







Article

Study on the Positioning Accuracy of the GNSS/INS System Supported by the RTK Receiver for Railway Measurements

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Abstract: Currently, the primary method for determining the object coordinates is positioning using Global Navigation Satellite Systems (GNSS) supported by Inertial Navigation Systems (INS). The main goal of this solution is to ensure high positioning availability, particularly when access to satellite signals is limited (in tunnels, areas with densely concentrated buildings and in forest areas). The aim of this article is to determine whether the GNSS/INS system supported by the RTK receiver is suitable for the implementation of selected geodetic and construction tasks in railway engineering, such as determining the place and extent of rail track deformations (1 cm ($p = 0.95$)), the process of a rapid stocktaking of existing rail tracks (3 cm ($p = 0.95$)) and for design and construction works (10 cm ($p = 0.95$)), as well as what the impact of various terrain obstacles have on the obtained positioning accuracy of the tested system. During the research, one INS was used, the Ekinox2-U by the SBG Systems, which was supported by the Real-Time Kinematic (RTK) receiver. GNSS/INS measurements were conducted on three representative sections varying in terms of terrain obstacles that limit the access to satellite signals during mobile railway measurements in Tricity (Poland). The acquired data allowed us to calculate the basic position accuracy measures that are commonly used in navigation and transport applications. On this basis, it was concluded that the Ekinox2-U system can satisfy the positioning accuracy requirements for rapid stocktaking of existing rail tracks (3 cm ($p = 0.95$)), as well as for design and construction works (10 cm ($p = 0.95$)). On the other hand, the system cannot be used to determine the place and extent of rail track deformations (1 cm ($p = 0.95$)).

Keywords: positioning accuracy; Global Navigation Satellite System (GNSS); inertial navigation system (INS); Real-Time Kinematic (RTK); railway measurements



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1. Introduction

Mobile Global Navigation Satellite System (GNSS) measurements in railway engineering were initiated by Cezary Specht and Władysław Koc in 2009 [1] during an inventory of a railway route on a section between Kościerzyna and Kartuzy (Poland) [2]. The study used four GNSS geodetic receivers and Aktywna Sieć Geodezyjna EUPOS (ASG-EUPOS), a newly-established GNSS geodetic network (the first in Poland). The results of this campaign confirmed the high applicability of this measurement method and showed the limitations of the GNSS signal availability in built-up areas. During subsequent studies, a continuous increase was noted in terms of the accuracy and availability of mobile satellite measurements, resulting primarily from the improvement in operational and technical characteristics of the two main GNSS systems (Global Positioning System (GPS) and GLOBal Navigation

Satellite System (GLONASS)), the construction of other GNSS systems (BeiDou Navigation Satellite System (BDS) and Galileo), the development of new methods for generating correction data (Real Time Network (RTN)) and the establishment of new GNSS geodetic networks in Poland (SmartNet, TPI NETpro and VRSNet.pl). Starting from the first measurement campaign, the study was conducted in two main directions, i.e., geodetic, which involved increasing the positioning accuracy and availability of mobile GNSS measurements, as well as design, which aimed at developing new design and operational methods [3]. The research was culminated by the implementation of a research project entitled “Development of an innovative method for determining the precise trajectory of a railway vehicle” (InnoSatTrack) in the years 2018–2021. The aim of this project was to develop an innovative method for determining the rail track axis trajectory using mobile photogrammetric methods, GNSS, Inertial Navigation System (INS) and 3D laser scanning [4–6]. The obtained results will be used to more efficiently reproduce the coordinates of the existing rail track infrastructure [7–9]. Another purpose of the study was to develop methods for more accurate positioning/locating railway vehicles in real-time (the position and velocity) using GNSS/INS systems [3]. The final aim of the project was to develop a data acquisition and processing system from all measurement systems [10]. The system was implemented into an online application based on the most recent technology for handling the following layers: business, database access and presentation.

Worldwide research results indicate that an increase in the number of measurement systems and their variability in terms of methods leads to an improvement in the precision of determining the course of a rail route, as well as its modelling [11–15]. In order to determine this clearly, in the years 2009–2021, the authors of this article assessed the availability of three accuracy levels: deformation (1 cm ($p = 0.95$)), stocktaking (3 cm ($p = 0.95$)) and design (10 cm ($p = 0.95$)), that were required to perform various construction and geodetic tasks in railway engineering [16]. Since the individual tasks realized in railway engineering have different positioning accuracy requirements, it is important to know which GNSS/INS system is suitable for what task. Hence, it was decided to determine the usefulness of the GNSS/INS system supported by the Real-Time Kinematic (RTK) receiver for railway measurements.

For several years now, GNSS/INS systems have been increasingly used in railway applications. Chen et al. [17] used these systems to study the railway track irregularity for high-speed lines. This made it possible to identify the railway track irregularity with a relative accuracy of 1 mm. Similar tests and results were carried out by Li et al. [18], during which they obtained that the accuracy of the deformation monitoring is 1 mm in the horizontal plane and 1.5 mm in the vertical plane. Other studies were conducted by Zhang et al. [19]. On their basis, they observed that the accuracy of the railway track irregularity is 0.67 mm (Root Mean Square (RMS)) and 0.16 mm (relative error). Zhou et al. [15] performed kinematic measurements of the railway track centerline position using multisensor data fusion from GNSS, INS and an odometer. Research has shown that errors do not exceed 0.6 cm in the horizontal plane and 1.1 cm in the vertical plane. Data fusion from different sensors is also used by other authors. Thanks to the data from GNSS, INS and an odometer, Zhang et al. [20] were able to determine the geometrical parameters of railway tracks with an accuracy of 0.2 mm. GNSS/INS systems are also tested in places where there is no access to GNSS signal reception. Reimer et al. [21] used data from GNSS, INS and an odometer to determine the railway track axis position for a tunnel with a length of 57 km. Measurements carried out indicated that the position error did not exceed 15 m. Inertial navigation systems are commonly used in navigation and transport applications. The most important of them include: tests using Autonomous Ground Vehicles (AGV) [22–24], Unmanned Aerial Vehicles (UAV) [25–27] and Unmanned Surface Vehicles (USV) [28,29]; locating mobile phones [30], indoor [31], terrestrial [32] and space [33]; navigation, geodetic [34–36] and hydrographic surveys [37–39]; and rail transport [40,41] and road transport [42–44]. Moreover, they are used in the case of preventing intentional interference [45,46] and in urban areas in which the multipath effect occurs [47–49].

