

Article



Impact of Temperature and Nanoparticle Concentration on Turbulent Forced Convective Heat Transfer of Nanofluids

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Abstract: Theoretical analysis of the influence of nanoparticles and temperature on the average Nusselt (Nu) number and the average heat transfer coefficient (HTC) during the turbulent flow of nanofluid in a horizontal, round tube was carried out. The Nu number is a function of the Reynolds (Re) number and the Prandtl (Pr) number, which in turn are functions of the thermophysical properties of the liquid and the flow conditions. On the other hand, the thermophysical properties of nanoliquids are primarily a function of nanoparticle concentration (NPC) and temperature. Hence, the correct determination of the value of the Nu number, and then the HTC, which is needed for engineering calculations, depends on the accuracy of determining the thermophysical properties of nanofluids. In most cases, the thermophysical properties of the nanofluids are calculated as functions of the corresponding thermophysical properties of the base liquid. Therefore, the accuracy of the calculations of the thermophysical properties of nanofluids is equally determined by the reliable correlations for the base liquids. Therefore, new correlations for the calculation of the thermophysical properties of water have been developed. The results of calculations of the thermophysical properties of the base liquid (water) and the water-Al₂O₃ nanofluids by use of carefully selected correlations is presented. It was established that even for small concentrations of nanoparticles, a significant intensification of heat transfer using nanofluids as compared to the base liquid is obtained for the tested temperature range.

Keywords: nanofluids; thermophysical properties; forced convective heat transfer; horizontal tube

1. Introduction

Constant technological progress means that the heat fluxes that occur in devices are increasing. This presents a real challenge for heat transfer engineers and researchers. Two directions of intensification of heat transfer are being developed. The first is related to the modification of the heat exchange surface, e.g., [1–3]. The second is related to the search for new thermal fluids that are characterized by better thermophysical properties, such as thermal conductivity or contact angle. Among the new thermal fluids, the greatest hope is raised by a mixture of a base liquid and nanoparticles with a size below 100 nm, referred to as a nanofluid [4]. The use of nanofluids in a great number of areas is considered, such as single-phase systems, e.g., [5,6], two-phase systems, e.g., [7,8], magnetic nanofluids, e.g., [9,10], non-Newtonian nanofluids, e.g., [11,12], viscoelastic nanofluids, e.g., [13,14], chemical reaction systems, e.g., [15,16], bio-nanofluids, e.g., [17,18], nanofuels, e.g., [19,20], and others [21].

The single-phase convective heat transfer of nanofluids is of particular interest due to potential applications in many cooling/heating systems, e.g., heat exchangers, electronics, nuclear reactors, car radiators, solar devices, e.g., [22–25], medical applications, e.g., [26,27], thermal energy storage, e.g., [28,29], or even rocketry applications [30]. Although different aspects, e.g., flow regimes—laminar or turbulent, boundary conditions, nanoparticle type



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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). and concentration, of single-phase forced convection of nanofluids in tubes were studied both experimentally [31–34] and numerically [35–42] there is still controversy about the influence of nanoparticles on heat transfer efficiency and flow resistance. Experimental works show that the addition of nanoparticles can both intensify and deteriorate heat transfer. In turn, numerical works most often show the intensification of heat transfer as a result of adding nanoparticles. A similar controversy concerns flow resistance. Intensive work is still underway to determine the thermophysical properties of nanofluids and their stability [43,44].

The nanofluid, which is inherently a two-phase mixture of liquid and solid particles, can be modeled as a single-phase continuum (single phase fluid) with the thermophysical properties which take into account the effect of the presence of nanoparticles. The results of numerical simulations obtained with the single-phase approach and the two-phase model [45,46], did not differ significantly. The condition for the accuracy of the single-phase approach is the correct selection of the correlation on the thermophysical properties of nanofluids.

In the present study, a theoretical analysis of the influence of temperature and NPC during forced convection of nanofluids inside a horizontal circular tube is presented. It was assumed that the analyzed nanofluid can be treated as a homogeneous, single-phase liquid. The Nu number and average HTC were parameters of the intensity of the convective heat transfer. For forced convection, the Nu number is a function of the Re number and *Pr* number. The Re number and *Pr* number are functions of the thermophysical properties of nanofluids. The thermophysical properties of nanofluids due to variations of thermal conductivity, viscosity, density, and specific heat, which are functions of NPC and temperature. Water-based nanofluids with dispersed alumina (Al₂O₃) nanoparticles at mass concentrations of 0.1%, 1%, and 5% within the temperature range 20–70 °C are considered. Water-Al₂O₃ nanofluids were selected because frequent application in both numerical and experimental studies. Moreover, thermophysical properties of water-Al₂O₃ nanofluids are comprehensively and thoroughly investigated [47].

2. Materials and Methods

2.1. Tested Nanofluids

In this study alumina (Al₂O₃) nanoparticles were selected while distilled, deionized water was tested as base fluid. Alumina nanoparticles were tested at the concentration of 0.1%, 1%, and 5% by weight. It was assumed that nanoparticles have a spherical form with mean diameter of $d_p = 47$ nm.

The properties of alumina (Al₂O₃) nanoparticles are shown in Table 1.

Table 1. Properties of Al₂O₃ nanoparticles.

Thermal Conductivity k _p [W/(mK)]	Density ρ _p [kg/m ³]	Specific Heat c _{p,p} [J/(kg K)]
35 *	3600 **	765 **
*[48]; **[49].		

2.2. Correlations for Forced Convection Heat Transfer inside Horizontal Tubes

Recognized correlation equations used for the determination of an average Nu number for forced convection inside horizontal cylinders in base fluids are collected in Table 2. The Nu number for water is a benchmark to the values calculated for the analyzed nanofluids. Hence, the selection of the correct correlation is important when comparing the results for the base fluid and nanofluids.

