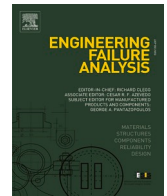




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## Fatigue fracture surface metrology of thin-walled tubular austenitic steel specimens after asynchronous loadings

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### ABSTRACT

This paper aims to study the effect of asynchronous axial-torsional strain-controlled loading histories on fracture surface behavior of thin-walled tubular X5CrNi18-10 (304/304L) austenitic steel specimens. Tests under pure axial loading and pure torsional loading are also conducted to better segregate the effect of multiaxiality. The fractures surface topographies were examined through the profiles over the entire surface with the support of an optical measurement system. Then, features of the post-failure fractures were related to the loading conditions and the fatigue life. The outcomes indicate that the multiaxial loading path significantly affects the surface topography. Overall, fracture surface parameters increase for higher fatigue lives. Based on the dialectic relationship, a fatigue damage model able to estimate the fatigue lifetime under asynchronous axial-torsional loading histories has been successfully developed. The fracture surface topology parameters collected from both sides of the same specimen lead to comparable results which reinforces the applicability of the proposed approach.

### 1. Introduction

Austenitic stainless steel is a material commonly used in engineering applications [1–5]. Thus, various austenitic steel grades are often mechanically tested, including fatigue and fracture tests. A few recent papers can be given as examples. Youn et al. studied the thermal aging effect on fracture toughness of gas-tungsten-arc-welded 316L steel [6]. Wu et al. [7] simulated crack extensions in 21-6-9 steel. Antunes et al. [8] used the plastic CTOD range parameter to investigate the crack propagation for the 304L steel. Nagaishi et al. performed fatigue tests on circumferentially-notched 304 steel specimens in air and in hydrogen atmosphere [9]. Jones et al. studied crack growth in specimens manufactured from 304L and 316L steel grades using two additive manufacturing techniques.

Since engineering parts and structures are often subjected to multiaxial loadings [10–13], many researchers study their effect on fatigue and fracture behavior [14–18], as well as the methods of fatigue life prediction [19–24]. One of the multiaxial loadings' features that gains particular interest is the non-proportionality of loading [25–28]. The reason is reduction of fatigue life compared to the proportional loadings [29] and other phenomena like additional hardening [30]. To study the effect of the non-proportional

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## Nomenclature

Symbol	Description [Unit]
$\Delta$	range of quantity [-]
$\varepsilon$	axial strain [mm/mm]
$\gamma$	shear strain [rad]
$r$	loading parameter [-]
$\lambda$	shear to normal strain ratio [-]
$f_r$	shear to normal strain frequency ratio [-]
$N_f$	number of cycles to failure [cycles]
$\lambda_c$	Gaussian cut-off filter length, wavelength to determine the bound between surface roughness component and waviness component [mm]
$\lambda_s$	Gaussian cut-off filter length, wavelength to determine the bound between surface roughness component and other shorter components [ $\mu\text{m}$ ]
$R_p$	Maximum peak height of the roughness profile [ $\mu\text{m}$ ]
$R_v$	Maximum valley depth of the roughness profile [ $\mu\text{m}$ ]
$R_z$	Maximum height of roughness profile [ $\mu\text{m}$ ]
$R_c$	Mean height of the roughness profile elements [ $\mu\text{m}$ ]
$R_t$	Total height of roughness profile [ $\mu\text{m}$ ]
$R_a$	Arithmetic mean deviation of the roughness profile [ $\mu\text{m}$ ]
$R_q$	Root-mean-square (RMS) deviation of the roughness profile [ $\mu\text{m}$ ]
$R_{sk}$	Skewness of the roughness profile [-]
$R_{ku}$	Kurtosis of the roughness profile [-]
$R_{mr}$	Relative material ratio of the roughness profile [%]
$R_{dc}$	Roughness profile section height difference [ $\mu\text{m}$ ]
$R^2$	Proportion of the variance for a dependent variable [-]
Abbreviation	Description
TC	Tension-compression (axial loading)
TOR	Torsion
IP	in-phase proportional loading
OP	out-of-phase loading
ASNx	asynchronous loading, where x stands for a number denoting the number of loading path
MON	monotonic tension
SEM	scanning electron microscope
ISO	International Organization for Standardization
L	longer part of the broken specimen
S	shorter part of the broken specimen

loadings on the fatigue life, out-of-phase loadings are typically chosen [31–33]. However, non-proportional loadings may be more complicated. To investigate the influence of other non-proportional loading paths on fatigue behavior of metal alloys, Pejkowski et al. conducted experiments employing asynchronous loadings [34,35]. In case of these loadings, there is a difference in frequencies of strain components. Principal axes of stress and strain rotate, like in case of out-of-phase loadings, and the degree of non-proportionality differs. It was shown that the material response to asynchronous loadings is more complex, and fatigue life prediction is more challenging. The idea of including the asynchronous loadings in multiaxial fatigue testing campaigns was also used by other authors [36–39].

The fracture surface of materials has a complicated morphology [40,41]. For brittle materials, such as ceramic microstructure, more deflections are reasoned by the poor grain boundaries and therefore, the roughness of these fracture surfaces is increased [42]. Falkowska et al. [43] showed that the monotonic crack growth in sintered metal typically has a mixed ductile-brittle nature, which of course also has a great deal to do with the fracture surface topography. The research on the morphology of fatigue fractures is carried out on various scales (from macro to nano) and the most common fractographic studies are observations using SEM [44–46]. This method gives very good possibilities of qualitative description of the fracture. However, in order to quantitatively compare the fracture surface topography parameters associated with different materials or loading characteristics, metrological tools should be used [47–49].

Extracting fracture profile gives additional information about the failure process but requires post-failure analysis. Similar analysis were carried out by Macek et al. [50] who demonstrated a relationship between the strain sequence with the surface topography behavior. These promising results motivate the analysis of other materials subjected to different loading histories.

Although some studies have addressed the correlation between the multiaxial proportional fatigue damage on fracture surface topology parameters, cases dealing with multiaxial asynchronous loading histories have not been reported yet. Thus, this paper addresses the effect of axial-torsional strain-controlled loading on fracture surface behavior in thin-walled tubular X5CrNi18-10 (304/304L) austenitic steel specimens. Tests under pure axial loading and pure torsional loading are also conducted to better understand the effect of multiaxiality. The fractures topographies are examined by taking into account the entire surfaces using an optical measurement system, and the different fracture surface parameters are related to the loading history and the associated fatigue life.

The present paper is organized as follows: Section 2 reports the materials and methods used for this investigation. Section 3 collects details on the experimental fatigue test and fractographic results. Section 4 presents the discussion and main results of the fatigue tests and the fracture profile parameters. The article finishes with a conclusion of the most relevant findings. In the end, Appendix A compiles the original area and profile for both sides of each specimen with a short table of results and the Abbott curve plots, respectively.

**2. Materials and methods**

*2.1. Material and fatigue tests*

Fatigue tests were performed during the experimental campaign described in [34]. Thin-walled specimens (see Fig. 1) were CNC machined from precise seamless pipes made of X5CrNi18-10 steel. All fatigue tests were conducted on an Instron 8874 servo-hydraulic

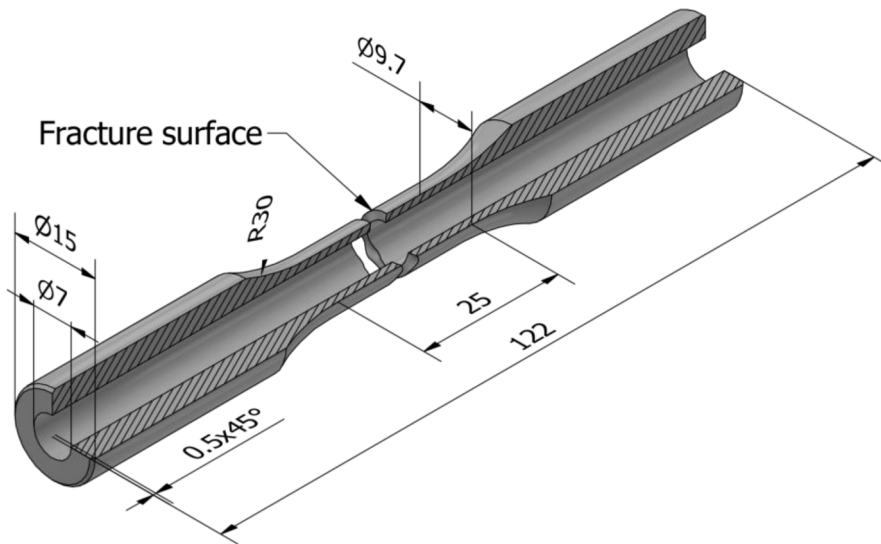


Fig. 1. Specimen shape and geometry (units: millimeters).