At the beginning of the 21st century, the establishment of active national networks by the geodetic authorities of individual countries intended to offer the users services, either for a fee or free of charge (including in real-time), became the dominant global trend [50]. Among the most commonly used positioning methods may include the RTK and RTN techniques. The main difference between them is that for the RTK method, the correction data are compiled exclusively on the basis of registrations from a single reference station, while, for the RTN method, observations from at least a few reference stations are used. Another advantage of the RTN technique is that the coordinate positioning accuracy does not decrease with the distance from the reference station so that the results are not inferior to those obtained by the RTK technique [51]. GNSS geodetic networks are primarily used in agriculture and forestry, engineering construction, geodesy and geodynamics [52,53], hydrography and hydrology [54,55], metrology [56], navigation and transport applications [57–59], as well as spatial information systems [60,61]. Moreover, work is currently underway to determine the position coordinates with high accuracy in areas with numerous terrain obstacles [62,63].

For the above reasons, the aim of this article is to determine whether the GNSS/INS system supported by the RTK receiver is suitable for the implementation of selected geodetic and construction tasks in railway engineering, such as determining the place and extent of rail track deformations (1 cm ($p = 0.95$)), the process of a rapid stocktaking of existing rail tracks (3 cm ($p = 0.95$)) and for design and construction works (10 cm ($p = 0.95$)), as well as what the impact of various terrain obstacles have on the obtained positioning accuracy of the tested system. To achieve this goal, the publication should be divided as follows: Section 2 describes the measurement equipment (inertial navigation system manufactured by the SBG Systems) that was used when carrying out the GNSS/INS surveys (including its calibration and configuration). Moreover, the section presents the method for conducting GNSS/INS measurements and specifies how the data recorded during the study were processed. Section 3 specifies the accuracy characteristics of the GNSS/INS system on three representative sections varying in terms of terrain obstacles that limit the access to the GNSS signal. It then discusses whether the system used is suitable for the purposes of railway measurements. The paper concludes with final (general) conclusions that summarise its content.

2. Materials and Methods

2.1. Measurement Equipment

As part of the InnoSatTrack research project, on 9 June 2021, surveys were conducted in Tricity. One of the aims was to determine the usefulness of GNSS/INS systems for railway measurements. To this end, one inertial navigation system was used: Ekinox2-U by the SBG Systems, which is comprised of the following components: an Inertial Measurement Unit (IMU) (Figure 1a); two antennas: an AERO GPS and GNSS Survey Antenna AT1675-382 (Figure 1b); a SplitBox computer system (Figure 1c); a modem enabling the reception of RTK/RTN corrections (Figure 1d); sbgCenter software (Figure 1e); and Qinertia software (Figure 1f) [64,65].

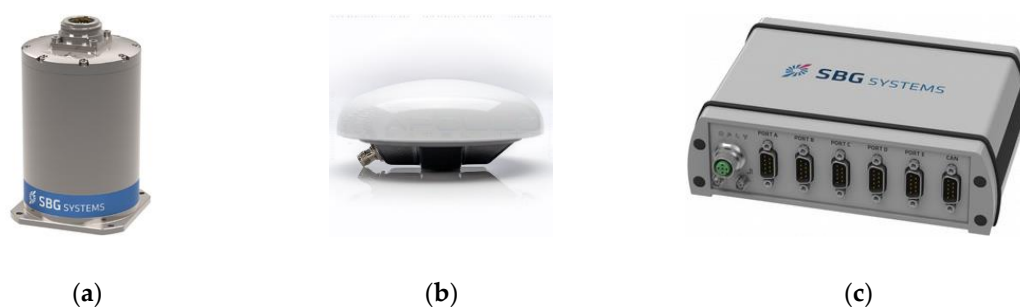


Figure 1. Cont.

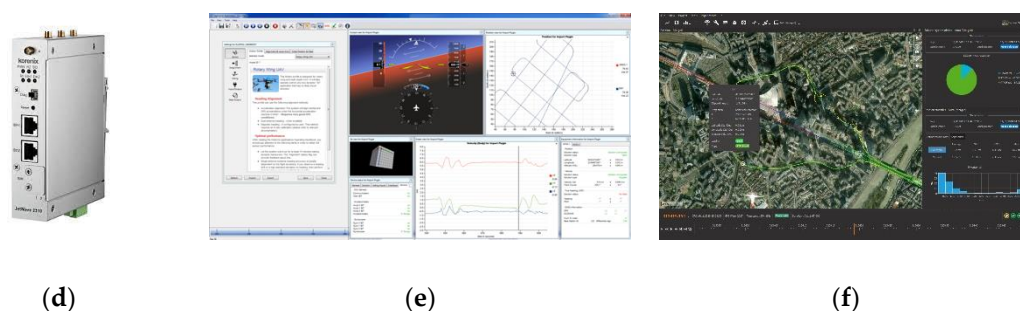


Figure 1. Components of the GNSS/INS system, model Ekinox2-U, by the SBG Systems: IMU (a), GNSS antennas (b), SplitBox computer system (c), modem enabling the reception of RTK/RTN corrections (d), sbgCenter software (e) and QInertia software (f) [64,65].

Moreover, the GNSS/INS system has functions which are important for the purpose of carrying out railway measurements [64,65]:

- The Ekinox2-U system enables operation in two modes:
 - Post-Processing (PP)—post-processed data using Inertial Explorer (IE) with at least Precise Point Positioning (PPP) data;
 - RTK—Real-Time Kinematics with a typical 1 cm accuracy position.
- The recording frequency for the data on angles, accelerations and position coordinates should be as high as possible. It is recommended that the IMU's data should be recorded with a max frequency of 200 Hz.

As regards the accuracy characteristics of the GNSS/INS system, model Ekinox2-U are presented in Table 1 [65]. Note that the GNSS/INS system can be successfully used to carry out selected construction and geodetic tasks in railway engineering. As regards the access to the GNSS signal, it can be used (in both RTK and PP modes) to determine the rail track deformations. Based on the GNSS research conducted in the years 2009–2021 on railway lines [16], the authors assumed that the max horizontal position error for this group of measurements was no more than 1 cm. However, in the event of GNSS signal loss (up to 10 s), the Ekinox2-U system can be used in the process of a rapid stocktaking of existing rail tracks (3 cm ($p = 0.95$)).

Table 1. Accuracy characteristics of the GNSS/INS system, model Ekinox2-U, by the SBG Systems [65].