Authors	Correlation	Range	Remarks	Equation
Dittus and Boelter [50]	$\overline{Nu} = 0.23 Re^{0.8} Pr^n$	$Re > 10^4$ 0.7 < Pr < 100	n = 0.4—heating n = 0.3—cooling	Equation (1)
Krauβold [51]	$\overline{Nu} = 0.032 Re^{0.8} Pr^n \left(\frac{L}{D}\right)^{-0.054}$	$Re > 10^{4}$	n = 0.37—heating n = 0.3—cooling	Equation (2)
Sieder and Tate [52]	$\overline{Nu} = 0.027 R e^{4/5} P r^{1/3} \left(\frac{\mu_f}{\mu_w}\right)^{0.14}$	$Re > 10^4$ 0.7 < Pr < 16,700	$T_w = \text{const.}$	Equation (3)
Mikhejev [53]	$\overline{Nu} = 0.021 Re^{0.8} Pr_f^{0.43} \left(\frac{Pr_f}{Pr_w}\right)^{0.25} \varepsilon_L$	$\begin{array}{l} 10^4 < Re < 5 \times 10^6 \\ 0.6 < Pr < 2500 \end{array}$	$\varepsilon_L = f(L/D, Re)$	Equation (4)
Petukhov [54]	$\overline{Nu} = \frac{(f/8)RePr}{1.07 + 12.7(f/8)^{\frac{1}{2}}(Pr^{\frac{2}{3}} - 1)}$	$\begin{array}{l} 10^4 < Re < 5 \times 10^6 \\ 0.5 < Pr < 2000 \end{array}$	$f = (1.82lnRe - 1.64)^{-2}$	Equation (5)
Notter and	$\overline{Nu} = 4.8 + 0.0156 Pe^{0.85} Pr^{0.08}$	$10^4 < Re < 10^6$	$T_w = \text{const.}$	Equation (6)
Sleicher [55]	$\overline{Nu} = 6.3 + 0.0167 Pe^{0.85} Pr^{0.08}$	0.004 < Pr < 0.1	$q_w = \text{const.}$	Equation (7)
Churchill and Ozoe [56]	$\overline{Nu} = \frac{0.3387Pr^{1/3}Re^{1/2}}{\left[1 + (0.0468/Pr)^{2/3}\right]^{1/4}}$	$\begin{array}{c} Re > 100 \\ 10^{-4} < Pr \rightarrow \infty \end{array}$	$q_w = \text{const.}$	Equation (8)
Hausen [57]	$Nu = 0.0235 \left[1 + \left(\frac{d}{L} \right)^{2/3} \right]$ $[Re^{0.8} - 230] Pr_f^{0.3} \left(\frac{\mu_f}{\mu_w} \right)^{0.14}$	$2300 < Re < 2 \times 10^{6}$ 1.5 < Pr < 500 d/L < 1		Equation (9)
Gnieliński [58]	$\overline{Nu} = \frac{(f/8)(Re-1000)Pr}{1+12.7(f/8)^{0.5}(Pr^{\frac{2}{3}}-1)}$	$3 \times 10^3 < Re < 5 \times 10^6$ 0.5 < Pr < 2000	$f = (0.79 ln Re - 1.64)^{-2}$	Equation (10)
Kutateladze [59]	$\overline{Nu} = 1.61 \left(Pe\frac{D}{L} \right)^{1/3}$	Pe > 12 d/L < 12		Equation (11)

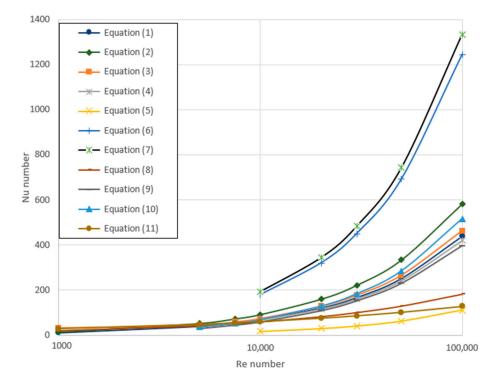
Table 2. Correlation equations for turbulent flow of base fluid.

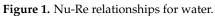
Figure 1 shows the dependence of the Nu number on the Re number on the basis of the correlations shown in Table 1. The calculations were performed for the Pr = 5. The values of the correction coefficients were assumed to be equal to one. Noteworthy is the fact that the values of the Nu number are significantly higher from the Notter and Sleicher correlation [55] compared to the other correlations. Note, however, that the Notter and Sleicher correlations (Equations (6) and (7)) are suitable for fluids with a very low *Pr* number. Figure 1 shows that the correlations proposed by Dittus and Boelter, Kraußold, Sieder and Tate, Mikhejew, Hausen, and Gnieliński give similar values of the Nu number, although the difference between the Kraußold correlation and Hausen correlation for $Re = 10^5$ is as much as 45%.

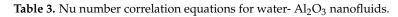
In Table 3 are collected experimental and numerical correlation equations used for determination of an average Nu number for forced convection inside horizontal cylinders in nanofluids.

Figure 2 shows the dependence of the Nu number on the Re number for nanofluids and correlations shown in Table 3. The calculations were performed for the Pr = 5, w = 1 m/s, $\varphi_v = 1\%$ and $d_p = 40$ nm.

As seen in Figure 2, except Equation (17), the correlations show pretty good consistency. The numerically developed correlation equation proposed by Saha and Paul, Equation (18), was selected for the analysis, as it fits the experimental data for water- Al_2O_3 nanofluids very well and contains parameters that characterize both nanoparticles and molecules of the base fluid.







Authors	Equation	Remarks	Equation
Xuan and Li [60]	$\overline{Nu} = 0.0059 \Big(1 + 7.6286 \varphi_v^{0.6886} Pe_p^{0.001} \Big) Re^{0.9238} Pr^{0.4}$	$Pe_p = rac{wd_p}{a_{nf}}$	Equation (12)
Vasu et al. [61]	$\overline{Nu} = 0.0256 \cdot Re^{0.8} Pr^{0.4}$	$10^4 < Re < 8 \times 10^4$	Equation (13)
Hussein et al. [62]	$\overline{Nu} = 0.02 \cdot Re^{0.788} Pr^{0.45}$	$5000 < Re < 5 \times 10^4 \\ 6.8 < Pr < 11.97$	Equation (14)
Sahin et al. [63]	$\overline{Nu} = 0.106 \cdot Re^{0.588} \cdot (1 + \varphi_v^{-0.1096}) \cdot Pr^{0.258}$	$\begin{array}{c} 4000 < Re < 20,000 \\ 5 < Pr < 7 \\ 0.5\% < \varphi_v < 4\% \end{array}$	Equation (15)
Chavan and Pise [64]	$\overline{Nu} = 0.508358 \cdot Re^{0.7401} \cdot Pr^{-0.7026}$	6000 < Re < 14,000 $0.3\% < \varphi < 1\%$	Equation (16)
Durga and Gupta [65]	$\overline{Nu} = 0.09589 \cdot Re^{0.8} \cdot Pr^{0.4} \cdot (1 + \varphi_v)^{2833}$	$\begin{array}{l} 3000 < Re < 30,000 \\ 5.12 < Pr < 6.54 \\ 0\% < \varphi_v < 0.03\% \end{array}$	Equation (17)
Saha and Paul [66]	$\overline{Nu} = 0.0126 Re^{0.85589} Pr^{0.44709} \left(\frac{d_f}{d_p}\right)^{-0.00176}$	$\begin{array}{c} 10^4 < Re < 10^5 \\ 8.45 < Pr < 20.29 \\ 4\% < \varphi_v < 6\% \\ 10 < d_p \ [nm] < 40 \end{array}$	Equation (18)

