  dB, and  $|S_{23}| = 12.8$  dB. The operating bandwidths achieved for the circuit are 2.55 GHz to 2.81 GHz (first operating channel), and 3.18 GHz to 3.38 GHz (second operating channel).

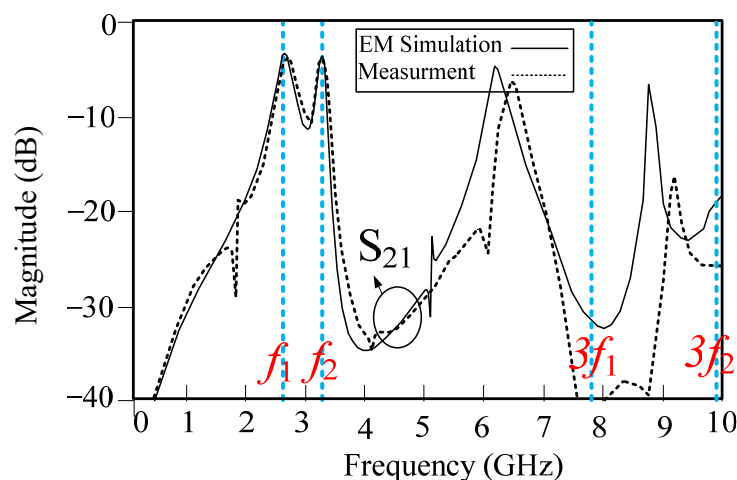


**Figure 8.**  $S$ -parameters of the designed divider circuit: (a)  $|S_{21}|$  and  $|S_{11}|$  and (b)  $|S_{22}|$  and  $|S_{23}|$ . The operating bands for the first and the second channel are indicated using the highlighted boxes in the figure.

The size of the proposed WPD is  $19.2 \text{ mm} \times 31.3 \text{ mm}$  or  $0.27 \lambda_g \times 0.44 \lambda_g$ , where  $\lambda_g = 70.5 \text{ mm}$  corresponds to the guided wavelength at the frequency of 2.6 GHz. Figure 9 shows the measured and simulated  $|S_{21}|$  of the divider evaluated over the broad frequency range. It can be observed that the third harmonics rejection has been achieved for both operating frequencies. The third harmonic of the first frequency,  $3f_1$ , is rejected with



−46 dB level, whereas the third harmonic of the second frequency,  $3f_2$ , is suppressed by more than 25 dB.



**Figure 9.** Measured and simulated and  $|S_{21}|$  of the designed dual-band divider, shown over the broad frequency range. The first and the second main frequencies are  $f_1 = 2.6$  GHz and  $f_2 = 3.3$  GHz, whereas the third harmonics for the first and the second operating frequencies are  $3f_1 = 7.8$  GHz and  $3f_2 = 9.9$  GHz.

A comparison between the performance of the designed dual-band WPD, and recent state-of-the-art dividers has been provided in Table 2. Based on the data analysis, it can be concluded that the proposed dual-band divider, apart from providing dual-band operation and harmonic suppression, has a competitive edge over the benchmark structures in terms of its physical size. Consequently, it may offer an alternative over existing circuits, especially for size-limited applications.

**Table 2.** This is a table performance comparison between the proposed dual-band WPD and related state-of-the-art dividers.

Ref.	$f_1/f_2$ (GHz)	HS	$ HSL $ (dB) $3f_1/3f_2$	Size ( $\lambda_g \times \lambda_g$ )	MTHD	Type
[78]	0.5/2	No	-	$0.6 \times 0.4$	Port extension Lumped elements	DWPD
[13]	0.9/3.5	No	-	$0.7 \times 0.6$	Port extension	DWPD
[20]	3.1/3.8	Yes	34/39	$0.42 \times 0.56$	DGS	DFPD
[27]	2.8/3.2	Yes	20/NA	$0.9 \times 0.3$	Coupled ring resonators	DBTUPD
[79]	1.8	No	-	$0.3 \times 1.1$	Open stubs Via	BTUPD
[28]	2.5/3.5	Yes	23/NA	$0.6 \times 0.47$	Slot lines Open stubs	DBTUPD
This work	2.6/3.3	Yes	46/25	$0.27 \times 0.44$	Patch resonators Open stubs	DFPD

The meaning of abbreviations utilized in the table: Ref.—reference,  $f_1/f_2$ —first and second operating frequency, HS—harmonic suppression ability, HSL—harmonic suppression level, MTHD—method (i.e., major circuit solutions utilized in the considered structure), NA—data not available, DWPD—dual-band Wilkinson power divider, DFPD—dual-band filtering power divider, BTUPD—balanced to unbalanced power divider, DBTUPD—dual-band balanced to unbalanced power divider.

One of the distinctive features of the proposed circuit is the ability to suppress the third harmonic, which is an important undesirable harmonic in microwave components



(while passed through the system channels may lead to considerable response degradation). The divider presented in this work offers a high level of attenuation thereof. This is in contrast to the benchmark structures reported in Table 2, the majority of which do not realize the filtering response at the third harmonic.

## 5. Conclusions

In this paper, a dual-band Wilkinson power divider with new and simple structure is proposed. The presented circuit incorporates a custom-designed dual-band bandpass filter for the purpose of harmonic suppression in both operating channels. A detailed design procedure and analysis has been provided to facilitate the parameter adjustment. The performance of the divider has been validated through full-wave EM simulations and physical measurements of the fabricated circuit prototype. A comprehensive comparison with the recent dividers reported in the literature corroborates the advantages of the proposed structure in terms of its overall utility (dual-band operation, harmonic suppression) but also small size. The latter makes our design potentially attractive for space-limited applications.

**Author Contributions:** Conceptualization, S.R. (Sobhan Roshani), S.K. and S.R. (Saeed Roshani); methodology, S.R. (Sobhan Roshani), F.S.H.M. and S.R. (Saeed Roshani); software, F.S.H.M. and S.R. (Saeed Roshani); validation, S.S.; formal analysis, S.S. and S.R. (Saeed Roshani); investigation, S.R. (Saeed Roshani); resources, S.R. (Sobhan Roshani) and F.S.H.M.; writing—original draft preparation, S.S. and S.R. (Saeed Roshani); writing—review and editing, S.R. (Sobhan Roshani), and S.S.; visualization, S.R. (Saeed Roshani) and S.S.; supervision, S.R. (Saeed Roshani); project administration. All authors have read and agreed to the published version of the manuscript.

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**Conflicts of Interest:** The authors declare no conflicts of interest regarding this article.

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