RMSE	Time That Has Elapsed Since the GNSS Signal Was Not Available					
	0 s		10 s		30 s	
	RTK	PP	RTK	PP	RTK	PP
2D position (m)	0.010	0.010	0.350	0.030	4.000	1.500
Height (m)	0.020	0.020	0.150	0.030	0.500	0.500
Pitch, roll (°)	0.050	0.020	0.100	0.020	0.150	0.040
Course (°)	0.050	0.040	0.100	0.050	0.150	0.070

2.2. Calibration and Configuration of the GNSS/INS System

Before the measurements are started, the GNSS/INS system needed to be configured. To this end, a 6-metre metal support structure was used, on which the following were installed: an IMU, two external GNSS antennas (“Primary” and “Secondary”) mounted on geodetic tribrachs, a SplitBox system and a modem enabling the reception of RTK/RTN corrections (Figure 2). According to the SBG Systems manufacturer’s recommendations, it was established that the distance between the GNSS antennas would be 5 m (it should be at least 4 m in order to ensure an accurate course measurement of a vehicle in motion). The



IMU was placed at the centre of the section connecting the two GNSS antennas, while the SplitBox system and the modem were also mounted on the metal support structure but between the “Secondary” antenna and the IMU.

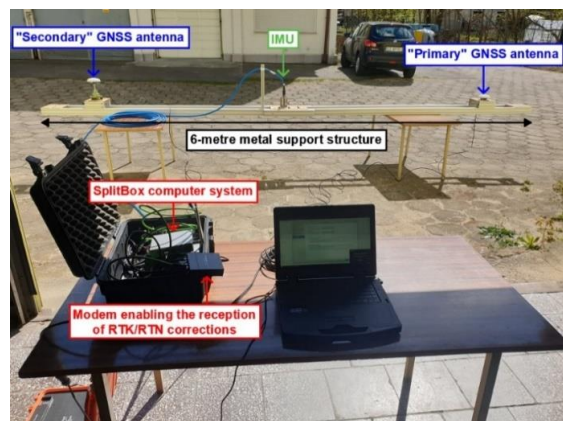


Figure 2. The arrangement of the GNSS/INS system on the metal support structure.

In the next stage, it was possible to perform the GNSS/INS system calibration in motion. To this end, a Melex electric vehicle was used, on which a metal support structure was installed along with the tested inertial navigation system (Figure 3a). Before starting the calibration of the inertial navigation system, several parameters of the GNSS/INS system had to be set in the sbgCenter software, including, inter alia, the movement profile. Given the nature of the railway measurements, it was decided to select the “Automotive” mode dedicated to vehicle applications, i.e., those in which there are slight (slow) changes in the movement direction and the object’s velocity is less than 3 m/s. In addition, it was necessary to determine the axis orientation of the GNSS/INS system. A left-handed orthogonal coordinate system was adopted, whose zero point was present on the IMU’s cover. The axes of the system were oriented in such a way that the x -axis ran towards the front of the Mobile Measurement Platform (MMP), the y -axis was oriented towards the left side of the platform, while the z -axis ran towards the bottom part of the MMP. In order to be able to calibrate the inertial navigation system, it was necessary to determine the geometric relationships between the IMU and two GNSS antennas with an accuracy not worse than 20 cm. After performing the steps described above, the correctness of the performed GNSS/INS system configuration can be verified using the sbgCenter software (Figure 3b).

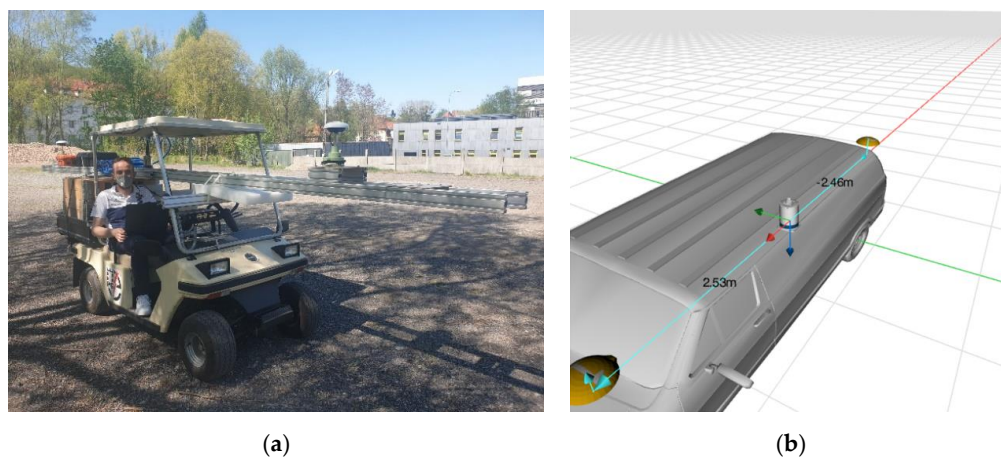
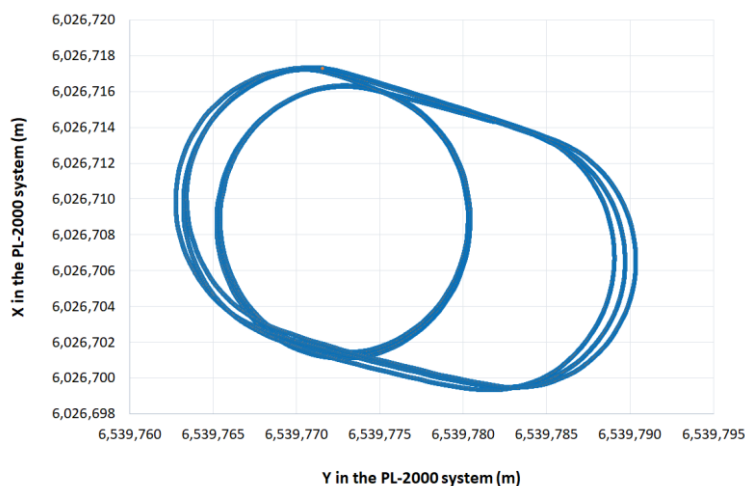
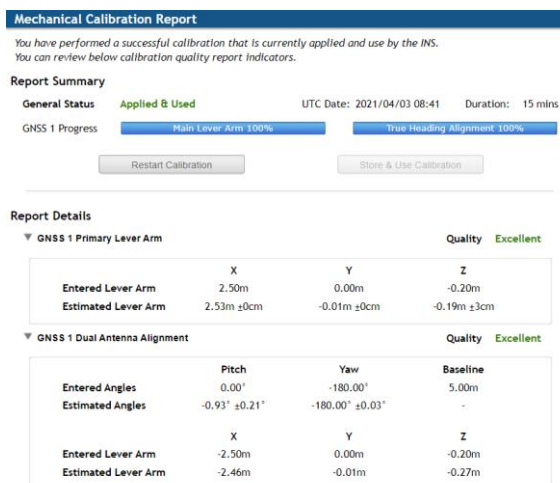


Figure 3. Melex electric vehicle used for the calibration of the GNSS/INS system (a) and the configuration window for the Ekinox2-U system in the sbgCenter software (b).