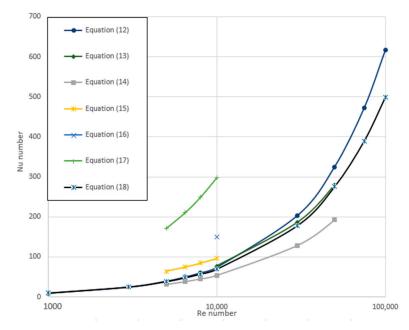


Figure 2. Nu-Re relationships for water-Al₂O₃ nanofluids.

2.3. Correlations for Thermophysical Properties of Nanofluids

A large number of correlations devoted to calculate viscosity of nanofluids are published in the literature, e.g., [67,68]. In Table 4 are shown correlations proposed for water- Al_2O_3 nanofluids.

Table 4. Correlations for viscosity of water- Al₂O₃ nanofluids.

Authors				Correla	ation				Remarks	Equation
Krieger and Dougherty [69]			$\mu_{nf} =$	$\mu_{bf} \Big(1 - 1 \Big)$	$\left(rac{\varphi_a}{\varphi_{vs}} ight)^{-2.5}$	φ_m)			φ_a volume fraction of aggregates $\varphi_a = \varphi_v (d_a/d_p)^{3-d_f}$ φ_v —volume fraction of the well-dispersed individual particles, d_a —diameter of aggregates, d_f —fractal dimension of aggregates φ_{vs} —volume fraction of densely packed spheres	Equation (19)
Palm et al. [70]					$^{-4}T + 2.9$ · $^{-4}T + 3.4$				$arphi_{v}=1\% \ arphi_{v}=4\%$	Equation (20) Equation (21)
Nguyen et al. [71]		μ_{bf}			$e^{0.148\varphi_v}\mu_{bf}$ 5·T + 0.00		f		$d_p = 47 \text{ nm}$ $\varphi_v = 4\%$	Equation (22) Equation (23)
Khanafer and Vafai [72]	$\mu_{nf}=-0$	$0.4491 + \frac{28}{23}$			$\frac{1634 \varphi_v^2 +}{\frac{\varphi_v^2}{d_p^2} - 3}$		+ 0.01	$32\varphi_{v}^{3} -$		Equation (24)
				$\mu_{nf} = e^{(A)}$	$+\frac{B}{T-To})$					
					ϕ_v					
Pastoriza- Gallego et al. [73]		0.000	0.005	0.010	0.015	0.021	0.031	0.048		
	A	-3.694	-3.632	-2.381	-1.702	-3.450	-3.302	-1.379		Equation (25)
	<i>B</i> [K]	999.0	999.0	689.3	534.7	999.0	999.0	518.4		
	T_o [K]	145.7	145.5	169.8	185.5	146.2	145.3	189.9		

Table 4. Cont.

Authors	Correlation	Remarks	Equation
Corcione [74]	$\mu_{nf} = \mu_{bf} \left(\frac{1}{1 - 34.87 \left(\frac{d_p}{d_f}\right)^{-0.3} \varphi_v^{1.03}} \right)$	$\begin{array}{l} d_{f} &\text{equivalent diameter of liquid} \\ & \text{molecule} \\ d_{f} & = 0.1 \Big(\frac{6M}{N\pi\rho_{fo}}\Big)^{1/3} \\ M &\text{molecular weight of water} \\ N &\text{Avogadro number} \\ \rho_{fo} & -\text{ density of water at} \\ T_{o} & = 293 \text{ K} \end{array}$	Equation (26)

The correlation proposed by Corcione, Equation (26), was selected for the analysis, as it fits the experimental data of the viscosity of water- Al_2O_3 nanofluids very well.

Equally important as reliable correlations for nanofluids are the formulas for calculating the properties of base liquids. Tested correlations for calculation viscosity of water are shown in Table 5.

Table 5. Correlations for viscosity of water.

Authors	Correlation	Range	Equation
Minea et al. Equation (31) in [36]	$ \mu_{bf} = 1.055787 - 0.0132897 \cdot T + 0.00006309 \cdot T^2 - 1.33730666 \cdot 10^{-7} \cdot T^3 - 1.06666666 \cdot 10^{-10} \cdot T^4 $	294 < T < 344	Equation (27)
Chon and Khim [75]	$\mu_{bf} = 2.414 \cdot 10^{-5} \cdot 10^{\frac{247.8}{T-140}}$	294 < T < 344	Equation (28)
Purohit et al. [76]	$\mu_{bf} = 999.79 + 0.068 \cdot t - 0.0107 \cdot t^2 + 0.00082 \cdot t^{2.5} - 2.303 \cdot 10^{-5} \cdot t^3$	300 < T < 350	Equation (29)
Saeed and Dulaimi [77]	$ \begin{aligned} \mu_{bf} &= 0.414092804247831 - \\ 4.792184560427 \cdot 10^{-3}T + 2.0927097596 \cdot 10^{-5}T^2 - \\ 4.0781184 \cdot 10^{-8}T^3 + 2.9885 \cdot 10^{-11} \cdot T^4 \end{aligned} $		Equation (30)
Present work [78]	$\mu_{bf} = 2.2551419 - 0.033948 \cdot T + 0.0002053 \cdot T^2 - 6.229 \cdot 10^{-7} \cdot T^3 + 9.4741 \cdot 10^{-10} \cdot T^4 - 5.775 \cdot 10^{-13} \cdot T^5$	283 < T < 343	Equation (31)

Figure 3 shows the viscosity of water against temperature calculated from correlations presented in Table 5. As seen in Figure 3, predictions realized with Equation (27) deviate by about 20% for minimum temperature 20 °C. Higher temperature difference between predictions is negligible.