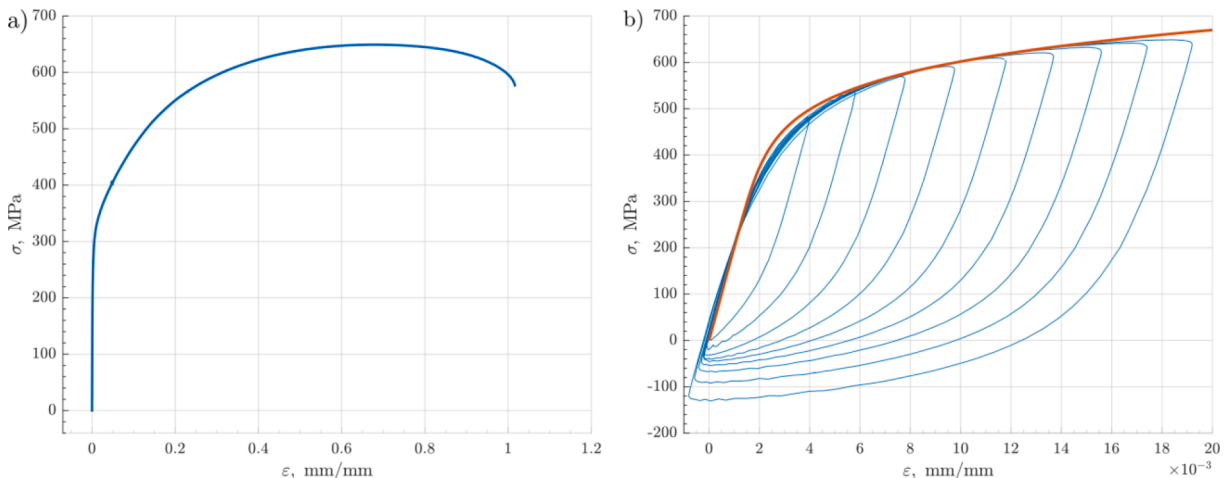


Fig. 2. a) Monotonic stress-strain curve, b) axial strain hysteresis loops with master curve.

**Table 1**  
Basic mechanical properties of X5CrNi18-10 steel.

$E$ , GPa	$\sigma_{y02}$ , MPa	$\sigma_u$ , MPa	$\epsilon_{u}$ , mm/mm	$\nu_e$ , -	$K^*$ , MPa	$n^*$
200.8	265.0	645.4	0.687	0.29	1110.8	0.1235

system, equipped with an Epsilon 3550 biaxial extensometer. The frequency of fatigue tests varied to keep the maximum value of the equivalent Huber-Mises strain rate below  $0.001 \text{ s}^{-1}$ . Nine different loading cases were applied. The parameters of loadings are presented in Fig. 2, and some complementary information is provided in Table 2. Fully-reversed sine signals of axial  $\epsilon(t)$  and shear  $\gamma(t)$  strains were applied:

$$\epsilon(t) = \epsilon_a \sin(2\pi f_\epsilon t) \tag{1}$$

$$\gamma(t) = \gamma_a \sin(2\pi f_\gamma t + \delta) \tag{2}$$

where  $\epsilon_a, \gamma_a, f_\epsilon, f_\gamma$  are amplitudes and frequencies of normal and shear strain, respectively, and  $\delta$  is a phase shift angle. The ratios of component strains amplitudes and frequencies are described by the coefficients  $\lambda = \gamma_a/\epsilon_a$  and  $f_\gamma = f_\gamma/f_\epsilon$ , respectively.

The basic mechanical properties of the tested austenitic steel, i.e. Young modulus  $E$ , offset yield stress  $\sigma_{y02}$ , ultimate tensile stress  $\sigma_u$ , total strain at failure  $\epsilon_u$ , elastic Poisson ratio  $\nu_e$ , strength parameter of master curve [51,52]  $K^*$ , and cyclic strain hardening exponent of Master curve  $n^*$  are listed in Table 1 [34]. Fig. 2 presents the monotonic tension stress-strain curve and the master curve determined based on the axial strain hysteresis loop.

**Table 2**  
Summary of fatigue testing campaign.

Specimen	$\Delta\epsilon/2$	$\Delta\gamma/2$	$\lambda$	$f_\gamma/f_\epsilon$	$2N_f$ , axial	$2N_f$ , torsional	$2N_f$ , path
029_TC	0.0055	0	0	1	3 758	0	3 758
009_TOR	0	0.0087	$\infty$	1	0	32 305	32 305
037_PRO	0.0039	0.0067	$\sqrt{3}$	1	7 248	7 248	7 248
024_OOP	0.005	0.0087	$\sqrt{3}$	1	1 244	1 244	1 244
030_ASN1	0.0044	0.0076	$\sqrt{3}$	0.5	1 435	718	718
045_ASN2	0.0047	0.0041	$\sqrt{3}/2$	4	2 465	9 860	2 465
059_ASN3	0.0016	0.0054	$2\sqrt{3}$	0.2	107 312	21 462	21 462
058_ASN4	0.0048	0.005	$3\sqrt{3}/5$	6	1 866	11 196	1 866
066_ASN5	0.0039	0.0068	$\sqrt{3}$	0.7	3 011	2 108	301

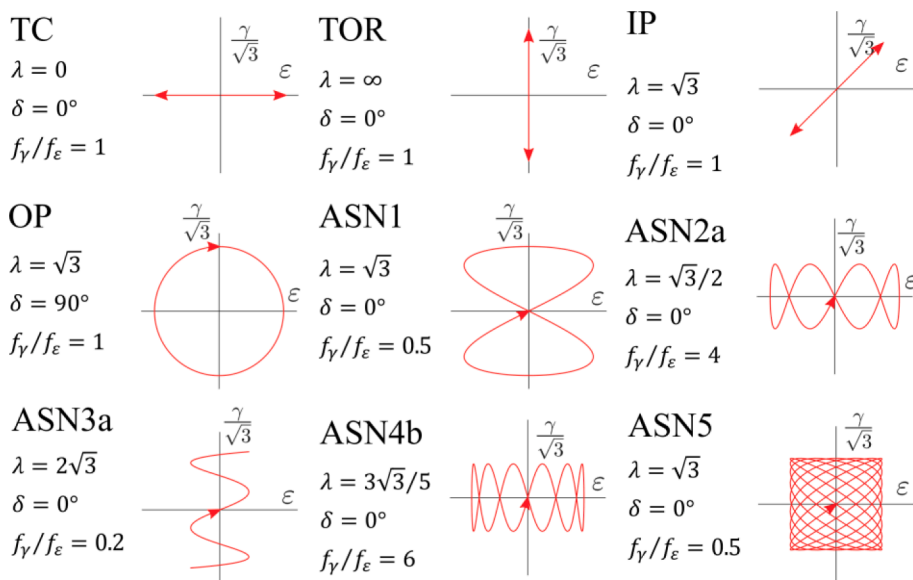


Fig. 3. Strain paths of applied loadings.



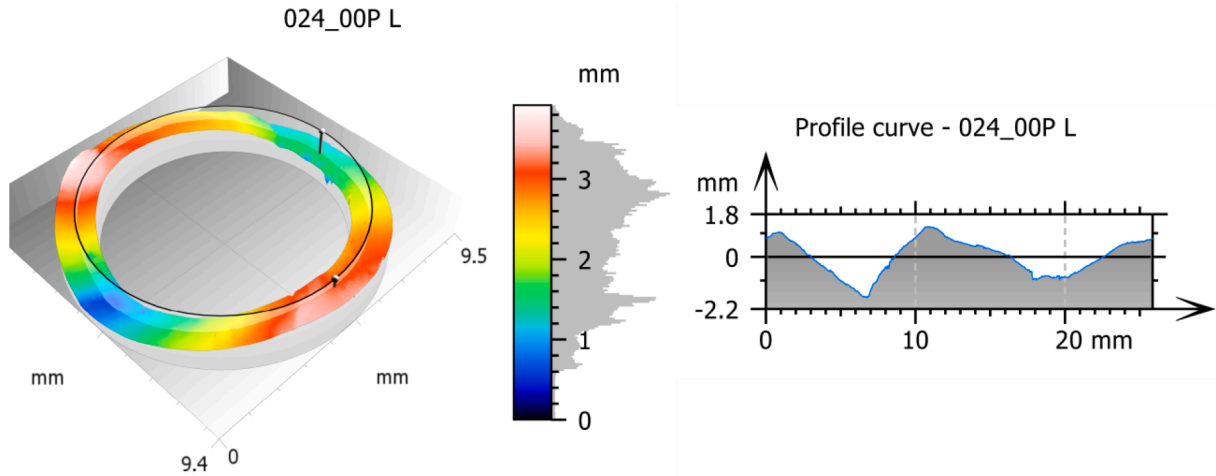


Fig. 4. Example of extracted profile.

## 2.2. Fracture surface metrology

A Sensofar S neox 3D optical surface metrology system was adopted to measure the fracture surface topography. The Focus Variation Method (FVM) was employed to determine the surface geometry of fractures, in the area of  $9.09 \times 9.36 \text{ mm}^2$  ( $3250 \times 3391$  pixels), with a pixel size of  $2.76 \mu\text{m}/\text{pixel}$ . The lens used for the measurements is a Nikon EPI 5 $\times$ .

In this study, a circular profile extraction was used (see Fig. 4). The profile of interest had a radius of 4.1 mm, generating profiles 25.76 mm long and with 18,667 points. Moreover, for confrontation, a specimen subjected to monotonic loading was checked, for which the extracted profile radius was 2.8 mm. Fig. 3 shows the 3D view of the 024\_00P fracture surface (at the top of Fig. 4) and its profile curve (at the bottom of Fig. 4). Additionally, palette cursors and histogram are marked on the 3D view scale.

The extracted circle was selected at the middle of the fracture surface. In this specimen geometry the crack propagation is more stable in that region and therefore, it is simpler to capture the central part of the thin-walled tubular surface during the surface assessment which is likely to be more deformed. Thus, the center axis of the fracture surface is more representative of the studied specimen geometry. This arrangement of the measurement profiles also allows to avoid the non-measured points near the edges of measured surfaces.

## 3. Results

### 3.1. Fatigue campaign results

The fatigue lives obtained in the tests are listed in Table 2. Since in the case of the asynchronous loadings there is a difference in frequencies of the normal and shear strain waveforms, the fatigue life was given in terms of the axial and torsional loading cycles. It was also given as the number of strain path repetitions [34].