Then, it was possible to calibrate the GNSS/INS system. It is advised that the calibration should be carried out in motion for 15 min at an average speed of at least 10 km/h. Moreover, the movement direction needed to be constantly changed in order to calibrate all sensors such as accelerometers and gyroscopes. Movement in circles, ovals, or the so-called “eights” is recommended (Figure 4a). The calibration of the inertial navigation system was completed after 15 min of driving the Melex. During it, it was possible to precisely (from ± 0 cm to ± 3 cm) to determine the geometric relationships between the IMU and two GNSS antennas (Figure 4b).



(a)



(b)

Figure 4. Melex movement trajectory (a) and the results of the Ekinox2-U system calibration (b) of 19 May 2021.

After saving the above settings, the railway measurement campaign within Tricity was commenced in an unchanged form.

2.3. Location of GNSS/INS Measurements

Upon completion of the installation and implementation works, a measurement campaign was carried out on the rail tracks located in Tricity on the following lines: LK9 (Gdańsk Południe-Gdańsk Główny), LK202 (Gdańsk Główny-Gdańsk Wrzeszcz), LK248 (Gdańsk Wrzeszcz-Gdańsk Osowa) and LK201 (Gdańsk Osowa-Gdynia Główna). Due to the heavy traffic on the above routes and the necessity to adapt to the timetable, the data were recorded in sections of a considerable length. The few stops of the MMP were used to control and monitor the GNSS/INS data recording. The measurement sections, also referred to as sessions, are shown in Figure 5. During the stops at the railway stations Gdańsk Wrzeszcz and Gdańsk Osowa, the measurements were conducted in the stationary mode. On the other sections, the recording was carried out in the kinematic mode used for the purposes of this paper.

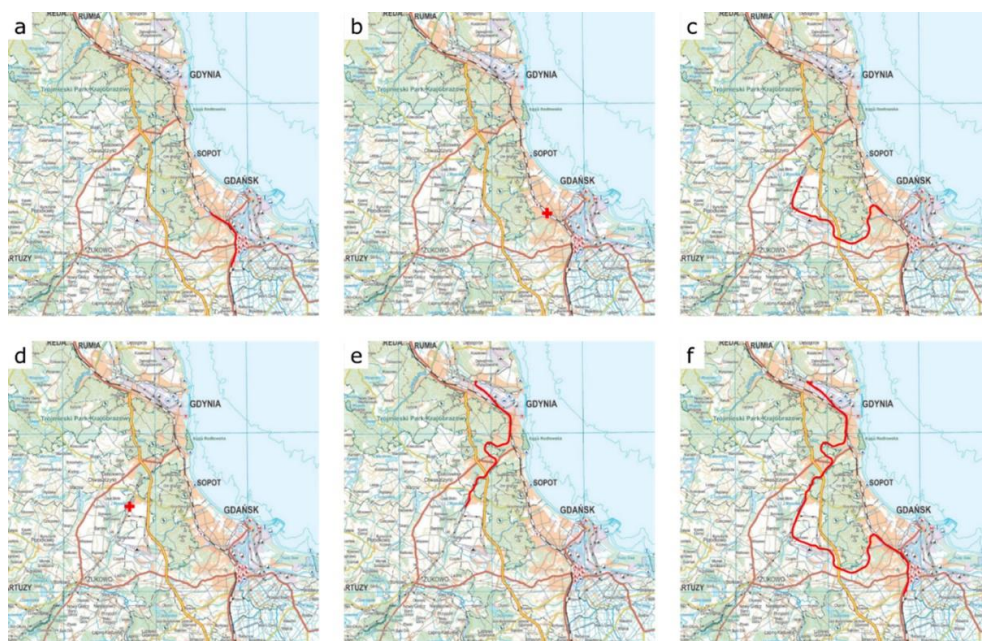


Figure 5. Sections of the GNSS/INS data recording in the kinematic mode: Gdańsk Południe-Gdańsk Wrzeszcz (a), Gdańsk Wrzeszcz-Gdańsk Osowa (c), Gdańsk Osowa-Gdynia Chylonia (e) and Gdynia Chylonia-Gdańsk Południe (f), as well as in the stationary mode: Gdańsk Wrzeszcz (b) and Gdańsk Osowa (d).

2.4. Realization of GNSS/INS Measurements

The measurement platform was separated from the towing vehicle by an additional empty carriage, which minimised the impact of terrain obstacles (in that case, the locomotive cab) on the recording of satellite data in the AERO GPS and GNSS Survey Antenna AT1675-382 receivers (Figure 6a). In the middle part of the carriage, the GNSS/INS system was installed on the metal support structure. At both the front and the rear of the MMP, a single metal support structure was mounted, on which three Trimble R10 receivers along with geodetic tribrachs were located. Meanwhile, the controllers that regulate GNSS receiver operation were placed in two yellow boxes (Figure 6b). During this mobile measurement campaign, the geodetic receivers were intended to be used to assess the usefulness of navigation satellite systems for application in rail transport.



Figure 6. MMP (a) with the equipment used (b) during the railway measurement campaign conducted on 9 June 2021.

2.5. Processing of GNSS/INS Data

The recorded GNSS/INS data were elaborated in the PP mode using the Qinertia software [66]. In order to carry out calculations, it was necessary to acquire synchronous satellite data from the nearest reference station located in Gdańsk (marked as GDSK), being part of the GNSS geodetic network VRSNet.pl of 9 June 2021, from the GPS time period from 05:00:00 to 15:00:00. The observation files are made available in the Receiver Independent Exchange System (RINEX) format [67] and contain observations from satellites of the GPS, GLONASS and Galileo systems recorded by the station's receiver with a frequency of 1 Hz. It was then necessary to enter the input parameters that were determined during the calibration of the GNSS/INS system. In turn, it was necessary to select one of the following three methods for processing data:

- Tight coupling Post-Processing Kinematic (PPK)—allows the highest GNSS/INS measurement accuracy to be obtained under conditions that are difficult in terms of satellite visibility. In order to be able to process GNSS/INS data using this method, it is necessary to have IMU data, raw GNSS data and the data from the GNSS geodetic network reference station;
- Loosely coupling—enables the determination of the IMU's coordinates when no GNSS signal is available. In order to be able to process GNSS/INS data using this method, it is necessary to have IMU data and the data from the GNSS geodetic network reference station;
- PPK—allows the highest GNSS measurement accuracy to be obtained under conditions that are difficult in terms of satellite visibility. In order to be able to process GNSS data using this method, it is necessary to have raw GNSS data and the data from the GNSS geodetic network reference station.