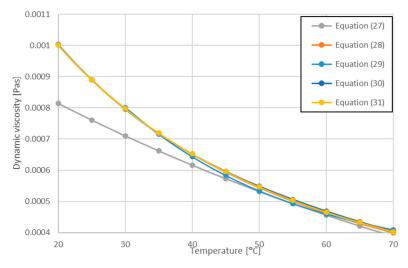


Figure 3. Viscosity of water.

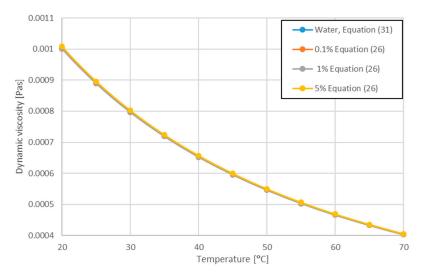


Figure 4 shows influence of NPC on the viscosity of the tested nanofluids against temperature, calculated by the use of Equation (26) in combination with Equation (31).

Figure 4. Viscosity of water-Al₂O₃ nanofluids.

As seen in Figure 4, viscosity of the tested nanofluids decreases sharply with a temperature increase and slightly increases with NPC increase. The slight influence of nanoparticles on the viscosity of the tested nanofluids is due to the very small used NPC.

Similarly to viscosity several correlations devoted to thermal conductivity of nanofluids are published in literature, e.g., [79,80]. In Table 6 are collected correlations proposed for water- Al_2O_3 nanofluids.

Table 6. Correlations for thermal conductivity of water- Al₂O₃ nanofluids.

Authors	Correlation	Remarks	Equation
Khanafer and Vafai [72]	$k_{nf} = k_{bf} \left(0.9843 + 0.398 \varphi_v^{0.7383} \left(\frac{1}{d_p} \right)^{0.2246} \\ \left(\frac{\mu_{nf}}{\mu_{bf}} \right)^{0.0235} - 3.9517 \frac{\varphi_v}{t} + 34.034 \frac{\varphi_v^2}{t^3} + 32.509 \frac{\varphi_v}{t^2} \right)$	water-Al ₂ O ₃ $0.01 \le \varphi_v \le 0.09$ $20 \le t[^{\circ}C] \le 70$ $13 \text{ nm} \le d_p \le 131 \text{ nm}$	Equation (32)
Corcione [74]	$k_{nf} = k_{bf} \left(1 + 4.4 R e_p^{0.4} P r^{0.66} \left(\frac{T}{T_{fr}}\right)^{10} \left(\frac{\lambda_p}{\lambda_f}\right)^{0.03} \varphi_v^{0.66}$	Re_{p} —Re number based on nanoparticle diameter $Re_{p} = \frac{\rho_{bf}u_{B}d_{p}}{\mu_{bf}}$ u_{B} —Brownian velocity of the nanoparticle $u_{B} = \frac{2k_{b}T}{\pi\mu_{bf}d_{p}^{2}}$	Equation (33)
Chen [81]	$k_p = k_{nf} rac{0.75 d_p / l_p}{0.75 d_p / l_p + 1}$	<i>l_p</i> —mean free path of nanoparticle	Equation (34)
Hassani et al. [82]	$\begin{aligned} k_{nf} &= k_{bf} \left(1.04 + \varphi_{V}^{1.11} \left(\frac{k_{p}}{k_{bf}} \right)^{0.33} P_{r}^{-1.7} \\ & \left[\frac{1}{P_{r}^{-1.7}} - \frac{262}{\left(\frac{k_{p}}{k_{bf}}\right)^{0.33}} + \left(135 \left(\frac{d_{ref}}{d_{p}} \right)^{0.23} \left(\frac{v_{bf}}{d_{p}u_{Br}} \right)^{0.82} \right) \left(\frac{c_{p}}{T^{-1} - u_{Br}^{2}} \right)^{-0.1} \left(\frac{T_{B}}{T} \right)^{-7} \right] \right] \end{aligned}$	Various base fluids, metal and oxide nanoparticles	Equation (35)
Sawicka et al. [83]	$k_{nf} = k_{bf} \left(1 + 0.1046 \varphi_m^{0.2388} \left(\frac{100}{d_p} \right)^{3.14 \cdot 10^{-3}} \right)$		Equation (36)

The correlation proposed by Corcione, Equation (33), was selected for the analysis, as it fits the experimental data of the thermal conductivity of water-Al₂O₃ nanofluids very well, as it takes into account the influence of Brownian motion on the thermal conductivity of nanofluids.

Authors Correlation Range Equation Minea et al. $k_{bf} = -0.98249 \cdot 10^{-5} \cdot T^2 + 7.535211 \cdot 10^{-3} \cdot T - 0.76761$ Equation (22) in 294 < T < 344Equation (37) [36] Minea et al. 294 < T < 344Equation (30) in Equation (38) $8.63331959 \cdot 10^{-18} \cdot T^3 + 7.301424 \cdot 10^{-21} \cdot T^4$ [36] $k_{bf} = 0.56112 + (0.00193 \cdot t) - (2.601 \cdot 10^{-6} \cdot t^2) - (6.08 \cdot 10^{-8} \cdot t^3)$ Purohit [76] 300 < T < 350Equation (39) Saeed and Dulaimi $k_{bf} = -0.46662403 + 0.00575419 \cdot T - 7.18 \cdot 10^{-6} \cdot T^2$ Equation (40) [77] $k_{bf} = 27.689 - 0.415 \cdot T + 0.000249 \cdot T^2 - 7.389 \cdot 10^{-6} \cdot T^3 + 0.000249 \cdot T^2 - 7.000249 \cdot T^2 + 0.000249 \cdot T^2$ Present work [78] 283 < T < 343Equation (41) $1.0839{\cdot}10^{-8} - 6.3292{\cdot}10^{-12}$

Correlations for calculation thermal conductivity of water are shown in Table 7.

	Table 7.	Correlations	for thermal	conductivity	of water.
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Figure 5 shows thermal conductivity of water against temperature calculated from correlations presented in Table 7.