### 3.2. Fracture surface topography analysis

The fracture profile parameters are calculated and evaluated according to ISO 4287 [53–55] standard. The  $\lambda_s$  (Gaussian) filter, applied in the level  $2.5 \mu\text{m}$ , removes scales smaller than the nesting index value of the filter. The  $\lambda_c$  filter (Gaussian) with a value of 0.8 mm that separates waviness from roughness was also applied. Evaluation length for all  $\lambda_c$  was 32. Fig. 5 shows an example of the original fracture profile and the same profile after filtering that was used to calculate the roughness parameters.

Based on the filtered profiles, the fracture surface profile measurement results are registered in Table 3 and are presented in Appendix A (see Fig. A1).

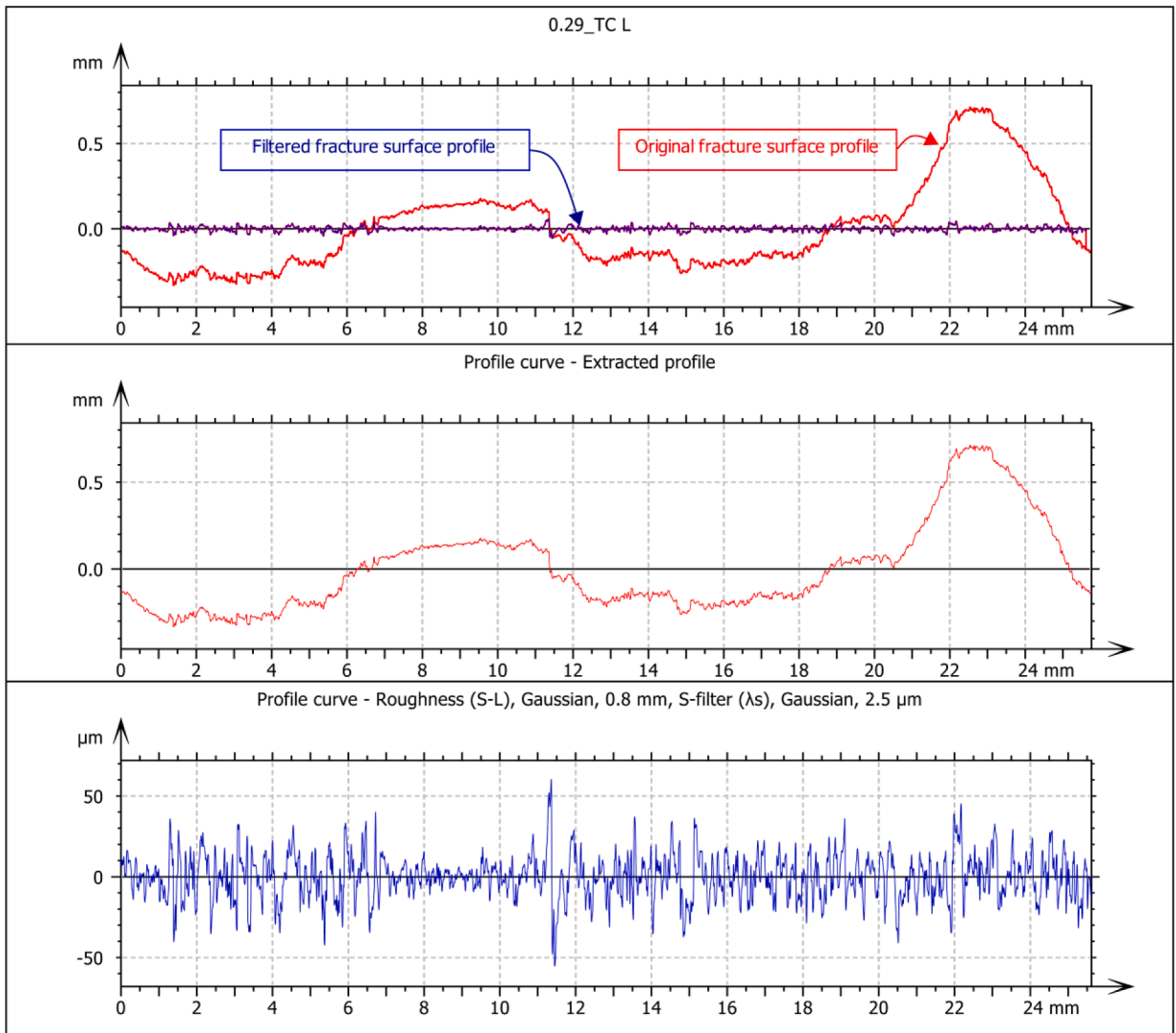


Fig. 5. Original and filtered fracture profile (roughness).

#### 4. Discussion

##### 4.1. Comparison of both sides of the specimen

Fig. 6 shows the surface profiles of fatigue fractures for the shorter and longer parts of the broken 0.29\_TC specimen, for both the original and the filtered ones. The fact that one part is shorter and the other part is longer is a random phenomenon. The nomenclature “L” and “S” is adopted for easier identification of the samples.

An interesting subject that is not completely clear at this point is the reciprocity of the measured values of the two profiles of the fracture surface. This is due to the fact that the immediate part of the fatigue fracture deforms plastically, and then the fracture surfaces rub against each other as a result of the torsion component. Fig. 7 plots the most compatible values of profile roughness parameters for the long (L) side (horizontal axis) versus those for the short (S) side (vertical axis).

Fig. 8 compares the fracture surface parameters versus fatigue life expressed in reversals to failure. The results were further fitted with a power function:

$$R_{xx} = A(2N_f)^b \tag{3}$$

where  $R_{xx}$  is a roughness parameter, and  $A$  and  $b$  are fitting coefficients. Robust fitting, based on the bisquare weight function, was used in order to reduce the influence of the outliers. Observing the charts, it was noted that some of the roughness parameters correlate quite well with the fatigue life ( $R_a, R_z, R_q$ ), while others do not ( $R_{qu}, R_{mr}, R_{sk}$ ).

**Table 3**  
Measured fracture surface profile parameters.

Specimen	$R_p$	$R_v$	$R_z$	$R_c$	$R_t$	$R_a$	$R_q$	$R_{sk}$	$R_{ku}$	$R_{mr}$	$R_{dc}$
029_TC L	26.9	28.19	55.09	31.94	115.6	10.52	12.89	-0.09	2.69	0.03	21.32
029_TC S	28.57	28.85	57.41	32.22	108.4	10.68	13.29	0.06	3.02	0.04	21.07
009_TOR L	132	118	250	492	2600	40.4	54.8	0.05	4.2	0.01	38.3
009_TOR S	125	119	244	327	1680	40.5	52.4	-0.09	3.56	0.01	38.2
037_PRO L	86.6	57.5	144	153	1170	23.3	31	0.275	4.96	0.00539	29.1
037_PRO S	144	53.9	198	648	2860	18.1	29.4	0.267	7.08	0.00539	27.2
024_OOP L	54.75	43.89	98.64	69.33	440.6	13.82	18.68	0.43	5.02	0.01	24.27
024_OOP S	49.98	35.83	85.81	82.08	681.1	11.53	16.15	0.14	4.4	0.01	20.21
030_ASN1 L	33.5	33.8	67.3	41.4	194	13	16.3	0.05	3.05	0.01	24.3
030_ASN1 S	37	38.9	75.9	48.3	282	12.7	16.5	-0.00285	3.66	0.01	22.6
045_ASN2 L	41.91	47.5	89.41	75.48	600.9	15.9	20.57	-0.02	2.94	0.01	23.58
045_ASN2 S	49.16	39.25	88.42	62.63	386.9	15.09	19.57	0.23	3.75	0.01	24.82
059_ASN3 L	30.1	30.5	60.6	36.4	294	8.56	11.6	-0.04	5.21	0.01	15.7
059_ASN3 S	23.06	26.2	50.1	29.5	159	7.48	9.88	-0.09	4.35	0.01	13.8
058_ASN4 L	65.84	61.6	127.4	92.92	594.4	15.45	22.72	0.06	6.31	0.01	25.49
058_ASN4 S	54.26	42.65	96.91	68.09	443.3	14.8	19.55	0.31	4.79	0.01	27.45
066_ASN5 L	21.1	27.9	49	28.1	202	7.48	9.86	-0.24	4.26	0.02	14.3
066_ASN5 S	19.6	21.3	41	23.9	128	7.2	9.09	-0.3	3.7	0.02	12.1
003_MON L	45.2	46.2	91.4	89.6	352	17.4	22.9	-0.07	3.01	0.03	22.6
003_MON S	43.8	56	99.7	93.9	518	17	23.5	-0.07	3.63	0.01	22.9