Processing the GNSS/INS data in the PP mode was followed by the selection of three representative measurement sections on the Gdańsk-Gdynia route. They were selected in such a manner so as to enable the assessment of the Ekinox2-U system's accuracy in sections varying in terms of terrain obstacles that limit the access to the GNSS signal:

- Section no. 1 (no terrain obstacles) was located on the railway line between the Radunia-Containers Ltd. in Gdynia and the Trasa Kwiatkowskiego (Figure 7a). Section no. 1 was approx. 2 km long. The measurement travel comprised long (several hundred metres), straight sections surrounded by virtually no terrain obstacles, the only exceptions being containers and bushes. The passage was performed on 9 June 2021 from 10:07:07 to 10:16:09 Coordinated Universal Time (UTC) (the duration of approx. 9 min).
- Section no. 2 (high building density) was located on the railway line between the Gdynia Główna railway station and the Gdańsk Osowa railway station (Figure 7b). Section no. 2 was approx. 15 km long. The measurement travel comprised circular curves with large turning angles. The second test section ran through numerous terrain obstacles, including multi-storey buildings and trees more than a dozen metres high. The passage was performed on 9 June 2021 from 08:35:03 to 09:05:50 UTC (the duration of approx. 31 min).
- Section no. 3 (no access to GNSS signal) was located on the railway line in a tunnel in the centre of Gdańsk between the Gdańsk Śródmieście railway station and the Gdańsk Główny railway station (Figure 7c). Section no. 3 was approx. 600 m long. The measurement travel comprised a long circular curve with a small turning angle under the tunnel, where no GNSS signal was received. Two passages were performed on 9 June 2021 from 06:41:47 to 06:43:02 UTC (the duration of 75 s) and from 11:58:47 to 11:59:55 UTC (the duration of 68 s).

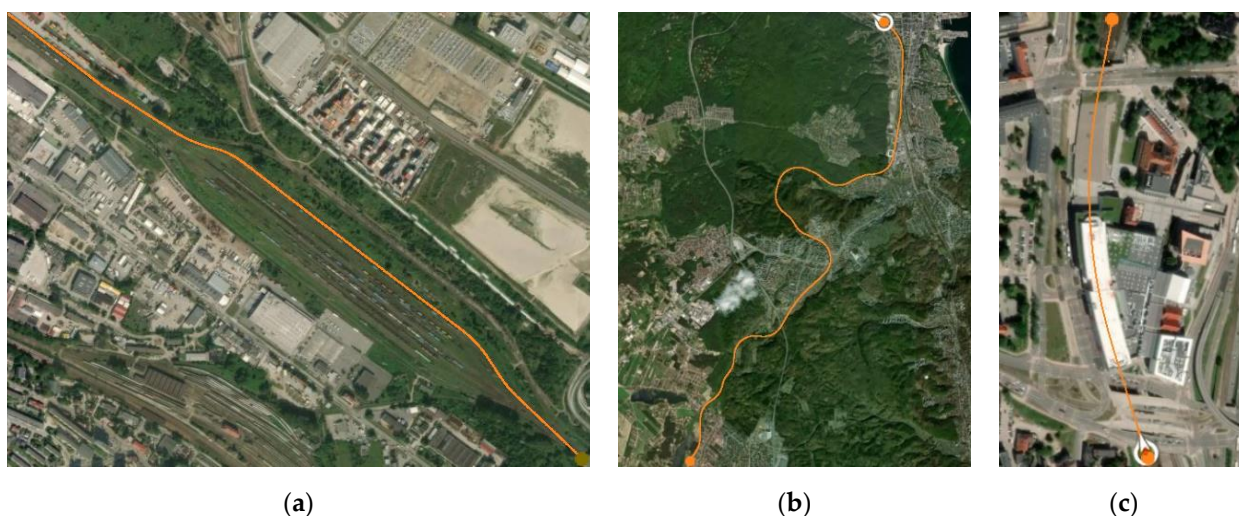


Figure 7. The division of the route into test sections: no. 1 (a), no. 2 (b) and no. 3 (c).

Each test section was subjected to an identical analysis of the obtained measurement results in order to formulate global conclusions. The IMU’s position errors were computed by the Qinertia software for two modes of the GNSS/INS system operation, i.e., PP and RTK. Subsequently, the errors were exported to text files. The files were then uploaded to the Mathcad software, where the position accuracy measures (RMS, Distance Root Mean Square (DRMS), Twice the Distance Root Mean Square (2DRMS), Circular Error Probable (CEP), Spherical Error Probable (SEP) and R68 and R95) were determined. From the perspective of navigation and transport applications linked to the process of controlling the object’s movement, the most important position accuracy measures are 2DRMS(2D) and R95(2D) [5,68].

3. Results

Table 2 shows the IMU’s position accuracy results obtained in section no. 1.

Table 2. Predictable accuracy of the Ekinox2-U system during the GNSS/INS measurements in section no. 1.

Statistics of Position Error	Type of Processing Data		Type of Registered Data
	RTK	PP	
Number of measurements	108,401	542	
RMS(ϕ)	0.019 m	0.007 m	
RMS(λ)	0.019 m	0.005 m	
RMS(h)	0.019 m	0.017 m	
DRMS(2D)	0.027 m	0.009 m	
2DRMS(2D)	0.054 m	0.018 m	
DRMS(3D)	0.033 m	0.020 m	
CEP(2D)	0.027 m	0.007 m	
R68(2D)	0.027 m	0.005 m	
R95(2D)	0.028 m	0.017 m	
SEP(3D)	0.033 m	0.009 m	
R68(3D)	0.033 m	0.018 m	
R95(3D)	0.035 m	0.020 m	

Note that the obtained position accuracy results in section no. 1 are higher for the data processed in the PP mode than for those processed in the RTK mode (Table 2). For example, the 2DRMS(2D) value is three times smaller for the data obtained in the PP mode (1.8 cm) than those obtained in the RTK mode (5.4 cm). What is more, the R95(2D) value is over

1.5 times smaller for the data acquired in the PP mode (1.7 cm) than those obtained in the RTK mode (2.8 cm).

Based on Figure 8, it should be stated that the variability of the 1D, 2D, and 3D position errors recorded in real-time is low along the entire section of the route. They fall within the following ranges: 1.8–2.3 cm (for the 1D position error), 2.6–2.9 cm (for the 2D position error) and 3.2–3.7 cm (for the 3D position error).