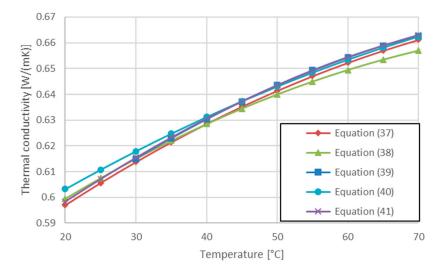


Figure 5. Thermal conductivity of water.

Figure 6 shows influence of NPC on the thermal conductivity of the tested nanofluids against temperature calculated by use of Equation (33) in combination with Equation (41). As seen in Figure 6 thermal conductivity of the tested nanofluids increases moderately

with temperature increase and for given temperature increases with NPC increase.

The density of nanofluids is generally calculated by the use of the mixture model (Table 8).

The correlation proposed by Pak and Cho, Equation (43), was selected for the analysis, as it fits the experimental data of the density of water- Al_2O_3 nanofluids very well and is based on the general mixture theory.

Density of pure water can be estimated by use of correlations given in Table 9.

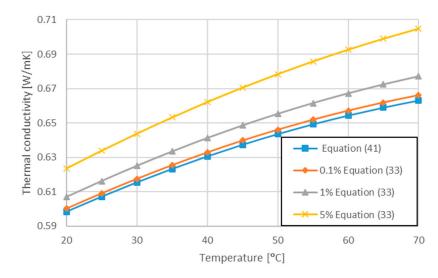


Figure 6. Thermal conductivity of water-Al $_2O_3$ nanofluids.

Table 8. Correlations for density of nanofluids.

Authors	Correlation	Remarks	Equation
Khanafer and Vafai [72]	$ ho_{nf} = 1001.064 + 2738.6191 arphi_v - 0.2095 \cdot t$	$egin{array}{l} ext{water-Al}_2 ext{O}_3 \ 0 \leq arphi_v \leq 0.04 \ 5 \leq t [^\circ ext{C}] \leq 40 \end{array}$	Equation (42)
Pak and Cho [84]	$\rho_{nf} = \varphi_v \rho_p + (1 - \varphi_v) \rho_{bf}$	Mixture model	Equation (43)
Sharifpur et al. [85]	$ ho_{nf,nl} = rac{ ho_{nf}}{(1-arphi_v)+arphi_v (r_p+t_v)^3/r_p^3}$	r_p —radius of nanoparticle t_v —nanolayer thickness $t_v = -0002833r_p^3 + 0.0475r_p - 0.1417$	Equation (44)

 Table 9. Correlations for density of water.

Autors	Correlation	Range	Equation
Minea et al. Equation (20) in [36]	$\begin{split} \rho_{bf} &= -2.0546 \cdot 10^{-10} \cdot T^5 + 4.0505 \cdot 10^{-7} \cdot T^4 - \\ 3.1285 \cdot 10^{-4} \cdot T^3 + 0.11576 \cdot T^2 - 20.674 \cdot T + 2446 \end{split}$		Equation (45)
Minea et al. Equation (28) in [36]	$\begin{split} \rho_{bf} &= -413.15683 + 13.24245 \cdot T - 0.040578 \cdot T^2 + \\ & 0.00004 \cdot T^3 - 2.27018 \cdot 10^{-17} \cdot T^4 \end{split}$		Equation (46)
Purohit et al. [76]	$\rho_{bf} = 999.79 + 0.068 \cdot t - 0.0107 \cdot t^2 + 0.00082 \cdot t^{2.5} - 2.303 \cdot 10^{-5} \cdot t^3$	300 < T < 350	Equation (47)
Saeed and Dulaimi [77]	$\rho_{bf} = 765.33 + 1.8142 \cdot T - 0.0035 \cdot 10^{-2} \cdot T^2$		Equation (48)
Present work [78]	$\rho_{bf} = -5859.3637 + 98.96855 \cdot T + 0.574747 \cdot T^2 + 0.0016856 \cdot T^3 - 2.4989 \cdot 10^{-6} \cdot T^4 - 1.4908 \cdot 10^{-9} \cdot T^5$		Equation (49)
Saha and Paul [86]	$\rho_{bf} = 330.12 + 5.92 \cdot T - 1.63 \cdot 10^{-2} \cdot T^2 + 1.33 \cdot 10^{-5} \cdot T^3$	278 < T < 363	Equation (50)

Figure 7 shows the density of water against temperature calculated from correlations presented in Table 9. The maximum difference between the predictions is equal to 0.4%.

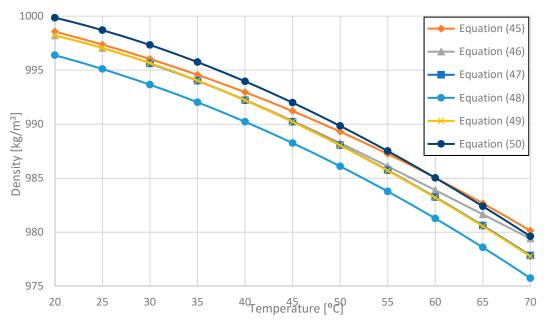
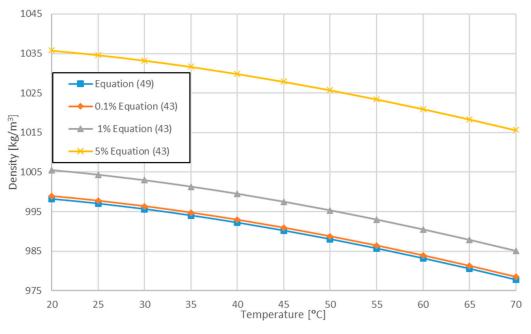
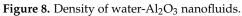


Figure 7. Density of water.

Figure 8 illustrates influence of the NPC on density of the tested nanofluids as a function of temperature by use of Equations (43) and (49).





As seen in Figure 8, the density of the analysed nanofluids decreases with temperature increase and increases with NPC increase because the density of the nanoparticle material (Table 1) is higher than density of water.

Several investigators have been involved in the physics of the specific heat of nanofluids [87–89]. In Table 10 are collected correlations proposed for water-Al₂O₃ nanofluids.