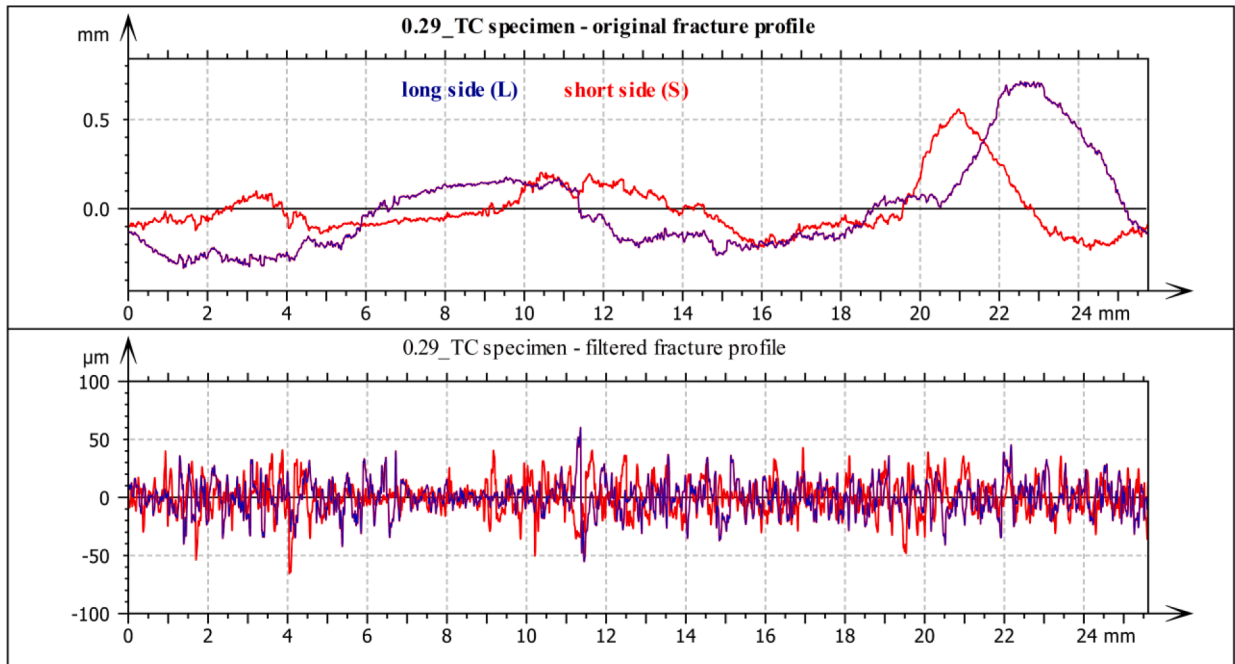


Fig. 6. Original profiles and result of filtering for both sides of 0.29\_TC specimen.

4.2. An attempt to retrace the fatigue damage history based on fracture parameter

Considering the high correlation of some of the fracture surface parameters with fatigue life, it is assumed that the fatigue damage history can be roughly retraced based on them [56,57]. By simple transformation of Eq. (3), the relationship between the fatigue life and the roughness parameter can be obtained. Fig. 9 presents a comparison of the experimental and retraced fatigue lives. Quite good compliance has been achieved. However, it should be further investigated if this method works for other loading levels and materials.

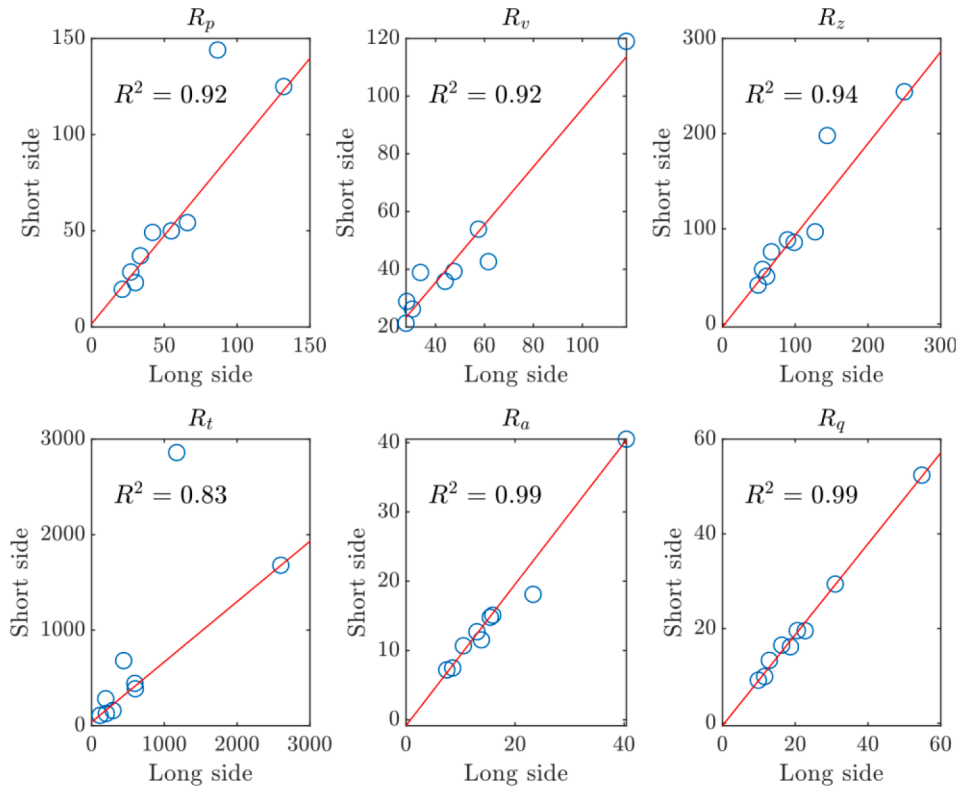


Fig. 7. Relationship of particular profile parameters evaluated for fracture of the long side (horizontal axis) and the short side (vertical axis): (a)  $R_p$ ; (b)  $R_v$ ; (c)  $R_z$ ; (d)  $R_c$ ; (e)  $R_t$ ; (f)  $R_a$ ; (g)  $R_q$ ; (h)  $R_{sk}$ ; (i)  $R_{ku}$ ; (j)  $R_{mr}$ ; and (k)  $R_{dc}$ .  $L$  denotes the long side and  $S$  denotes the short side.

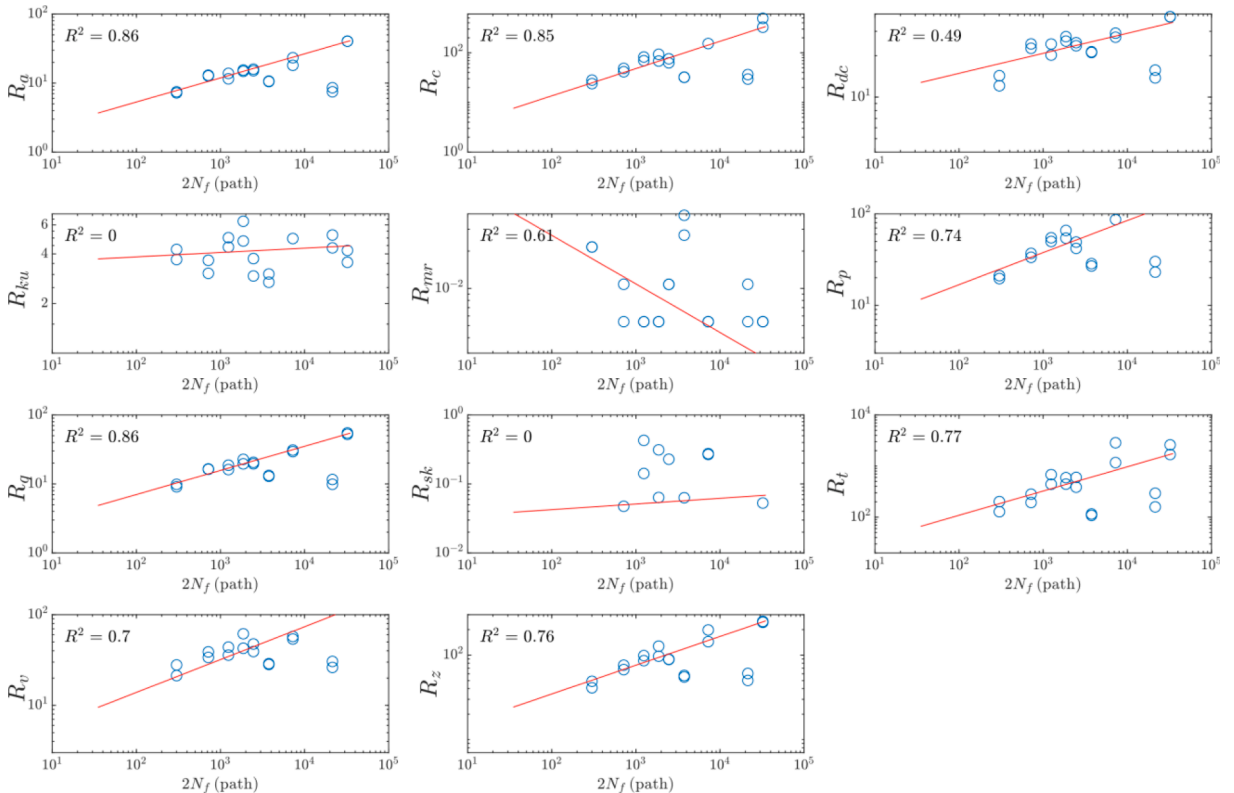


Fig. 8. Profile parameters versus fatigue life.

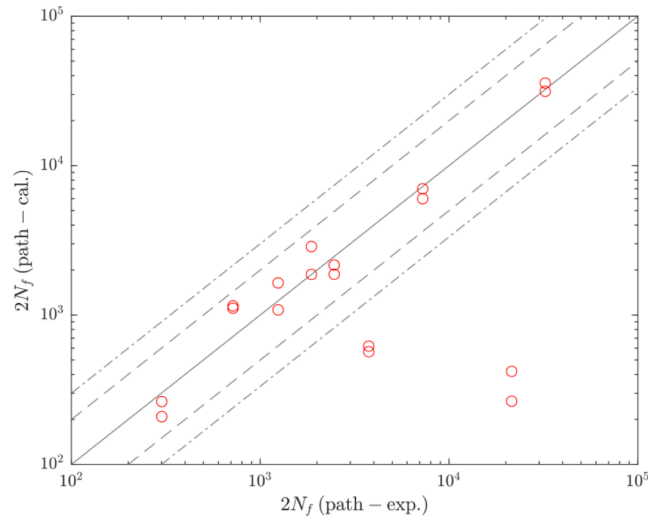


Fig. 9. A comparison of test versus retraced (calculated) fatigue life.