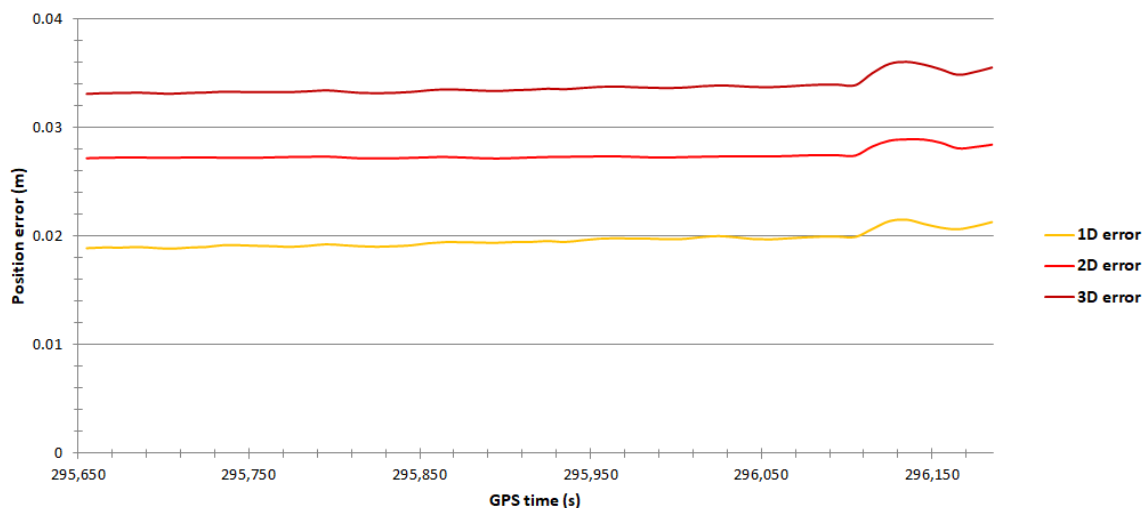


Figure 8. Variability in position errors recorded by the GNSS/INS system in the RTK mode in section no. 1.

Considerably lower values of the 1D position error (approx. 1 cm) can be observed for the data processed in the PP mode (Figure 9). This error is up to two times smaller than that for the data recorded in the RTK mode. Moreover, it is worth noting that the 2D position error values in the PP mode are slightly lower than those in the RTK mode. They virtually do not exceed the value of 3 cm, while in the second half of section no. 1, they range from 1 to 1.5 cm.

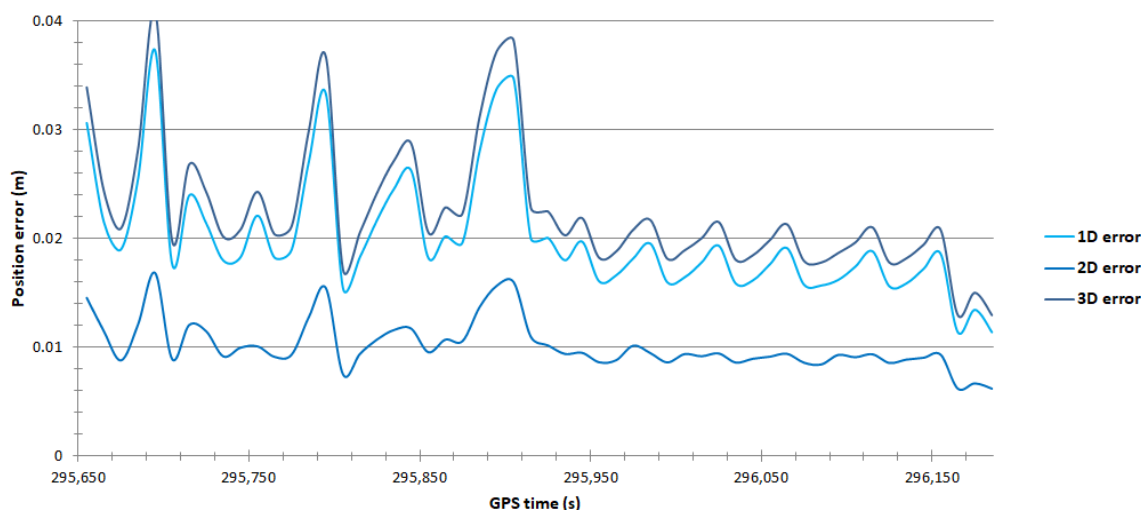
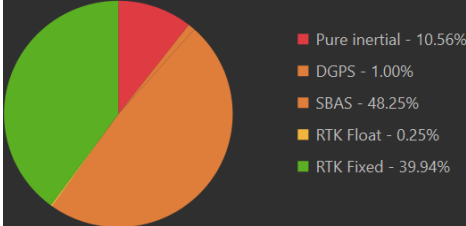


Figure 9. Variability in position errors recorded by the GNSS/INS system in the PP mode in section no. 1.

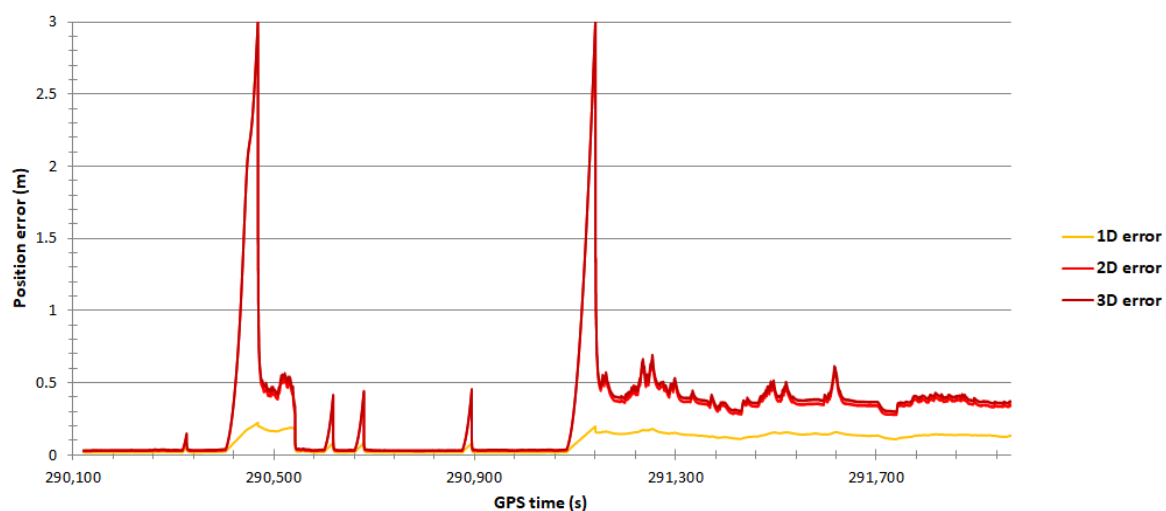
Table 3 shows the IMU's position accuracy results obtained in section no. 2.

Table 3. Predictable accuracy of the Ekinox2-U system during the GNSS/INS measurements in section no. 2.