Authors	Correlation	Remarks	Equation
Pak and Cho [84]	$c_{p,nf} = \varphi_v c_{p,p} + (1 - \varphi_v) c_{p,bf}$	Mixture model	Equation (51)
Williams et al. [90]	$c_{p,nf} = \frac{\rho_{bf}c_{p,bf}(1-\varphi_v) + \varphi_v\rho_pc_{p,p}}{\rho_{bf}}$	water-Al ₂ O ₃ , water-ZrO ₂	Equation (52)
Corcione et al. [91]	$c_{p,nf} = \frac{(1-\varphi_v)(\rho c_p)_{bf} + \varphi_v(\rho c_p)_p}{(1-\varphi_v)\rho_{bf} + \varphi_v\rho_p}$	water-Al ₂ O ₃ , water-CuO, water-TiO ₂	Equation (53)
Sekhar and Sharma [92]	$c_{p,nf} = c_{p,H_2O} \left[0.8429 \left(1 + \frac{t}{50} \right)^{-0.3037} \\ \left(1 + \frac{d_p}{50} \right)^{0.4167} \left(1 + \frac{\varphi_v}{100} \right)^{2.272} \right]$	water-Al ₂ O ₃ , water-CuO, water-TiO ₂ , water-SiO ₂ $0.01\% \le \varphi_v \le 4\%$, $20 \le t[^{\circ}C] \le 50$, $15 \text{ nm} \le d_p \le 50 \text{ nm}$	Equation (54)

Table 10. Correlations for specific heat of nanofluids.

The correlation proposed by Williams et al. [90] was selected for the analysis. As shown in [49] Equation (52) much better fits the experimental data of the specific heat of water- Al_2O_3 nanofluids than Equation (51) based on the mixture theory. The better accuracy of Equation (52) results from the assumption of thermal equilibrium between the particles and the liquid, which does not have to be present due to the Brownian motion of nanoparticles and different thermophysical properties of the nanoparticle material and the base liquid.

The specific heat of water can be estimated by use of correlations given in Table 11.

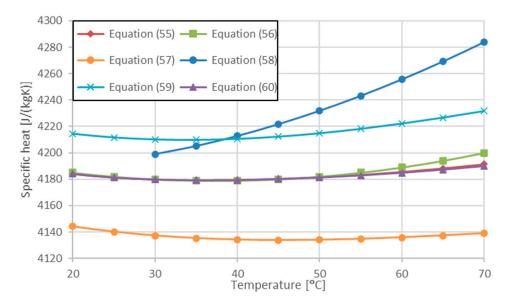
Authors	Correlation	Range	Equation
Minea et al. Equation (21) in [36]	$c_{p,bf} = -2.0546 \cdot 10^{-10} \cdot T^5 + 4.0505 \cdot 10^{-7} \cdot T^4 - 3.1285 \cdot 10^{-4} \cdot T^3 + 0.11576 \cdot T^2 - 20.674 \cdot T + 2446$	293 < T < 313	Equation (55)
Minea et al. Equation (25) in [36]	$\begin{split} c_{p,bf} &= 6108.94345 - 12.426 \cdot T + 0.02 \cdot T^2 - \\ &5.540012 \cdot 10^{-12} \cdot T^3 + 6.25929269 \cdot 10^{-21} \cdot T^4 \end{split}$	293 < T < 313	Equation (56)
Saha and Paul [66]	$c_{p,bf} = 10.01 - 5.14 \cdot 10^{-2} \cdot T + 1.49 \cdot 10^{-4} \cdot T^2 - 2.62 \cdot 10^{-12} \cdot T^3$	278 < T < 363	Equation (57)
Purohit et al. [76]	$c_{p,bf} = 4217.4 - 5.61 \cdot T + 1.299 \cdot T^{1.52} - 0.11 \cdot T^2 + 4149.6 \cdot 10^{-6} \cdot T^{2.5}$	300 < T < 350	Equation (58)
Saeed and Dulaimi [77]	$c_{p,bf} = 10444.58656104 - 54.08920728 \cdot T + 0.15359377 \cdot T^2 - 0.00014301 \cdot T^3$		Equation (59)
Present work [78]	$\begin{split} c_{p,bf} &= 185614 - 2737 \cdot T + 16.54446 \cdot T^2 - 0.5006 \cdot T^3 + \\ & 7.58 \cdot 10^{-5} \cdot T^4 - 4.5942 \cdot 10^{-8} \cdot T^5 \end{split}$	283 < T < 343	Equation (60)

Table 11. Correlations for specific heat of water.

Figure 9 shows the specific heat of water against temperature calculated from correlations presented in Table 11. The difference between the individual correlations seems large, but for 70 $^{\circ}$ C it does not exceed 3.4%.

As seen in Figure 10, the specific heat of water- Al_2O_3 nanofluids decreases with temperature increases, and for the given temperature decreases with NPC increases because the specific heat of the nanoparticle material (Table 1) is lower than the specific heat of water. It is *worthy to note* the non-monotonic course of specific heat for water-based nanofluids against the temperature that results from the data for water (Figure 9).

Figure 11 illustrates the influence of NPC on thermal diffusivity of the tested nanofluids as a function of temperature. The thermal diffusivity of water was calculated by the use of present correlations, i.e., Equations (41), (49) and (60), while thermal diffusivity of nanofluids was determined by use of Equations (33), (43) and (52). As seen in Figure 11, the thermal diffusivity of water and nanofluids increases with temperature increase, however



the growth rate is higher for nanofluids. Moreover, thermal diffusivity increases with NPC increase.

Figure 9. Specific heat of water.

Figure 10 illustrates influence of NPC on the specific heat of the tested nanofluids as a function of temperature calculated by the use of Equation (52) in combination with Equation (60).

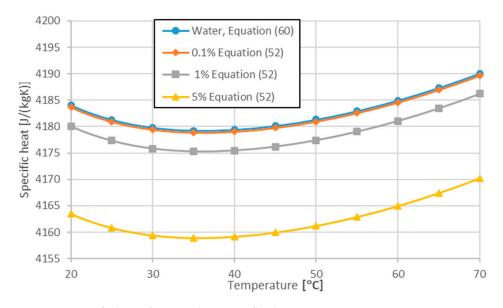


Figure 10. Specific heat of water-Al₂O₃ nanofluids.

As seen in Figure 12, the thermal diffusivity of the tested nanofluids increases slightly with NPC, although the rate of growth increases with temperature increase.