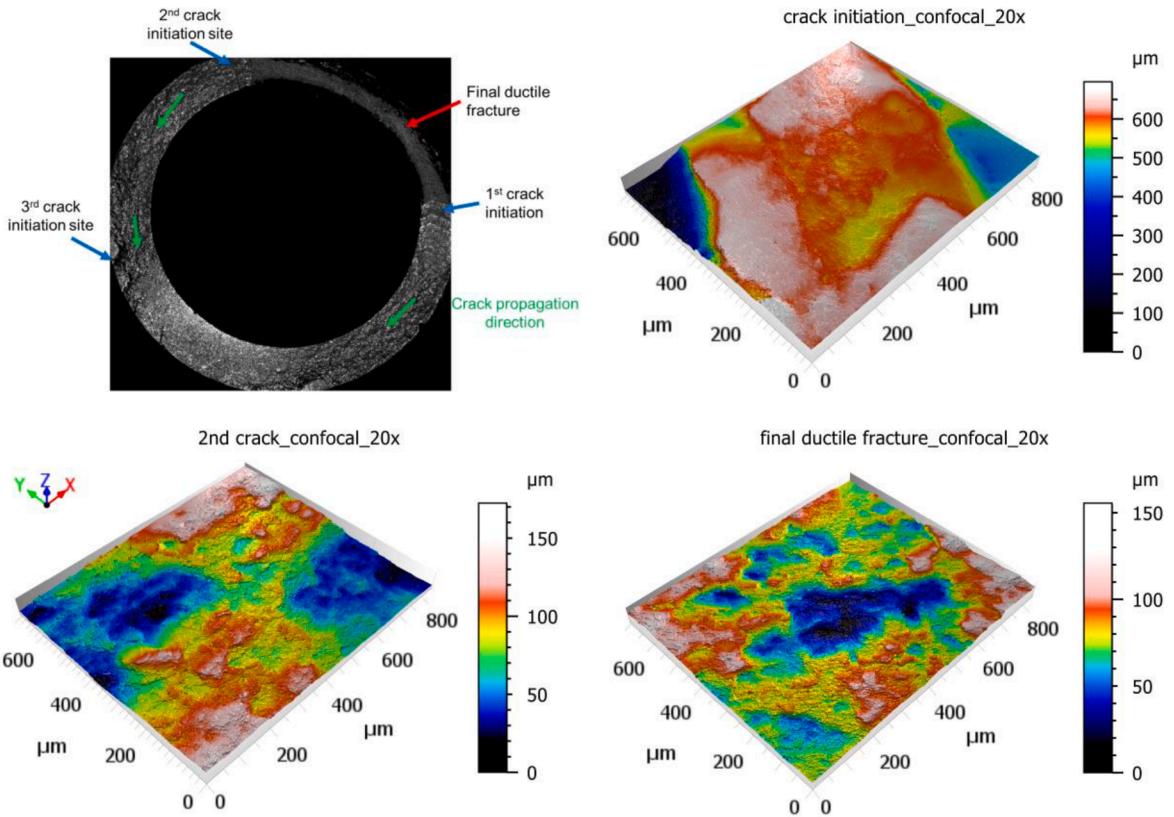


Fig. 10. Characteristic zones of selected fatigue fractures.

4.3. Fractographic analysis

Figs. 10 and 11 show characteristic images of the fatigue fracture surface features in terms of initiation and final ductile fracture zones obtained with both confocal and SEM shows, respectively. These areas were previously identified with FRASTA method [50]. Fig. 11 demonstrates the micrographs taken with a Tescan Vega 4 microscope for the zones in Fig. 10 (upper-left corner).

The failure process is characterized by the initiation of two cracks, nucleated from the surface of the specimen, in different regions of the outer surface (Fig. 10). As can be seen in the pseudo-color views, the images of both initiation sites are relatively similar in terms



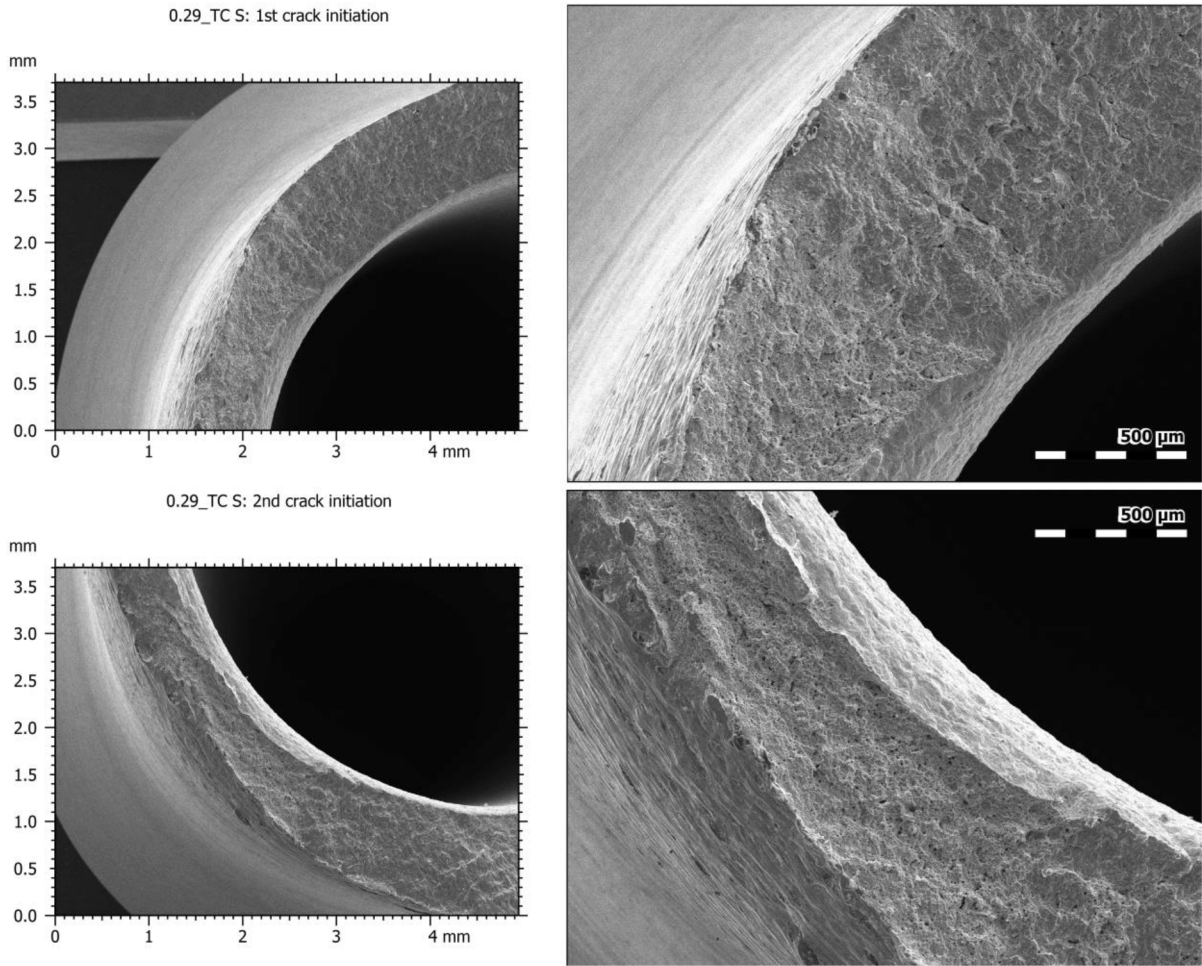


Fig. 11. SEM fractography for three different specimens shows crack initiation and final ductile fracture zones.

of surface topology features. On the contrary, for the final rupture area, the profiles are different, and the roughness is higher which can be explained by the higher fatigue crack growth rates.

Fig. 11 shows that the material exhibited the typical mechanisms associated to fatigue loading, such as traces of plastic deformation and ductility with evidence of microvoids (see black points in Fig. 11). It is also visible, particularly in the fatigue crack initiation regions, some river patterns with radial convergence to the initiation sites as well as the presence of secondary cracks of variable length. In the final rupture region, the pictures reveal more tortuous paths which are caused by the higher fatigue crack growth rates at this stage of propagation.