Statistics of Position Error	Type of Processing Data		Type of Registered Data
	RTK	PP	
Number of measurements	369,401	369,401	 <ul style="list-style-type: none"> ■ Pure inertial - 10.56% ■ DGPS - 1.00% ■ SBAS - 48.25% ■ RTK Float - 0.25% ■ RTK Fixed - 39.94%
RMS(ϕ)	0.408 m	0.122 m	
RMS(λ)	0.254 m	0.109 m	
RMS(h)	0.107 m	0.099 m	
DRMS(2D)	0.481 m	0.163 m	
2DRMS(2D)	0.961 m	0.326 m	
DRMS(3D)	0.492 m	0.191 m	
CEP(2D)	0.324 m	0.175 m	
R68(2D)	0.364 m	0.197 m	
R95(2D)	0.600 m	0.246 m	
SEP(3D)	0.345 m	0.204 m	
R68(3D)	0.388 m	0.231 m	
R95(3D)	0.621 m	0.279 m	

Note that the obtained position accuracy results in section no. 2 are higher for the data processed in the PP mode than for those processed in the RTK mode (Table 3). For example, the 2DRMS(2D) value is three times smaller for the data obtained in the PP mode (32.6 cm) than those obtained in the RTK mode (96.1 cm). What is more, the R95(2D) value is over 2.5 times smaller for the data acquired in the PP mode (24.6 cm) than those obtained in the RTK mode (60 cm).

Figure 10 shows the high variability of the 2D and 3D position error values for the data recorded in the RTK mode, which is due to the type of terrain obstacles found along section no. 2. In the forested area (GPS time: 290,400–291,300 s) and the urbanised area (GPS time: 291,301–291,900 s), stepwise changes in the 2D and 3D position errors ranging from 0 to 3 m are noticeable. As regards the height accuracy, it also changes stepwise within the range from 0 to 20 cm.

**Figure 10.** Variability in position errors recorded by the GNSS/INS system in the RTK mode in section no. 2.

A considerably lower variability in the 2D and 3D position error values can be observed for the data processed in the PP mode (Figure 11). In the forested area, the 2D and 3D position errors range from 20 to 30 cm. On the other hand, in the urbanised area, the 2D and 3D position errors oscillate around 10 cm, with a few exceptions reaching 20 to 30 cm. As regards the height accuracy, it is definitely more stabilised than the 2D and 3D position errors. In the forested area, it ranges from 10 to 14 cm, while in the urbanised area, the 1D position error is approx. 6 cm.

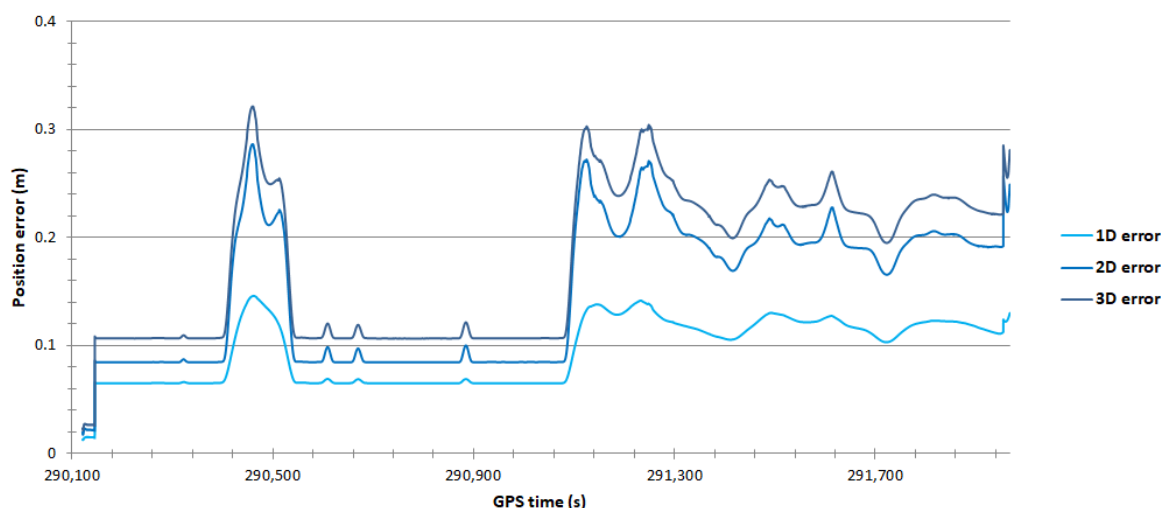


Figure 11. Variability in position errors recorded by the GNSS/INS system in the PP mode in section no. 2.

Table 4 shows the IMU’s position accuracy results obtained in section no. 3.

Table 4. Predictable accuracy of the Ekinox2-U system during the GNSS/INS measurements in section no. 3.

Statistics of Position Error	Type of Processing Data				Type of Registered Data
	First Trip		Second Trip		
	RTK	PP	RTK	PP	
Number of measurements	15,001	15,001	13,601	13,601	
RMS(ϕ)	2.904 m	0.305 m	2.376 m	0.236 m	
RMS(λ)	0.389 m	0.303 m	0.431 m	0.134 m	
RMS(h)	0.167 m	0.109 m	0.143 m	0.078 m	
DRMS(2D)	2.930 m	0.430 m	2.415 m	0.271 m	
2DRMS(2D)	5.860 m	0.859 m	4.829 m	0.543 m	
DRMS(3D)	2.935 m	0.443 m	2.419 m	0.282 m	
CEP(2D)	1.577 m	0.398 m	1.340 m	0.315 m	
R68(2D)	2.991 m	0.534 m	2.482 m	0.322 m	
R95(2D)	5.886 m	0.640 m	4.811 m	0.328 m	
SEP(3D)	1.584 m	0.413 m	1.347 m	0.325 m	
R68(3D)	2.998 m	0.548 m	2.487 m	0.335 m	
R95(3D)	5.891 m	0.655 m	4.816 m	0.340 m	

Note that the obtained position accuracy results in section no. 3 are considerably higher for the data processed in the PP mode than for those processed in the RTK mode

(Table 4). For example, the 2DRMS(2D) value is nearly 10 times smaller for the data obtained in the PP mode (54.3 and 85.9 cm) than those obtained in the RTK mode (4.829 and 5.86 m). Moreover, the R95(2D) value is a dozen or so times smaller for the data obtained in the PP mode (32.8 and 64 cm) than those obtained in the RTK mode (4.811 and 5.886 m).

Figure 12 shows the high variability in the 2D and 3D position error values for the data recorded in the RTK mode. During the second trip through the tunnel, the 2D and 3D position errors increased linearly with the time elapsed since the moment the access to the GNSS signal was lost. At the end of the tunnel, these errors reached a value of approx. 5 m. As regards the 1D position error, it increased definitely slower than the 2D and 3D position errors. At the end of the tunnel, the error reached a value of approx. 20 cm.