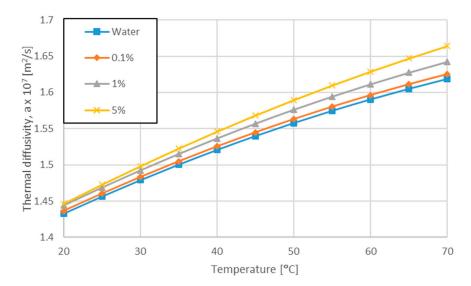


Figure 11. Thermal diffusivity of water-Al₂O₃ nanofluids.

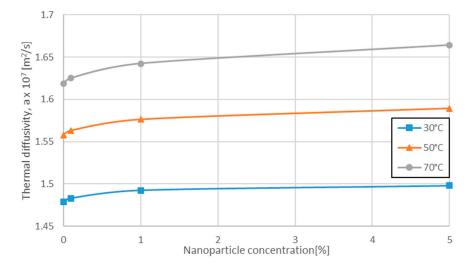


Figure 12. Thermal diffusivity of water-Al₂O₃ nanofluids.

3. Results and Discussion

3.1. Variation of Pr Number

Figure 13 shows a comparison of Pr numbers of the water-Al₂O₃ nanofluids as a function of temperature. The Pr number for water was calculated by use of present correlations, i.e., Equations (31), (41), (49) and (60), while the Pr number of nanofluids was determined by use of Equations (26), (33), (43) and (52). For the tested nanofluids, the Pr number decreases with an increase in temperature, predominantly due to the decrease in viscosity (Figure 4).

Figure 14 illustrates the influence of NPC on Pr number of the tested nanofluids at three temperatures, namely 30 °C, 50 °C, and 70 °C. As seen in Figure 12, the Pr number for water-Al₂O₃ decreases slightly with the NPC increase. Regardless of the temperature, the decrease in Pr number with the increase in NPC does not exceed 3%.

As shown in Figures 13 and 14, the Pr number decreases with both temperature increase and NPC increase. However, the decrease due to the increase in NPC for a given temperature is small, and the decrease due to the increase in temperature is very large for a given NPC. The Pr number of the nanofluid for the tested range of temperature and NPC is determined by the temperature, not by the NPC. As it results from the correlations presented in Table 2, the Nu number is a function of Pr^m , hence the higher the value of the Pr number, the higher the value of the Nu number.

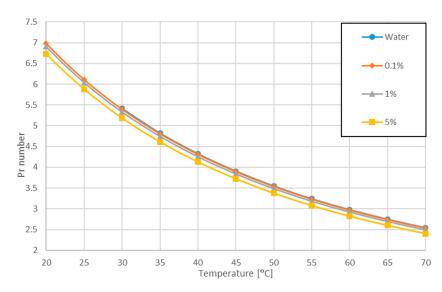


Figure 13. Prandtl number for water-Al₂O₃ nanofluids.

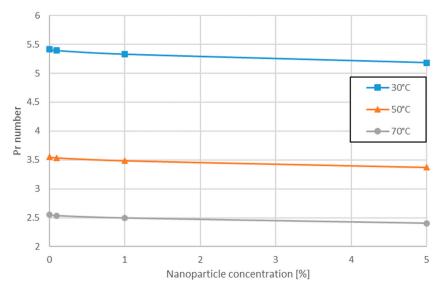


Figure 14. Variation of *Pr* number for water-Al₂O₃ nanofluids.

3.2. Variation of Re Number

Figure 15 illustrates the change of Re number versus temperature for the tested nanofluids. In this case the average velocity and the diameter of the horizontal tube are held constant at the values taken from the experiment presented in [93], i.e., w = 1 m/s, D = 10 mm. The Re number for water was calculated by use of present correlations, i.e., Equations (31) and (49), while the Re number of nanofluids was determined by use of Equations (26) and (43).

As seen in Figure 15 Re number definitively increases with temperature increase, which also results in increase of the Nu number.

Figure 16 shows the change of Re number against NPC for selected temperatures. It is observed that an increase in NPC results in a gradual increase of Re number for all tested temperatures.

As shown in Figures 15 and 16, Re number increases with both temperature increase and NPC increase. However, the increase due to the increase in NPC for a given temperature is small, and the increase due to the increase in temperature is substantial. It follows that the value of the Re number in the studied temperature and NPC range is primarily determined by temperature, and the influence of NPC is modest.

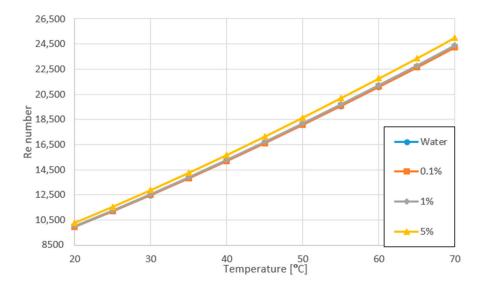


Figure 15. Variation of Re number for water-Al₂O₃ nanofluids.

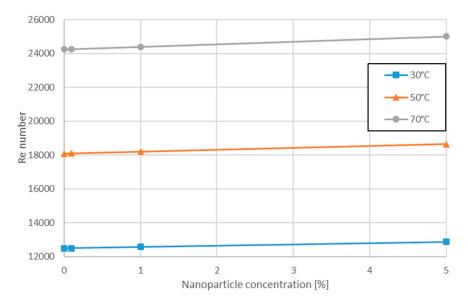


Figure 16. Variation of Re number for water-Al₂O₃ nanofluids.

3.3. Variation of Nu Number

Figure 17 shows the variation of Nu number against temperature for water-Al₂O₃ nanofluids predicted from the Saha and Paul correlation, Equation (18). Results are compared to the predictions for water from the commonly accepted Gnieliński correlation, Equation (10). Calculations for water were conducted by the use of present correlations for thermophysical properties of water. As seen in Figure 17, Nu number increases with temperature increase. For the tested NPC range $0.1\% \le \varphi_m \le 5\%$ Nu number for nanofluids is higher than for pure water. It means that the addition of Al₂O₃ nanoparticles to water results in substantial heat transfer improvement.

The influence of nanoparticles on the Nu number is clearer in Figure 18. Figure 18 shows the variation of the Nu number against NPC for water-Al₂O₃ nanofluids and three selected temperatures, namely 30 °C, 50 °C, and 70 °C. As seen in Figure 18, the addition of even the smallest amount of nanoparticles ($\varphi_m = 0.001$) causes a sharp increase in the Nu number. However, the Nu number increase for $\varphi_m > 0.001$ is negligible, and the increase in the Nu number is practically due to the increase in temperature.