## 5. Conclusions

The post-failure fracture surface behavior of thin-walled tubular X5CrNi18-10 austenitic steel specimens subjected to asynchronous axial-torsional fatigue loading has been herein investigated. Pure axial and pure torsional loading were analyzed to better understand the effect of multi-axiality on fracture surface topology parameters. It was found that the loading path significantly affects the surface topography. Thanks to this, it is possible to read from it how a given element has been damaged. On the other hand, it also allows the development of a model for determining the fatigue life of materials subjected to multi-axial asynchronous loading based on the fracture surface parameters, which is an important outcome. There is one additional benefit from implementing this method, the ability to read the fracture mechanisms. In more detail, the results of the present study suggest the following:

- The analysis of the fracture topography parameters, especially  $R_q$ , based on the profiles over the entire fracture surface, demonstrated that their values increase with higher values of the fatigue life  $N_f$ ;
- The fracture surface topology parameters collected from both sides of the same specimen led to comparable results which reinforces the applicability of the proposed approach;

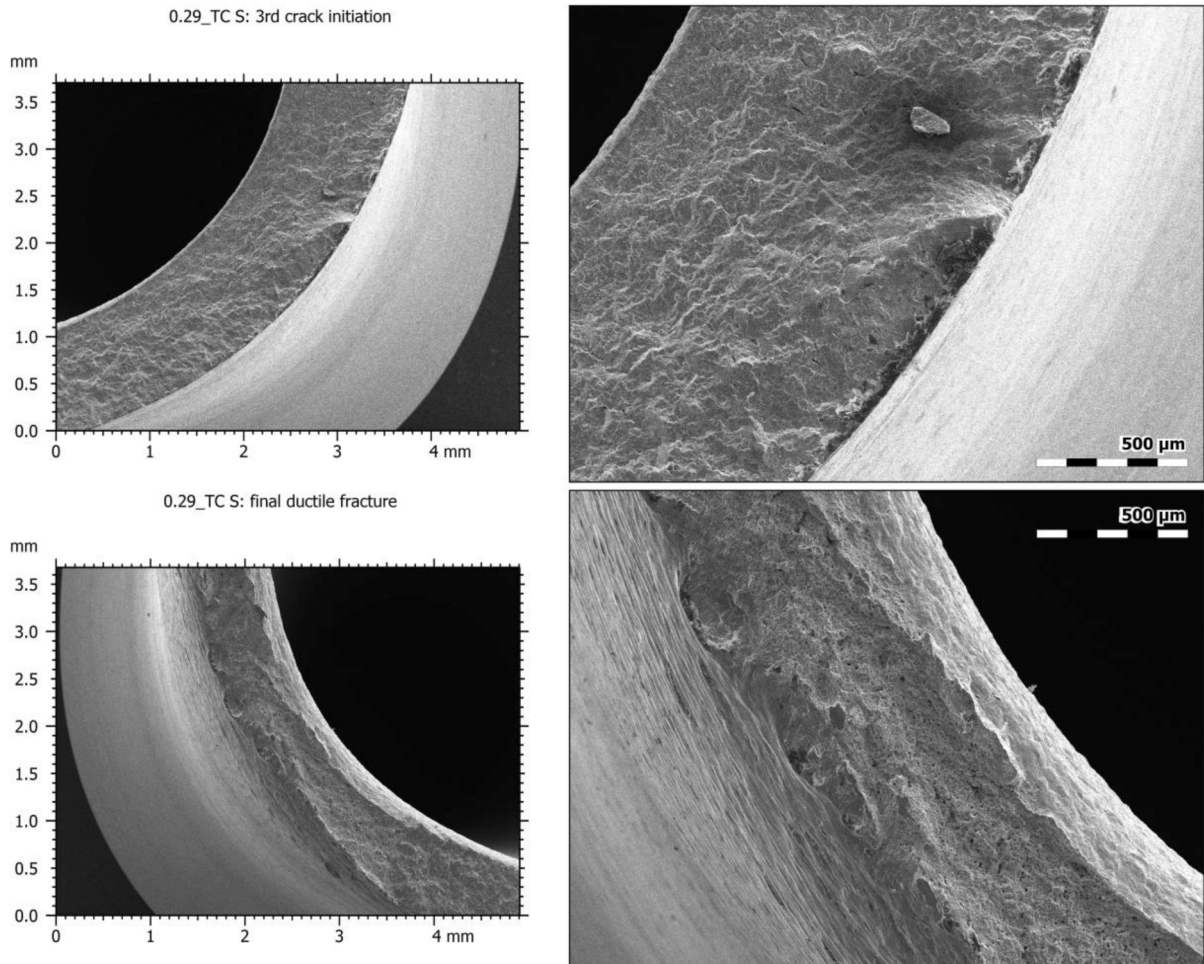


Fig. 11. (continued).

- The proposed fatigue damage model based on the  $R_q$  parameter was capable to estimate the fatigue life for the tested multiaxial asynchronous loading cases with a quite good compliance;
- The fractographic analysis of characteristic zones associated with the fatigue phenomenon showed differences failure mechanisms in the initiation region and the propagation region.

#### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

#### Acknowledgements

The surface topography data were processed using the Mountains® software courtesy of Digital Surf, France.

#### Appendix A

Original profiles for both sides of each specimen are presented in Fig. A1. The letters “L” and “S” in the descriptions indicate the “long” and the “short” side of the broken specimen, respectively. The extracted profiles are provided below the isometric views of the fracture surface of each both broken part of the specimens for comparison.



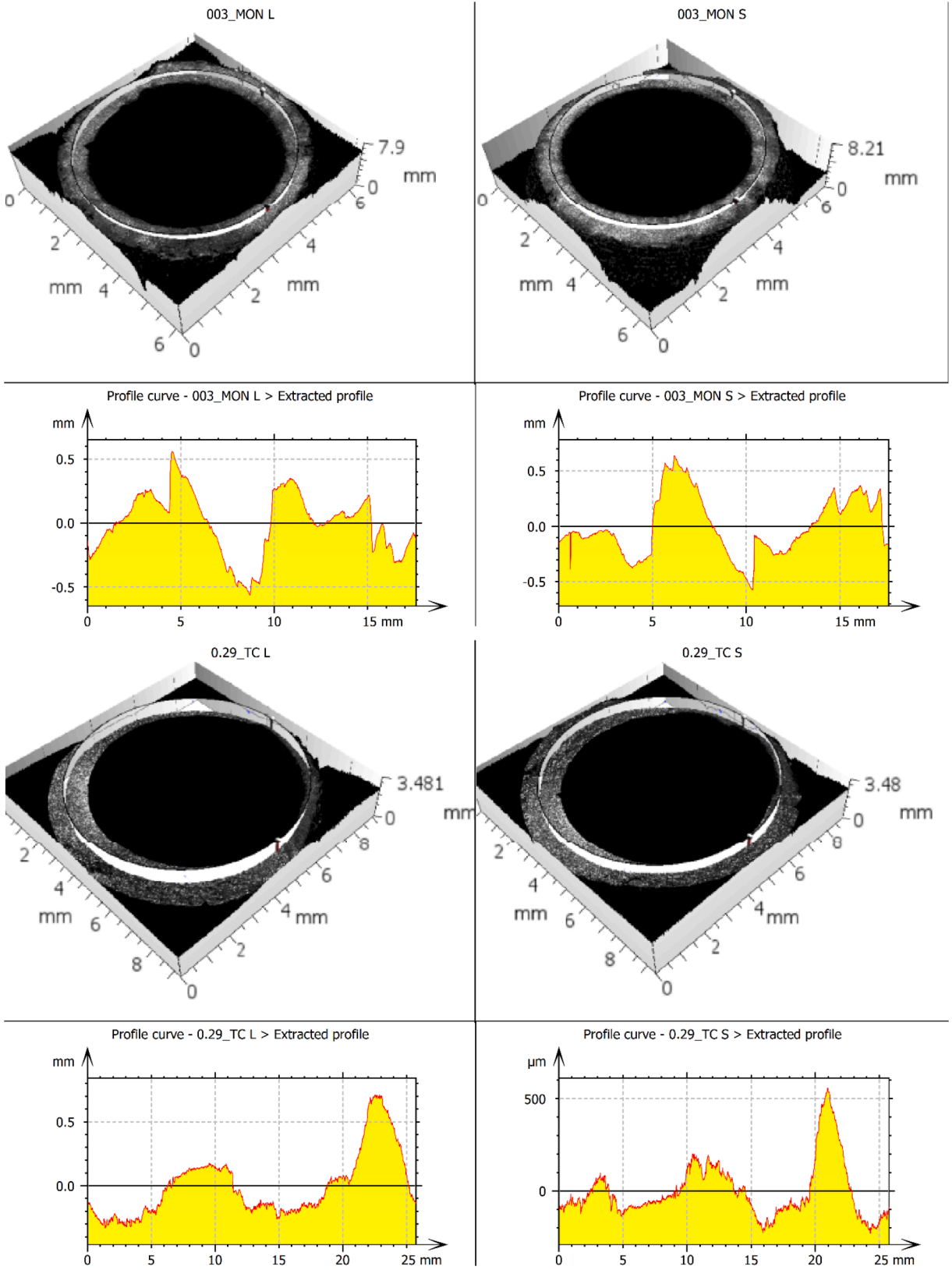


Fig. A1. Original profiles for both sides of each specimen.