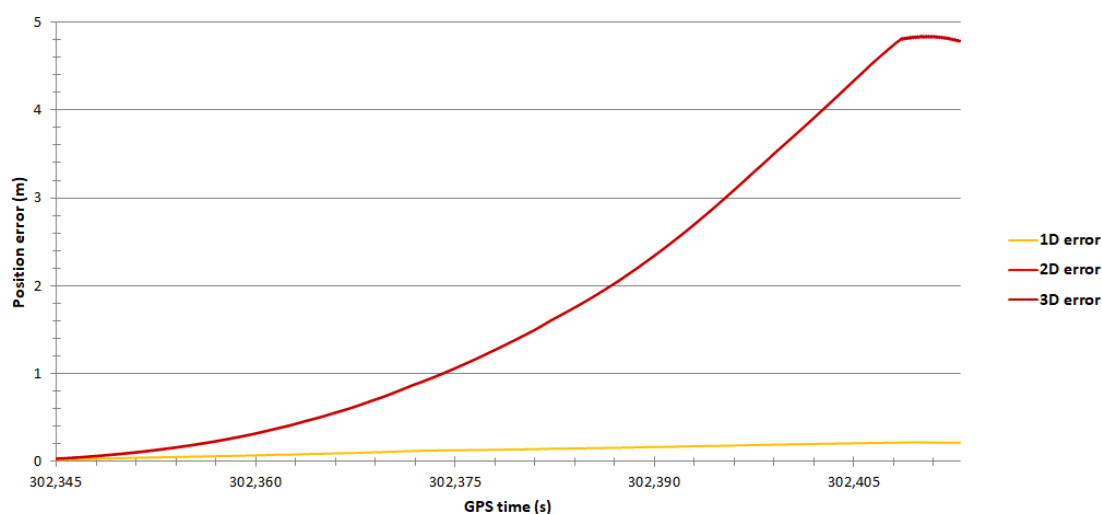


Figure 12. Variability in position errors recorded by the GNSS/INS system in the RTK mode in section no. 3.

It is worth noting that the position errors for the data processed in the PP mode are from a few to several times smaller than those for the data recorded in the RTK mode (Figure 13). For example, for approx. 15 s at both the entry to and exit from the tunnel, the 2D and 3D position errors increased from a few centimetres to over 30 cm. On the other hand, the 1D error ranged from 4 to 10 cm over the entire section of the route.

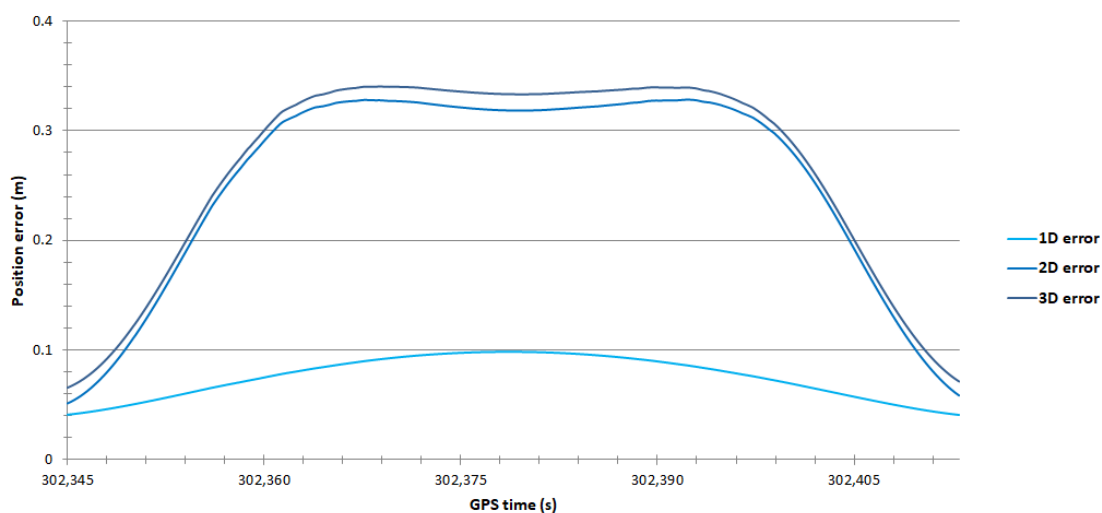


Figure 13. Variability in position errors recorded by the GNSS/INS system in the PP mode in section no. 3.

4. Discussion

The position error values obtained by the Ekinox2-U system are similar to (or even smaller than) the accuracy characteristics recommended by the SBG Systems. As for the non-built-up area, the 2DRMS(2D) measure was 5.4 cm (RTK) and 1.8 cm (PP), while the R95(2D) measure was 2.8 cm (RTK) and 1.7 cm (PP). As regards the area in which numerous terrain obstacles were found, e.g., multi-storey buildings or trees several metres tall, the 2DRMS(2D) measure was 96.1 cm (RTK) and 32.6 cm (PP), while the R95(2D) measure was 60 cm (RTK) and 24.6 cm (PP). For the tunnel, where there was no access to the GNSS signal for more than 60 s, the 2DRMS(2D) measures were 4.829–5.86 m (RTK) and 54.3–85.9 cm (PP), while the R95(2D) measures were 4.811–5.886 m (RTK) and 32.8–64 cm (PP).

Also note that the GNSS/INS data, which were converted in the post-processing mode, allowed the measurement accuracies to be considerably higher than in real-time. Where there was access to the GNSS signal, the 2DRMS(2D) and R95(2D) values increased by 1.5–3 times. However, where there was no access to the GNSS signal, the analysed position accuracy results decreased by up to several times.

5. Conclusions

This study has shown that the rapid development of GNSS/INS techniques, manifesting itself in recent years in the construction of new positioning systems and the modernisation of existing ones, as well as the implementation of new technical solutions for positioning, makes them usable for increasingly precise position determination, as well as in the kinematic mode.

Research has shown that GNSS/INS systems, which are supported by RTK receivers, can be used to carry out selected geodetic and construction tasks in railway engineering. The obtained measurement results indicate that the Ekinox2-U system can satisfy the accuracy requirements in the process of a rapid stocktaking of existing rail tracks (3 cm ($p = 0.95$)), as well as for design and construction works (10 cm ($p = 0.95$)), which is, however, determined by the type of terrain obstacles found in the test area. On the other hand, the system cannot be used to determine the place and extent of rail track deformations (1 cm, ($p = 0.95$)). The most important advantage of GNSS/INS systems over methods based only on GNSS systems is a significant increase (up to several times) in the positioning accuracy in signal-obstructed areas, such as tunnels.

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