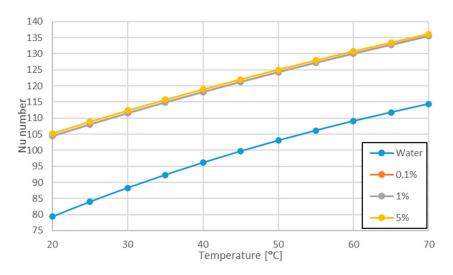


Figure 17. Variation of Nu number for water-Al₂O₃ nanofluids.

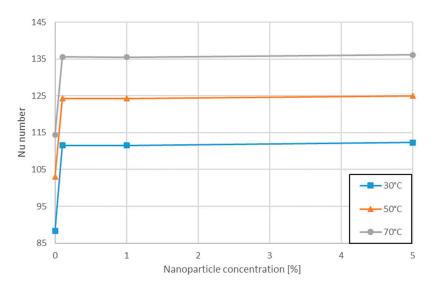


Figure 18. Variation of Nu number for water-Al₂O₃ nanofluids.

3.4. Variation of Heat Transfer Coefficient

Figure 19 shows the variation of heat transfer coefficient against temperature for water-Al₂O₃ nanofluids predicted from the Saha and Paul correlation (Equation (18)). The results are compared to the predictions from the Gnieliński correlation (Equation (10)) for water. As seen in Figure 19, heat transfer coefficient increases with temperature. For the tested mass concentration range $0.1\% \le \varphi_m \le 5\%$ heat transfer coefficient for nanofluids is higher than for water. It means that addition of Al₂O₃ nanoparticles to water results in substantial heat transfer improvement. In the literature, several mechanisms of heat transfer improvement in nanofluids have been discussed, e.g., [44,94]. According to Buongiorno [95], two mechanisms are responsible for heat transfer improvement in nanofluids, namely Brownian motion and thermophoresis.

Figure 20 shows variation of heat transfer coefficient against NPC for water-Al₂O₃ nanofluids and three selected temperatures, namely 30 °C, 50 °C and 70 °C. As seen in Figure 20, the influence of NPC on HTC for the tested mass concentration range $0.1\% < \varphi_m \le 5\%$ is negligible for the given temperature.

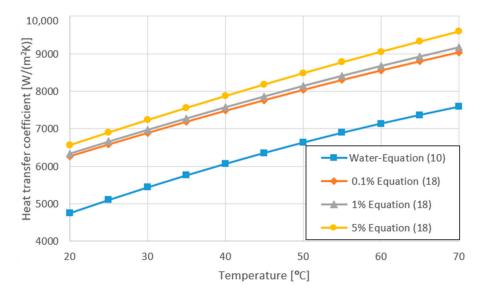


Figure 19. Variation of heat transfer coefficient for water-Al₂O₃ nanofluids.

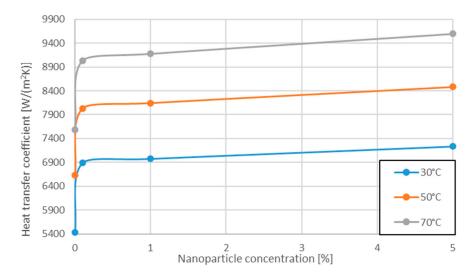


Figure 20. Variation of heat transfer coefficient for water-Al₂O₃ nanofluids.

As shown in Figures 19 and 20, HTC increases with both temperature increase and NPC increase. However, the increase due to the increase in NPC for a given temperature is small, and the increase due to the increase in temperature is significant. It is worth noting that maximum HTC increase is higher than Nu number increase and equals 38%, while for the Nu number it is 31%.

4. Conclusions

The analysis showed that the addition of Al₂O₃ nanoparticles with a mass concentration of $0.1\% \le \varphi_m \le 5\%$ within the temperature range of 20–70 °C to water as a base liquid causes the intensification of heat transfer under conditions of turbulent forced convection in round tubes.

The slight influence of the studied concentration of nanoparticles on the thermophysical properties of nanofluids indicates that the intensification of heat transfer results from the transport mechanisms, and not from the improvement of the thermophysical properties of nanofluids. Author Contributions: Conceptualization, J.T.C.; methodology, J.T.C. and S.S.; software, D.L.; validation, J.T.C.; formal analysis J.T.C. and S.S.; investigation, D.L.; data curation, D.L.; writing—original draft preparation, J.T.C.; writing—review and editing, J.T.C. and S.S.; funding acquisition, S.S. All authors have read and agreed to the published version of the manuscript.

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Nomenclature

а	Thermal diffusivity	(m^2/s)
c _p	Specific heat	(J/(kgK))
d_f	Base fluid molecule diameter	(m) (mgr())
d_p	Particle diameter	(m)
D	Inside diameter of tube	(m)
f	Friction factor	(-)
h	Local heat transfer coefficient	$(W/(m^2 K))$
$\frac{h}{h}$	Average heat transfer coefficient	$(W/(m^2 K))$
k	Thermal conductivity	(W/(m K))
L	Length	(m)
$Nu = \frac{hD}{k}$	Local Nusselt number	(-)
$\overline{Nu} = \frac{\overline{hD}}{k}$	Average Nusselt number	(-)
Pe = RePr	Peclet number	(-)
$Pe_p = \frac{wd_p}{a_{nf}}$	Peclet number related to d _p	(-)
$Pr = \frac{v}{a}$	Prandtl number	(-) (141 (- 2)
q D wD	Heat flux	(W/m^2)
$Re = \frac{wD}{v}$	Reynolds number	(-)
t T	Temperature	[°C]
Т	Temperature	[K]
W	Velocity	(m/s)
x Currels courses les	Axial coordinate	(m)
Greek symbols	Dumanaia visassitu	(Dec)
μ ν	Dynamic viscosity	(Pas) (m ² /s)
	Kinematic viscosity	(hr / s) (kg/m^3)
ρ	Density Nanoparticle concentration	
φ Subcerinte	Nanoparticle concentration	(-)
Subscripts bf	Base fluid	
f	Fluid	
) m	Mass	
nf	Nanofluid	
nj	Nanolayer	
p	Particle	
P V	Volume	
w	Wall	
Abbreviations	• • •	
HTC	Heat transfer coefficient	
NPC	Nanoparticle concentration	
	1	

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