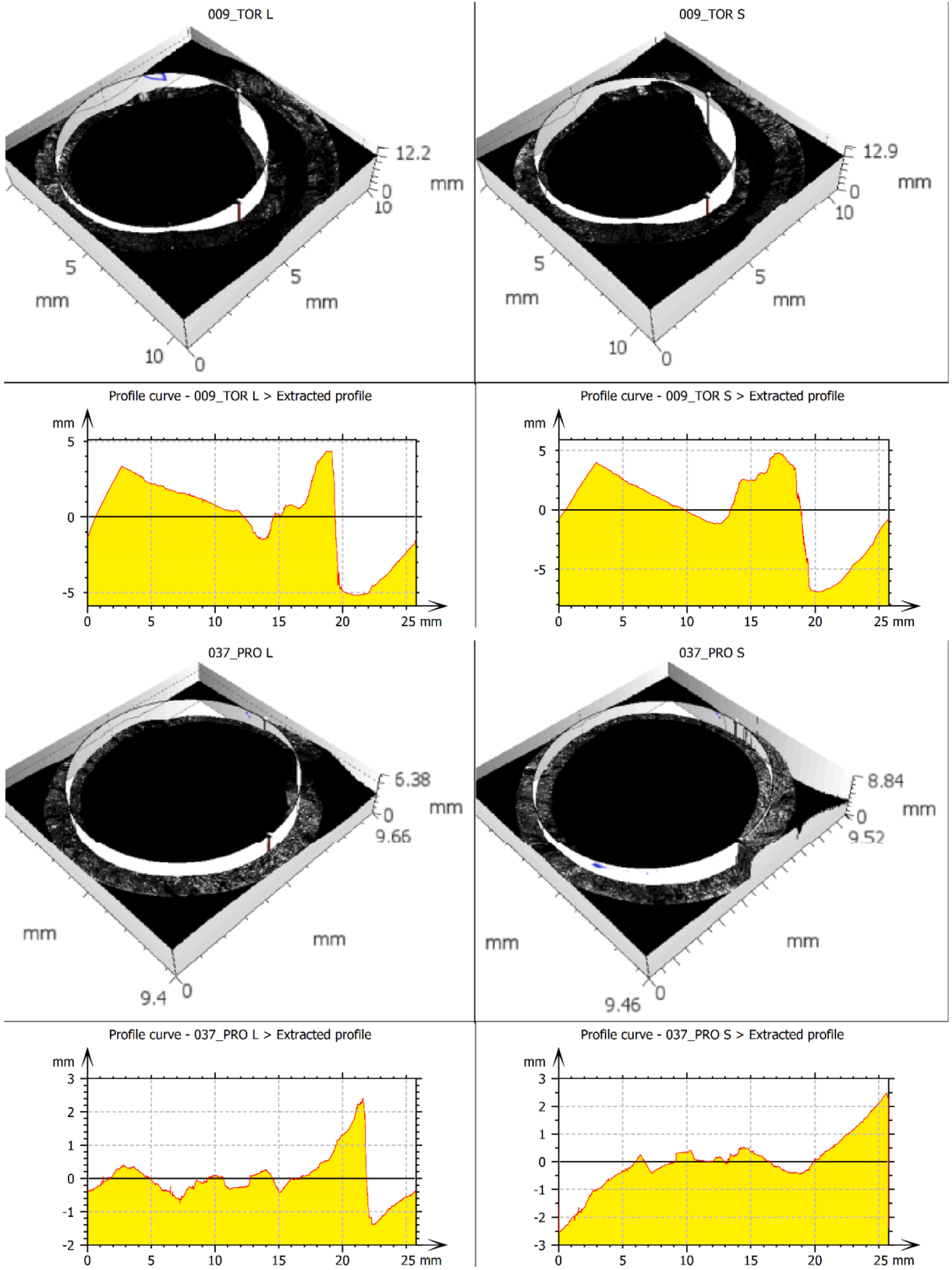


Fig. A1. (continued).

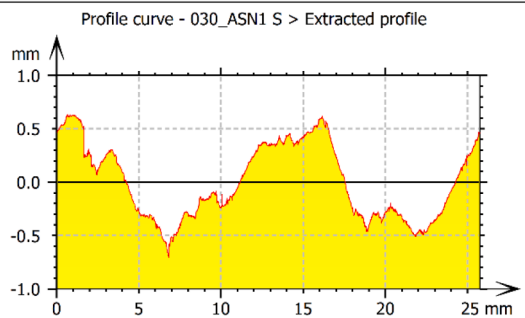
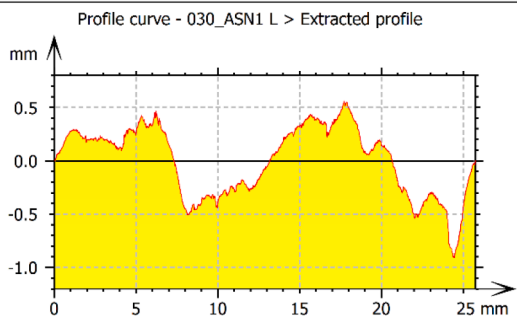
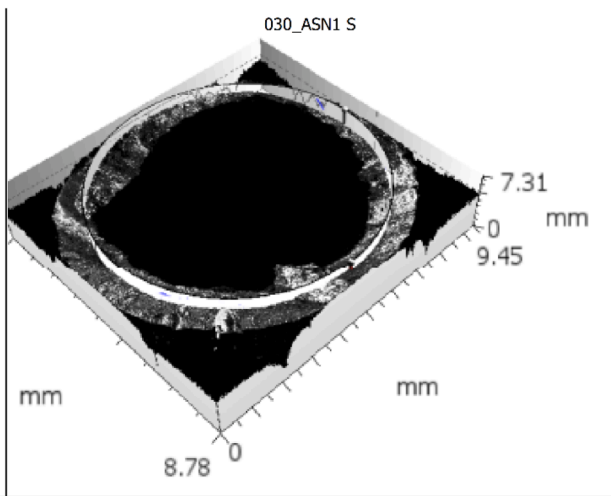
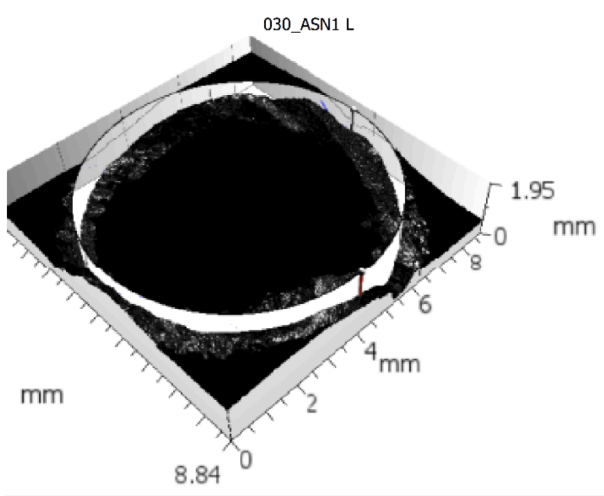
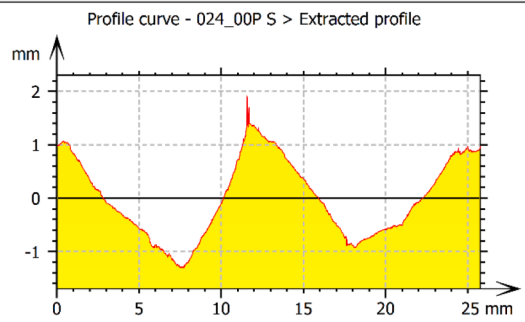
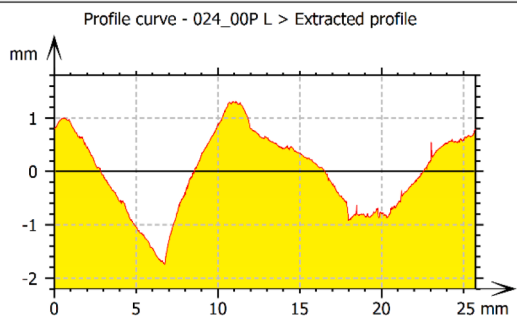
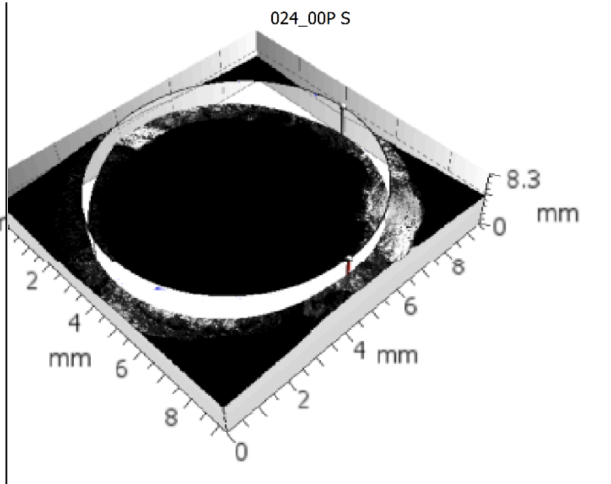
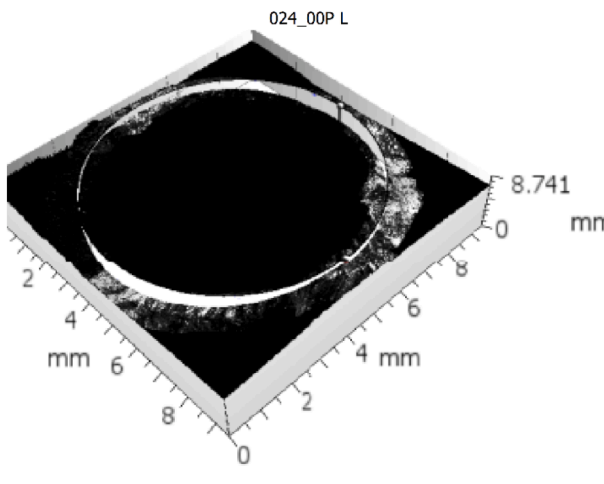


Fig. A1. (continued).

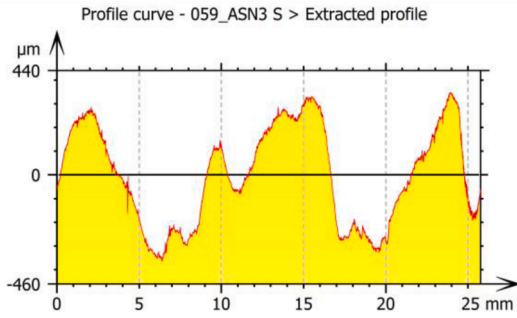
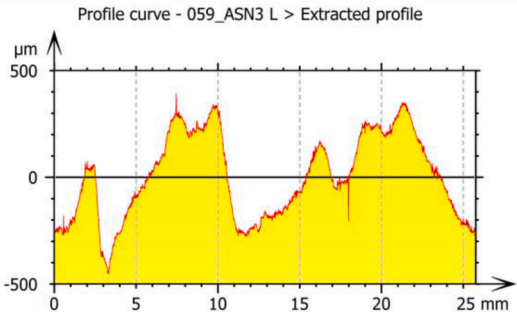
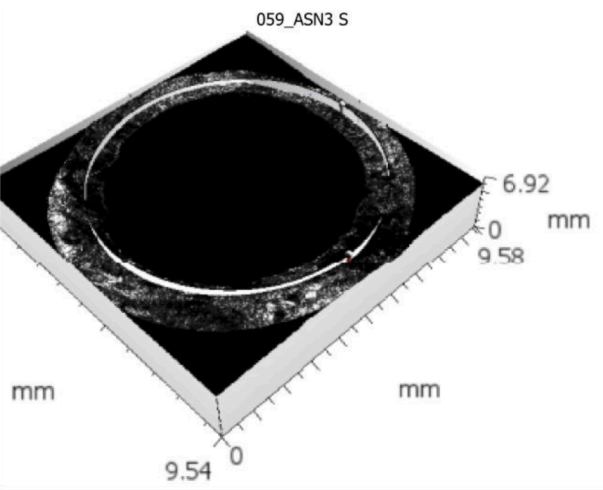
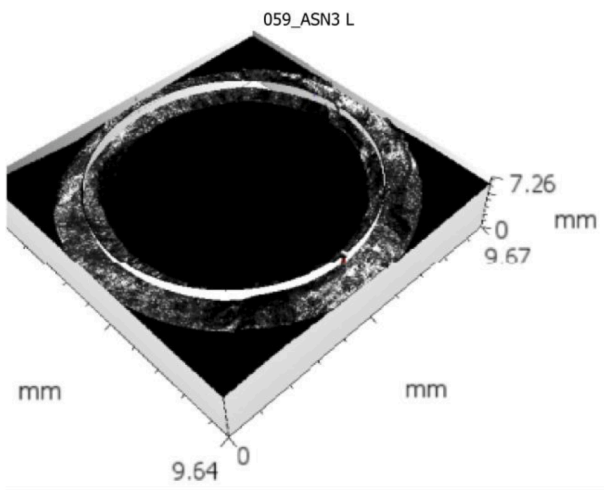
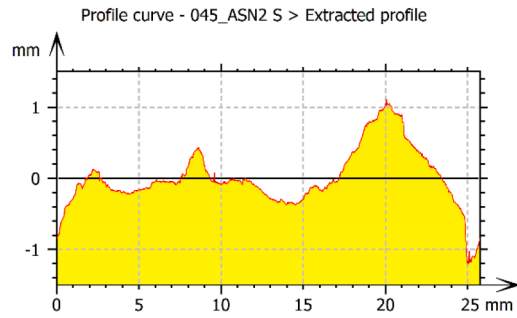
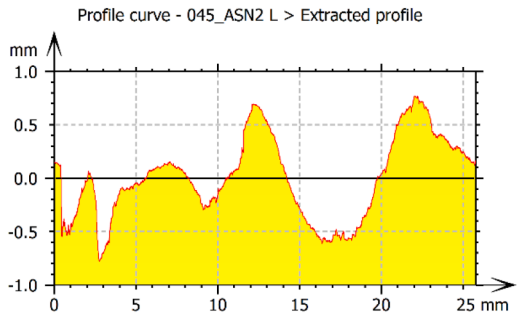
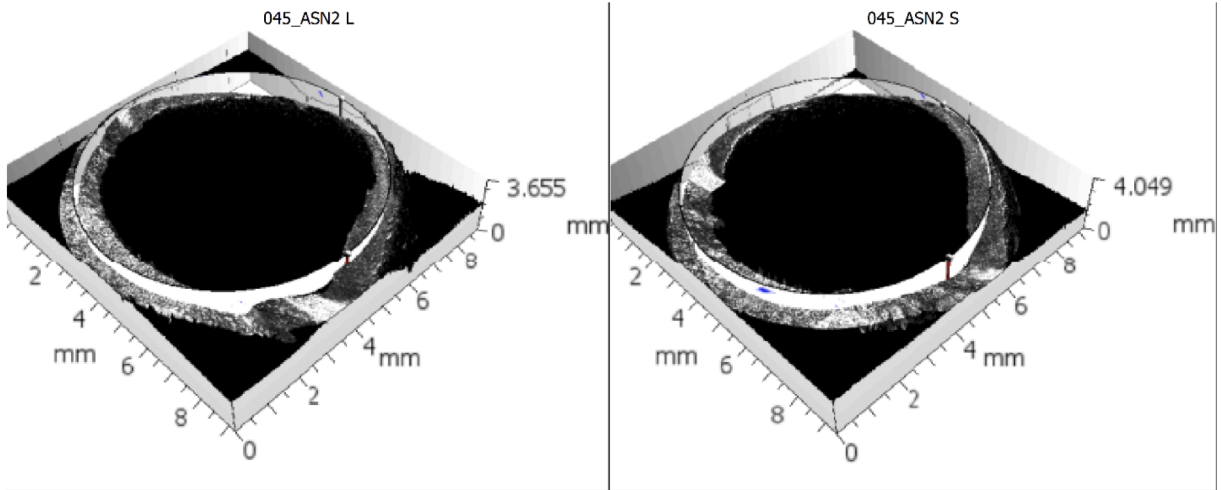


Fig. A1. (continued).

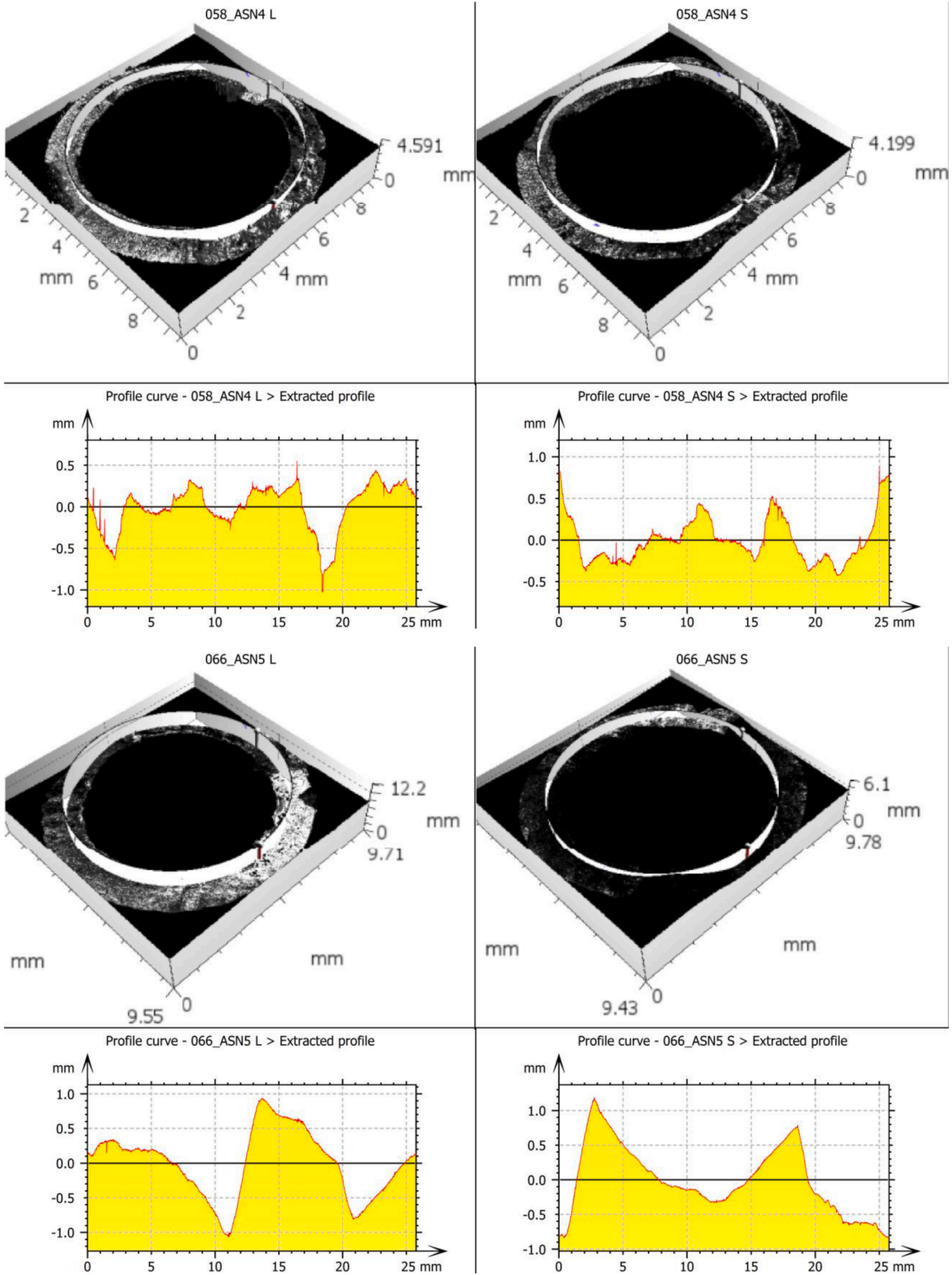


Fig. A1. (continued).



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